

Package ‘BAMBI’

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bridgesampling

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add_burnin_thin	<i>Add (extra) burnin and thin to angmcmc object after original run</i>
-----------------	---

Description

Add (extra) burnin and thin to angmcmc object after original run

Usage

```
add_burnin_thin(object, burnin.prop = 0, thin = 1)
```

Arguments

object	angmcmc object
burnin.prop	proportion of iterations to used for burnin. Must be a be a number in [0, 1]. Default is 0.5.
thin	thining size to be used. Must be a positive integer. If thin = n, then every nth iteration is retained in the final MCMC sample.

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
lpdtrace(fit.vmsin.20)
# Now add extra burn-in
fit.vmsin.20.burn <- add_burnin_thin(fit.vmsin.20, 0.3)
lpdtrace(fit.vmsin.20.burn)
```

AIC.angmcmc	<i>AIC and BIC for angmcmc objects</i>
-------------	--

Description

AIC and BIC for angmcmc objects

Usage

```
## S3 method for class 'angmcmc'
AIC(object, ..., k = 2)

## S3 method for class 'angmcmc'
BIC(object, ...)
```

Arguments

object	a fitted model object for which there exists a <code>logLik</code> method to extract the corresponding log-likelihood, or an object inheriting from class <code>logLik</code> .
...	additional argument to be passed to <code>logLik.angmcmc</code>
k	numeric, the <i>penalty</i> per parameter to be used; the default <code>k = 2</code> is the classical AIC.

Details

Note that `AIC.angmcmc` and `BIC.angmcmc` calls `logLik.angmcmc`, which calculates Bayes estimate of the log-likelihood and *not* the maximum likelihood. As such, care needs to be taken while using these quantities.

\hat{L} is estimated by the sample maximum obtained from the MCMC realizations.

Value

AIC computes the AIC and BIC computes BIC for `angmcmc` objects.

Examples

```
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)

AIC(fit.vmsin.20)
BIC(fit.vmsin.20)
```

`as.mcmc.list.angmcmc` *Create an mcmc.list object from an angmcmc object*

Description

Create an `mcmc.list` object from an `angmcmc` object

Usage

```
## S3 method for class 'angmcmc'
as.mcmc.list(x, ...)
```

Arguments

x	angmcmc object
...	unused

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)

# now convert it to mcmc.list
library(coda)
fit.vmsin.20.mcmc <- as.mcmc.list(fit.vmsin.20)
```

bestmodel	<i>Extracting angmcmc object corresponding to the best fitted model in stepwise fits</i>
-----------	--

Description

Extracting angmcmc object corresponding to the best fitted model in stepwise fits

Usage

```
bestmodel(step_object)
```

Arguments

step_object stepwise fitted object obtained from [fit_incremental_angmix](#).

Value

Returns an angmcmc object corresponding to the the best fitted model in step_object.

Examples

```
# illustration only - more iterations needed for convergence
set.seed(1)
fit.vmsin.step.15 <- fit_incremental_angmix("vmsin", tim8, start_ncomp = 1,
                                         max_ncomp = 3, n.iter = 15,
                                         n.chains = 1)

fit.vmsin.best.15 <- bestmodel(fit.vmsin.step.15)
fit.vmsin.best.15
```

`bridge_sampler.angmcmc`*Log Marginal Likelihood via Bridge Sampling for angmcmc objects*

Description

Log Marginal Likelihood via Bridge Sampling for angmcmc objects

Usage

```
## S3 method for class 'angmcmc'  
bridge_sampler(samples, ..., ave_over_chains = TRUE)
```

Arguments

<code>samples</code>	angmcmc object
<code>...</code>	additional argument passed to bridge_sampler
<code>ave_over_chains</code>	logical. Separately call bridge_sampler on each chain in the angmcmc object and then take the average? Defaults to TRUE. See details.

Details

Marginal likelihood is calculated by first converting the angmcmc object `samples` to an `mcmc.list` object, and then by passing the resulting `mcmc.list` object to [bridge_sampler](#). If variability across multiple chains (if any) are very different, then calling [bridge_sampler](#) separately for each chain usually provides more stable results; the final log ML is computed by averaging over chain specific MLs.

Examples

```
## Not run:  
library(future)  
library(parallel)  
plan(multiprocess)  
  
set.seed(100)  
MC.fit <- fit_angmix("vmsin", tim8, ncomp=3, n.iter=500,  
                    n.chains = 3)  
  
library(bridgesampling)  
bridge_sampler(MC.fit)  
  
## End(Not run)
```

circ_cor

Sample circular correlation coefficients

Description

Sample circular correlation coefficients

Usage

```
circ_cor(x, type = "js")
```

Arguments

x	two column matrix. NA values are not allowed.
type	type of the circular correlation. Must be one of "fl", "js", "tau1" and "tau2". See details.

Details

circ_cor calculates the (sample) circular correlation between the columns of x. Two parametric (the Jammalamadaka-Sarma (1988, equation 2.6) form "js", and the Fisher-Lee (1983, Section 3) form "fl") and two non-parametric (two versions of Kendall's tau) correlation coefficients are considered. The first version of Kendall's tau ("tau1") is based on equation 2.1 in Fisher and Lee (1982), whereas the second version ("tau2") is computed using equations 6.7-6.8 in Zhan et al (2017).

The cost-complexity for "js", "fl", "tau2" and "tau1" are $O(n)$, $O(n^2)$, $O(n^2)$ and $O(n^3)$ respectively, where n denotes the number of rows in x. As such, for large n evaluation of "tau1" will be slow.

References

- Fisher, N. I. and Lee, A. J. (1982). Nonparametric measures of angular-angular association. *Biometrika*, 69(2), 315-321.
- Fisher, N. I. and Lee, A. J. (1983). A correlation coefficient for circular data. *Biometrika*, 70(2):327-332.
- Jammalamadaka, S. R. and Sarma, Y. (1988). A correlation coefficient for angular variables. *Statistical theory and data analysis II*, pages 349-364.
- Zhan, X., Ma, T., Liu, S., & Shimizu, K. (2017). On circular correlation for data on the torus. *Statistical Papers*, 1-21.

Examples

```
# generate data from vmsin model
set.seed(1)
dat <- rvmsin(100, 2, 3, -0.8, 0, 0)
```

```
# now calculate circular correlation(s) between the 2 columns of dat
circ_cor(dat, type="js")
circ_cor(dat, type="fl")
circ_cor(dat, type="tau1")
circ_cor(dat, type="tau2")
```

circ_varcor_model	<i>Analytic circular variances and correlations for bivariate angular models</i>
-------------------	--

Description

Analytic circular variances and correlations for bivariate angular models

Usage

```
circ_varcor_model(model = "vmsin", kappa1 = 1, kappa2 = 1, kappa3 = 0,
  mu1 = 0, mu2 = 0, nsim = 10000, ...)
```

Arguments

model	bivariate angular model. Must be one of "vmsin", "vmcos", or "wnorm2".
kappa1, kappa2, kappa3	concentration and covariance parameters. Recycled to the same size. kappa3^2 must be $< \text{kappa1} * \text{kappa2}$ in the wnorm2 model (see rwnorm2 for a detailed parameterization of wnorm2).
mu1, mu2	mean parameters. Ignored as they do not play any role in the analytical formulas.
nsim	Monte Carlo sample size. Ignored if all of kappa1, kappa2 and $\text{abs}(\text{kappa3})$ are < 150 or if model = "wnorm2".
...	additional model specific argument

Details

The function computes the analytic circular variances and correlations (both Jammalamadaka-Sarma (JS) and Fisher-Lee (FL) forms) for von Mises sine, von Mises cosine and bivariate wrapped normal distributions.

For wnorm2, expressions for the circular variances, JS and FL correlation coefficients can be found in Mardia and Jupp (2009), Jammalamadaka and Sarma (1988) and Fisher and Lee (1983) respectively. For vmsin and vmcos these expressions are provided in Chakraborty and Wong (2018).

Because the analytic expressions in vmsin and vmcos models involve infinite sums of product of Bessel functions, if any of kappa1, kappa2 and $\text{abs}(\text{kappa3})$ is larger than or equal to 150, IID Monte Carlo with sample size nsim is used to approximate rho_js for numerical stability. From rho_js, rho_fl is computed using Corollary 2.2 in Chakraborty and Wong (2018), which makes

cost-complexity for the rho_f1 evaluation to be of order $O(\text{nsim})$ for vmsin and vmcos models. (In general, rho_f1 evaluation is of order $O(\text{nsim}^2)$).

In addition, for the vmcos model, when $-150 < \text{kappa3} < -1$ or $50 < \max(\text{kappa1}, \text{kappa2}, \text{abs}(\text{kappa3})) \leq 150$, the analytic formulas in Chakraborty and Wong (2018) are used; however, the reciprocal of the normalizing constant and its partial derivatives are all calculated numerically via (quasi) Monte carlo method for numerical stability. These (quasi) random numbers can be provided through the argument qrnd, which must be a two column matrix, with each element being a (quasi) random number between 0 and 1. Alternatively, if n_qrnd is provided (and qrnd is missing), a two dimensional sobol sequence of size n_qrnd is generated via the function `sobol` from the R package qrng. If none of qrnd or n_qrnd is available, a two dimensional sobol sequence of size 1e4 is used.

Value

Returns a list with elements var1, var2 (circular variances for the first and second coordinates), rho_f1 and rho_js (circular correlations). See details.

References

Fisher, N. I. and Lee, A. (1983). A correlation coefficient for circular data. *Biometrika*, 70(2):327-332.

Jammalamadaka, S. R. and Sarma, Y. (1988). A correlation coefficient for angular variables. *Statistical theory and data analysis II*, pages 349-364.

Mardia, K. and Jupp, P. (2009). *Directional Statistics*. Wiley Series in Probability and Statistics. Wiley.

Chakraborty, S. and Wong, S, W.K. (2018). On the circular correlation coefficients for bivariate von Mises distributions on a torus. arXiv e-print.

Examples

```
circ_varcor_model("vmsin", kappa1= 1, kappa2 = 2, kappa3 = 3)

# Monte Carlo approximation
set.seed(1)
dat <- rvmsin(1000, 1, 2, 3)
# sample circular variance
circ_var <- function(x)
  1 - mean(cos(x - atan2(mean(sin(x)), mean(cos(x)))) )
circ_var(dat[, 1])
circ_var(dat[, 2])
circ_cor(dat, "f1")
circ_cor(dat, "js")
```

 contour.angmcmc

Contour plot for angmcmc objects with bivariate data

Description

Contour plot for angmcmc objects with bivariate data

Usage

```
## S3 method for class 'angmcmc'
contour(x, fn = mean, show.data = TRUE, xpoints = seq(0,
  2 * pi, length.out = 100), ypoints = seq(0, 2 * pi, length.out = 100),
  levels, nlevels = 20, cex = 1, col = "red", ...)
```

Arguments

x	angular MCMC object (with bivariate data).
fn	function, or a single character string specifying its name, to evaluate on MCMC samples to estimate parameters. Defaults to mean, which computes the estimated posterior mean. Note that if fn = "MODE" (warning: not "mode") or fn = "MAP", then the maximum a posteriori estimate (MAP) is calculated.
show.data	logical. Should the data points be added to the contour plot? Ignored if object is NOT supplied.
xpoints	Points on the first (x-) coordinate where the density is to be evaluated. Default to seq(0, 2*pi, length.out=100).
ypoints	Points on the first (x-) coordinate where the density is to be evaluated. Default to seq(0, 2*pi, length.out=100).
levels	numeric vector of levels at which to draw contour lines; passed to the contour function in graphics.
nlevels	number of contour levels desired if levels is not supplied; passed to the contour function in graphics.
cex, col	graphical parameters passed to points in graphics for plotting the data points. Ignored if show.data == FALSE.
...	additional arguments to be passed to the function contour .

Details

contour.angmcmc is an S3 function for angmcmc objects that calls [contour](#) from graphics.

To estimate the mixture density required to construct the contour plot, first the parameter vector η is estimated by applying fn on the MCMC samples, yielding the (consistent) Bayes estimate $\hat{\eta}$. Then the mixture density $f(x|\eta)$ at any point x is (consistently) estimated by $f(x|\hat{\eta})$.

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)

# now create a contour plot
contour(fit.vmsin.20)
```

contour_model

Contourplot for bivariate angular mixture model densities

Description

Contourplot for bivariate angular mixture model densities

Usage

```
contour_model(model = "vmsin", kappa1, kappa2, kappa3, mu1, mu2,
             pmix = rep(1/length(kappa1), length(kappa1)), xpoints = seq(0, 2 * pi,
             length.out = 100), ypoints = seq(0, 2 * pi, length.out = 100), levels,
             nlevels = 20, xlab = "x", ylab = "y", col = "black", lty = 1, main,
             ...)
```

Arguments

model	bivariate angular model whose mixture is of interest. Must be one of "vmsin", "vmcos" and "wnorm2".
kappa1, kappa2, kappa3, mu1, mu2, pmix	model parameters and mixing proportions. See the respective mixture model densities (dvmsinmix , dvmcosmix , dwnorm2mix) for more details.
xpoints	Points on the first (x-) coordinate where the density is to be evaluated. Default to seq(0, 2*pi, length.out=100).
ypoints	Points on the first (x-) coordinate where the density is to be evaluated. Default to seq(0, 2*pi, length.out=100).
levels	numeric vector of levels at which to draw contour lines; passed to the contour function in graphics.
nlevels	number of contour levels desired if levels is not supplied; passed to the contour function in graphics.
xlab, ylab, col, lty, main	graphical parameters passed to contour .
...	additional model specific argument

densityplot.angmcmc *Density plots for angmcmc objects*

Description

Plot fitted angular mixture model density surfaces or curves.

Usage

```
## S3 method for class 'angmcmc'
densityplot(x, fn = mean, log.density = FALSE,
  xpoints = seq(0, 2 * pi, length.out = 35), ypoints = seq(0, 2 * pi,
  length.out = 35), plot = TRUE, show.hist = ifelse(log.density, FALSE,
  TRUE), theta = 30, phi = 30, shade = 0.01, expand = 0.5, xlab, ylab,
  zlab = ifelse(log.density, "Log Density", "Density"), main, ...)
```

Arguments

x	angmcmc object.
fn	function, or a single character string specifying its name, to evaluate on MCMC samples to estimate parameters. Defaults to mean, which computes the estimated posterior mean. Note that if fn = "MODE" (warning: not "mode") or fn = "MAP", then the maximum a posteriori estimate (MAP) is calculated.
log.density	logical. Should log density be used for the plot?
xpoints, ypoints	Points on the x and y coordinates (if bivariate) or only x coordinate (if univariate) where the density is to be evaluated. Each defaults to seq(0, 2*pi, length.out=100).
plot	logical. Should the density surface (if the fitted data is bivariate) or the density curve (if univariate) be plotted?
show.hist	logical. Should a histogram for the data points be added to the plot, if the fitted data is univariate? Ignored if data is bivariate.
theta, phi, shade, expand, xlab, ylab, zlab, main	graphical parameters passed to persp (if bivariate) or plot (if univariate). If the data is univariate, theta, phi, shade, expand are ignored, and zlab plays the role of ylab.
...	additional arguments passed to persp , if fitted data is bivariate, or to hist (if (show.hist == TRUE)), if the fitted data is univariate

Details

When plot==TRUE, densityplot.angmcmc calls [persp](#) or [plot](#) from graphics to draw the surface or curve.

To estimate the mixture density, first the parameter vector η is estimated by applying fn on the MCMC samples, yielding the (consistent) Bayes estimate $\hat{\eta}$. Then the mixture density $f(x|\eta)$ at any point x is (consistently) estimated by $f(x|\hat{\eta})$.

Note that `densityplot.angmcmc` **does not** plot the kernel density estimates of the MCMC parameters. (These plots can be obtained by first converting an `angmcmc` object to an `mcmc` object via [as.mcmc.list](#), and then by using `densplot` from package `coda` on the resulting `mcmc.list` object. Instead, `densityplot.angmcmc` returns the surface (if 2-D) or the curve (if 1-D) of the fitted model density evaluated at the estimated parameter vector (obtain through [pointest](#)).

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
# now create density surface with the default first 1/3 as burn-in and thin = 1
library(lattice)
densityplot(fit.vmsin.20)
# the viewing angles can be changed through the arguments theta and phi
# (passed to persp from graphics)
densityplot(fit.vmsin.20, theta = 45, phi = 45)

# Now fit a vm mixture model
# illustration only - more iterations needed for convergence
fit.vm.20 <- fit_vmmix(wind$angle, ncomp = 3, n.iter = 20,
                      n.chains = 1)
densityplot(fit.vm.20)
```

 DIC

Deviance Information Criterion (DIC) for angmcmc objects

Description

Deviance Information Criterion (DIC) for `angmcmc` objects

Usage

```
DIC(object, form = 2, ...)
```

Arguments

<code>object</code>	angular MCMC object.
<code>form</code>	form of DIC to use. Available choices are 1 and 2 (default). See details.
<code>...</code>	additional model specific arguments to be passed to DIC. For example, <code>int.displ</code> specifies integer displacement in <code>wnorm</code> and <code>wnorm2</code> models. See fit_wnormmix and fit_wnorm2mix for more details.

Details

Given a deviance function $D(\theta) = -2\log(p(y|\theta))$, and an estimate $\theta^* = (\sum \theta_i)/N$ of the posterior mean $E(\theta|y)$, where y denote the data, θ are the unknown parameters of the model, $\theta_1, \dots, \theta_N$ are MCMC samples from the posterior distribution of θ given y and $p(y|\theta)$ is the likelihood function, the (form 1 of) Deviance Information Criterion (DIC) is defined as

$$DIC = 2\left(\frac{\sum_{s=1}^N D(\theta_s)}{N} - D(\theta^*)\right)$$

The second form for DIC is given by

$$DIC = D(\theta^*) - 4\hat{var} \log p(y|\theta_s)$$

where for $i = 1, \dots, n$, $\hat{var} \log p(y|\theta)$ denotes the estimated variance of the log likelihood based on the realizations $\theta_1, \dots, \theta_N$.

Like AIC and BIC, DIC is an asymptotic approximation for large samples, and is only valid when the posterior distribution is approximately normal.

Value

Computes the DIC for a given `angmcmc` object

Examples

```
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
DIC(fit.vmsin.20)
```

d_fitted

Density and random deviates from an angmcmc object

Description

Density and random deviates from an `angmcmc` object

Usage

```
d_fitted(x, object, fn = mean, log = FALSE, ...)
```

```
r_fitted(n = 1, object, fn = mean, ...)
```

Arguments

x	vector, if univariate or a two column matrix, if bivariate, with each row a 2-D vector, (can also be a data frame of similar dimensions) of points where the densities are to be computed.
object	angular MCMC object. The dimension of the model must match with x.
fn	function, or a single character string specifying its name, to evaluate on MCMC samples to estimate parameters. Defaults to mean, which computes the estimated posterior mean. Note that if fn = "MODE" (warning: not "mode") or fn = "MAP", then the maximum a posteriori estimate (MAP) is calculated.
log	logical. Should the log density be returned instead?
...	additional arguments to be passed to the function.
n	number of observations to be generated.

Details

To estimate the mixture density, first the parameter vector η is estimated by applying fn on the MCMC samples (using the function [pointest](#)), yielding the (consistent) Bayes estimate $\hat{\eta}$. Then the mixture density $f(x|\eta)$ at any point x is (consistently) estimated by $f(x|\hat{\eta})$.

The random deviates are generated from the estimated mixture density $f(x|\hat{\eta})$.

Value

d_fitted gives a vector the densities computed at the given points and r_fitted creates a vector (if univariate) or a matrix (if bivariate) with each row being a 2-D point, of random deviates.

Examples

```
set.seed(1)
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
d_fitted(c(0,0), fit.vmsin.20)
r_fitted(10, fit.vmsin.20)
```

 extractsamples

Extract MCMC samples for parameters from an angmcmc object

Description

Extract MCMC samples for parameters from an angmcmc object

Usage

```
extractsamples(object, par.name, comp.label, chain.no, drop = TRUE, ...)
```

Arguments

object	angular MCMC object
par.name	vector of names of parameters for which point estimates are to be computed. If NULL, results for all parameters are provided.
comp.label	vector of component labels (positive integers, e.g., 1, 2, ...) for which point estimates are to be computed. If NULL, results for all components are provided.
chain.no	vector of chain numbers whose samples are to be used. in the estimation. By default all chains are used.
drop	logical. Should the dimension of the output be dropped, if par.name, comp.label or chain.no has a single level?
...	additional arguments to be passed to the function.

Details

The default for both par.name and comp.label are the all possible choices available in object.

Value

Returns a four dimensional array with

dimension 1 - model parameters and mixing proportions dimension 2 - components dimension 3 - MCMC iterations dimension 4 - chain number

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
# extract Markov chain realizations for kappa1 from component 1
extr_kappa1_1 <- extractsamples(fit.vmsin.20, "kappa1", 1)
# for kappa1 from component from all components
extr_kappa1 <- extractsamples(fit.vmsin.20, "kappa1")
# for all parameters in component 1
extr_1 <- extractsamples(fit.vmsin.20, comp.label = 1)
```

fit_angmix

Fitting Bivariate and univariate angular mixture models

Description

Fitting Bivariate and univariate angular mixture models

Usage

```
fit_angmix(model = "vmsin", data, ncomp, cov.restrict = "NONE",
  unimodal.component = FALSE, start_par = NULL, rand_start = rep(FALSE,
  n.chains), method = "hmc", perm_sampling = FALSE, n.chains = 3,
  chains_parallel = TRUE, return_llik_contri = FALSE, int.displ = 3,
  epsilon = 0.1, L = 10, epsilon.random = TRUE, L.random = FALSE,
  burnin.prop = 0.5, tune.prop = 1, thin = 1, propscale = 0.05,
  n.iter = 500, pmix.alpha = NULL, norm.var = 1000, autotune = TRUE,
  show.progress = TRUE, accpt.prob.upper, accpt.prob.lower,
  epsilon.incr = 0.05, L.incr = 0.075, tune.incr = 0.05,
  tune_ave_size = 100, kappa_upper = 150, kappa_lower = 1e-04,
  return_tune_param = FALSE, qrnd_grid = NULL, n_qrnd = NULL, ...)
```

Arguments

model	angular model whose mixtures are to be fitted. Available choices are "vmsin", "vmcos" and "wnorm2" for bivariate data, and "vm" and "wnorm" for univariate data.
data	data matrix (if bivariate, in which case it must have two columns) or vector. If outside, the values are transformed into the scale $[0, 2\pi)$.
ncomp	number of components in the mixture model. Must be a positive integer. vector values are not allowed. If <code>comp == 1</code> , a single component model is fitted.
cov.restrict	Should there be any restriction on the covariance parameter for a bivariate model. Available choices are "POSITIVE", "NEGATIVE", "ZERO" and "NONE". Note that "ZERO" fits a mixture with product components. Defaults to "NONE".
unimodal.component	logical. Should each component in the mixture model be unimodal? Only used if model is either "vmsin" or "vmcos". Defaults to FALSE.
start_par	list with elements pmix (ignored if <code>comp == 1</code>), together with kappa1, kappa2, mu1 and mu2, for bivariate models, and kappa and mu for univariate models, all being vectors of length same as ncomp. These provides the starting values for the Markov chain; with j -th component of each vector corresponding to the j -th component of the mixture distribution. If missing, the data is first clustered into ncomp groups either via k-means (after projecting onto a unit sphere), or randomly, depending on rand_start, and then moment estimators for components are used as the starting points. Note that a very wrong starting point can potentially lead the chain to get stuck at a wrong solution for thousands of iterations. As such, we recommend using the default option, which is k-means followed by moment estimation.
rand_start	logical. Should a random starting clustering be used? Must be either a scalar, or a vector of length ncomp, one for each chain. Ignored if start_par is supplied. See start_par for more details. Defaults to FALSE.
method	MCMC strategy to be used for the model parameters: "hmc" or "rwmh".
perm_sampling	logical. Should the permutation sampling algorithm of Fruhwirth-Schnatter (2001) be used? If TRUE, at every iteration after burnin, once model parameters and mixing proportions are sampled, a random permutation of 1, ..., ncomp

is considered, and components are relabelled according to this random permutation. This forced random label switchings may improve the mixing rate of the chage. However, (automated) tuning is very difficult with such a scheme, as there is no simple way of keeping track of the "original" component labels. This creates problem with computing standard deviations of the generated model parameters, thus making the scaling step used in tuning for epsilon or paramscale problematic as well. As such, perm_sampling is always turned off during burn-in (even if autotune = FALSE), and turned on thereafter, if TRUE. Defaults to and is set to FALSE.

n.chains	number of chains to run. Must be a positive integer.
chains_parallel	logical. Should the chains be run in parallel? Defaluts to TRUE, and ignored if n.chains = 1. Note that parallelization is implemented via future_lapply from package <code>future.apply</code> which uses futures for this purpose, and thus provides a convenient way of parallelization across various OSs and computing environments. However, a proper plan must be set for the parallization before running the chain. Otherwise the chains will run sequentially.
return_llik_contri	logical. Should the log likelihood contribution of each data point for each MCMC iteration in each chain be returned? This makes computation of waic.angmcmc and loo.angmcmc much faster. <i>*Warning*</i> : Depending on the length of data and n.iter, this can be very memory intensive. We suggest setting return_llik_contri = TRUE only if waic.angmcmc and loo.angmcmc are aimed for. Defaults to FALSE.
int.displ	absolute integer displacement for each coordinate for wnorm and wnorm2 models (ignored otherwise). Default is 3. Allowed minimum and maximum are 1 and 5 respectively.
epsilon, L	tuning parameters for HMC; ignored if method = "rwmh". epsilon (step-size) is a single number, or a vector of size 2*ncomp for univariate models and 5*ncomp for bivariate models. Note that the "mass matrix" in HMC is assumed to be identity. As such, epsilon's corresponding to different model parameters need to be in proper scale for optimal acceptance rate. Can be autotuned during burnin. See autotune. L (leapfrog steps) is a positive integer or a vector of positive integers of length n.chains. If multiple chains are used, we suggest same L values acorss different chains to make the chains as homogenous as possible.
epsilon.random	logical. Should epsilon*delta, where delta is a random number between (1-epsilon.incr, 1+epsilon.incr) be used instead of epsilon at each iteration? Ignored if method = "rwmh".
L.random	logical. Should a random integer between L.orig/exp(L.incr) and L.orig*exp(L.incr) be used instead as L at each iteration? Ignored if method = "rwmh". Defaults to TRUE.
burnin.prop	proportion of iterations to used for burnin. Must be a be a number in [0, 1]. Default is 0.5.
tune.prop	proportion of *burnin* used to tune the parameters (epsilon in HMC and propscale in RWMH). Must be a number between 0 and 1; defaults to 1. Ignored if autotune == FALSE.

thin	thinning size to be used. Must be a positive integer. If thin = n, then every nth iteration is retained in the final MCMC sample.
propscale	tuning parameters for RWMH; a vector of size 5 (for bivariate models) or 2 (for univariate models) representing the variances for the proposal normal densities for the model parameters. Ignored if method = "hmc". Can be autotuned during burnin. See autotune.
n.iter	number of iterations for the Markov Chain.
pmix.alpha	concentration parameter(s) for the Dirichlet prior for pmix. Must either be a positive real number, or a vector with positive entries and of length ncomp. The default is $(r+r(r+1)/2)/2+3$, where r is 1 or 2 according as whether the model is univariate or bivariate. Note that it is recommended to use larger alpha values to ensure the a good posterior behavior, especially when fit_incremental_angmix is used for model selection, which handles overfitting in "let two component-specific parameters be size, and then penalizes for model complexity. See Fruhwirth-Schnatter (2011) for more details on this.
norm.var	variance (hyper-) parameters in the normal prior for log(kappa), log(kappa1), log(kappa2) and kappa3. (Prior mean is zero). Can be a vector. Default is 1000 that makes the prior non-informative.
autotune	logical. Should the Markov chain auto-tune the parameter epsilon (in HMC) or propscale (in RWMH) during burn-in? Set to TRUE by default. An adaptive tuning strategy is implemented. Here, at every 10th iteration during burn-in, the acceptance ratio in the last tune_ave_size iterations is calculated. Then the tuning parameter is decreased (increased) by a factor of 1-tune.incr (1+tune.incr) if the calculated acceptance rate falls below (above) acpt.prob.lower (acpt.prob.upper). In additon, when iter is a multiple of tune_ave_size, epsilon for each model parameter is rescaled via the standard deviation of the corresponding parameter over the past tune_ave_size iterations.
show.progress	logical. Should a progress bar be included?
acpt.prob.lower, acpt.prob.upper	lower and upper limits of acceptance ratio to be maintained while tuning during burn-in. Must be numbers between 0 and 1, which acpt.prob.lower < acpt.prob.upper. See autotune. Default to (0.6, 0.9) for HMC and (0.3, 0.5) for RWMH. Ignored if autotune = FALSE.
epsilon.incr	amount of randomness incorporated in epsilon if epsilon.random = TRUE.
L.incr	amount of randomness incorporated in L if L.random = TRUE.
tune.incr	how much should the tuning parameter be increased or decreased at each step while tuning during burn-in? Must be a number between 0 and 1. See autotune. Defaults to 0.05. Ignored if autotune = FALSE.
tune_ave_size	number previous iterations used to compute the acceptance rate while tuning in burn-in. Must be a positive integer. Defaults to 100.
kappa_upper, kappa_lower	upper and lower bounds for the concentration and (absolute) association parameters. Must be a positive integers. Defaults to 150 and 1e-4, and parameter with value above or below these limits rarely make sense in practice. Warning: values much larger or smaller than the default are not recommended as they can cause numerical instability.

```

return_tune_param
    logical. Should the values of the tuning parameters used at each iteration in each
    chain be returned? Defaults to FALSE.
qrnd_grid, n_qrnd
    Used only if method="vmcos". See dvocos for details.
...
    Unused.

```

Note

Sampling is done in log scale for the concentration parameters (κ , κ_1 and κ_2).

Parallelization is done by default when more than one chain is used, but the chains can be run sequentially as well by setting `chains_parallel = FALSE`. To retain reproducibility while running multiple chains in parallel, the same RNG state is passed to each chain (then the state is changed across chains so that no two chains can become identical, even if they have the same starting and tuning parameters). This, however creates a difference between a `fit_angmix` call with multiple chains, one run sequentially by setting `chains_parallel = FALSE`, and another run sequentially due to a sequential `plan()` (or no `plan()`) used before the `fit_angmix` call, with `chains_parallel = TRUE`. In the former, different RNG states are passed at the initiation of each chain.

References

Fruhwirth-Schnatter, S. (2011). Label switching under model uncertainty. *Mixtures: Estimation and Application*, 213-239.

Fruhwirth-Schnatter, S. (2001). Markov chain Monte Carlo estimation of classical and dynamic switching and mixture models. *Journal of the American Statistical Association*, 96(453), 194-209.

Examples

```

# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_angmix("vmsin", tim8, ncomp = 3, n.iter = 20,
                        n.chains = 1)

fit.vmsin.20

# Parallelization is implemented via \link{future_lapply} from the
# package future.apply. To parallelize, first provide a parallel
# plan() for futures. Otherwise the chains will run sequentially.
# Note that not all plan() might work on every OS, as they execute
# functions defined internally in fit_mixmodel. We suggest
# plan(multiprocess).

## Not run:
library(future)
library(parallel)
plan(multiprocess)

set.seed(1)
MC.fit <- fit_angmix("vmsin", tim8, ncomp=3, n.iter=500,
                    n.chains = 3)

```

```

pointest(MC.fit)

MC.fix <- fix_label(MC.fit)

contour(MC.fit)
contour(MC.fix)
lpdtrace(MC.fit)

## End(Not run)

```

```
fit_incremental_angmix
```

Stepwise fitting of angular mixture models with incremental component sizes and optimum model selection

Description

Stepwise fitting of angular mixture models with incremental component sizes and optimum model selection

Usage

```

fit_incremental_angmix(model, data, crit = "LOOIC", start_ncomp = 1,
  max_ncomp = 10, L = NULL, fn = mean, fix_label = NULL, form = 2,
  start_par = NULL, prev_par = TRUE, logml_maxiter = 10000,
  return_all = FALSE, save_fits = FALSE, save_file = NULL,
  save_dir = "", silent = FALSE, return_llik_contri = (crit %in%
  c("LOOIC", "WAIC")), use_best_chain = TRUE, ...)

```

Arguments

model	angular model whose mixtures are to be fitted. Available choices are "vmsin", "vmcos" and "wnorm2" for bivariate data, and "vm" and "wnorm" for univariate data.
data	data matrix (if bivariate, in which case it must have two columns) or vector. If outside, the values are transformed into the scale $[0, 2\pi)$.
crit	model selection criteria, one of "AIC", "BIC", "DIC", "LOGML", "LOOIC" or "WAIC". Default is "LOOIC".
start_ncomp	starting component size. A single component model is fitted if start_ncomp is equal to one.
max_ncomp	maximum number of components allowed in the mixture model.
L	HMC tuning parameter (trajectory length) passed to <code>fit_angmix</code> . Can be a numeric vector (or scalar), in which case the same L is passed to all <code>fit_angmix</code> calls, or can be a list of length <code>max_ncomp-start_ncomp+1</code> , so that <code>L_list[[i]]</code> is

	passed as the argument <code>L</code> to <code>fit_angmix</code> call with <code>ncomp = max_ncomp+i-1</code> . See <code>fit_angmix</code> for more details on <code>L</code> including its default values. Ignored if <code>method = "rwmh"</code> .
<code>fn</code>	function to evaluate on MCMC samples to estimate parameters. Defaults to <code>mean</code> , which computes the estimated posterior means. If <code>fn = max</code> , then MAP estimate is calculated from the MCMC run. Used only if <code>crit = "DIC"</code> , and ignored otherwise.
<code>fix_label</code>	logical. Should the label switchings on the current fit (only the corresponding "best chain" if <code>use_best_chain = TRUE</code>) be fixed before computing parameter estimates and model selection criterion? Defaults to <code>TRUE</code> if <code>perm_sampling</code> is true in the <code>fit_angmix</code> call, or if <code>crit = "DIC"</code> and <code>form = 1</code> .
<code>form</code>	form of <code>crit</code> to be used. Available choices are 1 and 2. Used only if <code>crit</code> is "DIC" and ignored otherwise.
<code>start_par</code>	list with elements <code>pmix</code> (ignored if <code>comp == 1</code>), together with <code>kappa1</code> , <code>kappa2</code> , <code>mu1</code> and <code>mu2</code> , for bivariate models, and <code>kappa</code> and <code>mu</code> for univariate models, all being vectors of length same as <code>ncomp</code> . These provides the starting values for the Markov chain; with j -th component of each vector corresponding to the j -th component of the mixture distribution. If missing, the data is first clustered into <code>ncomp</code> groups either via k-means (after projecting onto a unit sphere), or randomly, depending on <code>rand_start</code> , and then moment estimators for components are used as the starting points. Note that a very wrong starting point can potentially lead the chain to get stuck at a wrong solution for thousands of iterations. As such, we recommend using the default option, which is k-means followed by moment estimation.
<code>prev_par</code>	logical. Should the MAP estimated parameters from the model with <code>ncomp = K</code> be used in the model with <code>ncomp = K+1</code> as the starting parameters, with the component with largest mixing proportion appearing twice in the bigger model?
<code>logml_maxiter</code>	maximum number of iterations (<code>maxiter</code>) passed to <code>bridge_sampler</code> for calculating LOGML. Ignored if <code>crit</code> is not LOGML.
<code>return_all</code>	logical. Should all <code>angmcmc</code> objects obtained during step-wise run be returned? <i>*Warning*</i> : depending on the sizes of <code>n.iter</code> , <code>start_ncomp</code> , <code>max_ncomp</code> and <code>n.chains</code> , this can be very memory intensive. In such cases, it is recommended that <code>return_all</code> be set to <code>FALSE</code> , and, if required, the intermediate fitted objects be saved to file by setting <code>save_fits = TRUE</code> .
<code>save_fits</code>	logical. Should the intermediate <code>angmcmc</code> objects obtained during step-wise run be saved to file using <code>save</code> ? Defaults to <code>TRUE</code> . See <code>save_file</code> and <code>save_dir</code> .
<code>save_file</code> , <code>save_dir</code>	<code>save_file</code> is a list of size <code>max_ncomp-start_ncomp+1</code> , with k -th entry providing the file argument used to <code>save</code> the intermediate <code>angmcmc</code> object with <code>ncomp = k</code> (titled "fit_angmcmc"). If not provided, then k -th element of <code>save_file[[k]]</code> is taken to be <code>paste(save_dir, "comp_k", sep="/")</code> . Both are ignored if <code>save_fits = FALSE</code> .
<code>silent</code>	logical. Should the current status (such as what is the current component labels, which job is being done etc.) be printed? Defaults to <code>TRUE</code> .
<code>return_llik_contri</code>	passed to <code>fit_angmix</code> . By default, set to <code>TRUE</code> if <code>crit</code> is either "LOOIC" or "WAIC", and to <code>FALSE</code> otherwise.

`use_best_chain` logical. Should only the "best" chain obtained during each intermediate fit be used during computation of model selection criterion? Here "best" means the chain with largest (mean over iterations) log-posterior density. This can be helpful if one of the chains gets stuck at local optima. Defaults to TRUE.

... additional arguments passed to `fit_angmix`.

Details

The goal is to fit an angular mixture model with an optimally chosen component size K . To obtain an optimum K , mixture models with incremental component sizes between `start_ncomp` and `max_ncomp` are fitted stepwise using `fit_angmix`. The mixture model with the first minimum value of the model selection criterion `crit` is taken as the best model.

Note that in each intermediate fitted model, the total number of components (instead of the number of "non-empty components") in the model is used to estimate of the true component size, and then the fitted model is penalized for model complexity (via the model selection criterion). This approach of selecting an optimal K follows the perspective "let two component specific parameters be identical" for overfitting mixtures, and as such the Dirichlet prior hyper-parameters `pmix.alpha` (passed to `fit_angmix`) should be large. See Fruhwirth-Schnatter (2011) and Mengerson for more details.

Note that the stability of `bridge_sampler` used in marginal likelihood estimation heavily depends on stationarity of the chains. As such, while using this criterion, we recommending running the chain long enough, and setting `fix_label = TRUE` for optimal performance.

Value

Returns a named list (with class = `stepfit`) with the following seven elements:

`fit.all` (if `return_all = TRUE`) - a list all `angmcmc` objects created at each component size;

`fit.best` - `angmcmc` object corresponding to the optimum component size;

`ncomp.best` - optimum component size (integer);

`crit` - which model comparison criterion used (one of "AIC", "BIC", "DIC" or "WAIC");

`crit.all` - all `crit` values calculated (for all component sizes);

`crit.best` - `crit` value for the optimum component size; and

`maxllik.all` - maximum (obtained from MCMC iterations) log likelihood for all fitted models

`maxllik.best` - maximum log likelihood for the optimal model; and

`check_min` - logical; is the optimum component size less than `max_ncomp`?

References

Fruhwirth-Schnatter, S.: Label switching under model uncertainty. In: Mengerson, K., Robert, C., Titterton, D. (eds.) Mixtures: Estimation and Application, pp. 213-239. Wiley, New York (2011).

Examples

```
# illustration only - more iterations needed for convergence
set.seed(1)
fit.vm.step.15 <- fit_incremental_angmix("vmsin", tim8, "BIC", start_ncomp = 1,
                                       max_ncomp = 3, n.iter = 15,
                                       n.chains = 1, save_fits=FALSE)
(fit.vm.best.15 <- bestmodel(fit.vm.step.15))
lattice::densityplot(fit.vm.best.15)
```

fit_vmcosmix

Fitting bivariate von Mises cosine model mixtures using MCMC

Description

Fitting bivariate von Mises cosine model mixtures using MCMC

Usage

```
fit_vmcosmix(...)
```

Arguments

... arguments (other than model) passed to [fit_angmix](#)

Details

Wrapper for [fit_angmix](#) with model = "vmcos".

Examples

```
# illustration only - more iterations needed for convergence
fit.vmcos.10 <- fit_vmcosmix(tim8, ncomp = 3, n.iter = 10,
                           n.chains = 1)
fit.vmcos.10
```

`fit_vmmix`*Fitting univariate von Mises mixtures using MCMC*

Description

Fitting univariate von Mises mixtures using MCMC

Usage

```
fit_vmmix(...)
```

Arguments

... arguments (other than model) passed to [fit_angmix](#)

Details

Wrapper for [fit_angmix](#) with model = "vm".

Examples

```
# illustration only - more iterations needed for convergence
fit.vm.20 <- fit_vmmix(wind$angle, ncomp = 3, n.iter = 20,
                     n.chains = 1)
fit.vm.20
```

`fit_vmsinmix`*Fitting bivariate von Mises sine model mixtures using MCMC*

Description

Fitting bivariate von Mises sine model mixtures using MCMC

Usage

```
fit_vmsinmix(...)
```

Arguments

... arguments (other than model) passed to [fit_angmix](#)

Details

Wrapper for [fit_angmix](#) with model = "vmsin"

Examples

```
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
fit.vmsin.20
```

fit_wnorm2mix

Fitting bivariate wrapped normal model mixtures using MCMC

Description

Fitting bivariate wrapped normal model mixtures using MCMC

Usage

```
fit_wnorm2mix(...)
```

Arguments

... arguments (other than model) passed to [fit_angmix](#)

Details

Wrapper for [fit_angmix](#) with model = "wnorm2".

Examples

```
# illustration only - more iterations needed for convergence
fit.wnorm2.10 <- fit_wnorm2mix(tim8, ncomp = 3, n.iter = 10,
                              n.chains = 1)
fit.wnorm2.10
```

fit_wnormmix

Fitting univariate wrapped normal mixtures using MCMC

Description

Fitting univariate wrapped normal mixtures using MCMC

Usage

```
fit_wnormmix(...)
```

Arguments

... arguments (other than model) passed to [fit_angmix](#)

Details

Wrapper for [fit_angmix](#) with model = "wnorm".

Examples

```
# illustration only - more iterations needed for convergence
fit.wnorm.20 <- fit_wnormmix(wind$angle, ncomp = 3, n.iter = 20,
                           n.chains = 1)
fit.wnorm.20
```

fix_label	<i>Fix label switching in angmcmc objects</i>
-----------	---

Description

Fix label switching in angmcmc objects

Usage

```
fix_label(object, ...)
```

Arguments

object angular MCMC object.
 ... arguments other than z, K, complete, mcmc, p and data passed to [label.switching](#). See details.

Details

fix_label is a wrapper for [label.switching](#) from package label.switching for angmcmc objects. The arguments z, K, complete, mcmc, p and data are appropriately filled in from object. The label.switching argument method can be a scalar or vector; for this wrapper it defaults to "STEPHENS" if the angmcmc was created with permutation sampling (by setting perm_sampling = TRUE in [fit_angmix](#)), and to "DATA-BASED" otherwise.

Value

Returns a single angmcmc object or a list of angmcmc objects (according as whether the argument method is a scalar or vector) with label switchings corrected (after burn-in and thin) according to the resulting permutation from [label.switching](#).

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)

# now apply fix_label
fit.vmsin.20.fix <- fix_label(fit.vmsin.20)
```

is.angmcmc

Angular MCMC (angmcmc) Object

Description

Checking for and creating an angmcmc object

Usage

```
is.angmcmc(object)
```

```
angmcmc(...)
```

Arguments

object any R object

... arguments required to make an angmcmc object. See details

Details

angmcmc objects are classified lists that are created when any of the five mixture model fitting functions, viz., `fit_vmmix`, `fit_wnormmix`, `fit_vmsinmix`, `fit_vmcosmix` and `fit_wnorm2mix` is used. An angmcmc object contains a number of elements, including the dataset, the model being fitted on the dataset and dimension of the model (univariate or bivariate), the tuning parameters used, MCMC samples for the mixture model parameters, the (hidden) component or cluster indicators for data points in each iteration and the (iteration-wise) log likelihood and log posterior density values (both calculated upto some normalizing constants). When printed, an angmcmc object returns a brief summary of the function arguments used to produce the object and the average acceptance rate of the proposals (in HMC and RWMH) used over iterations. An angmcmc object can be used as an argument for the diagnostic and post-processing functions available in BAMBI for making further inferences.

Value

logical. Is the input an angmcmc object?

Examples

```
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
is.angmcmc(fit.vmsin.20)
```

latent_allocation	<i>Finding latent allocation (component indicators) from an angmcmc object</i>
-------------------	--

Description

Finding latent allocation (component indicators) from an angmcmc object

Usage

```
latent_allocation(object, ...)
```

Arguments

object	angular MCMC object.
...	passed to pointest to estimate parameters.

Details

In order to find the latent component indicators, estimates of mixing proportions and model parameters are first computed via [pointest](#). Then, a data point is assigned label j , if the j -th component gives highest density for that point.

Value

Returns a vector of length n , where n is the length (if univariate) or number of rows (if bivariate) of the data used in original fit. i -th entry of the output vector provides component label for the i -th data point.

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
# now find latent allocation
latent_allocation(fit.vmsin.20)
```

loo.angmcmc	<i>Leave-one-out cross-validation (LOO) for angmcmc objects</i>
-------------	---

Description

Leave-one-out cross-validation (LOO) for angmcmc objects

Usage

```
## S3 method for class 'angmcmc'
loo(x, ...)
```

Arguments

x	angmcmc object.
...	additional model specific arguments to be passed to waic from loo. For example, <code>int.displ</code> specifies integer displacement in <code>wnorm</code> and <code>wnorm2</code> models. See fit_wnormmix and fit_wnorm2mix for more details.

Details

Note that `loo.angmcmc` calls [loo](#) for computation. If the likelihood contribution of each data point for each MCMC iteration is available in object (can be returned by setting `return_llik_contri = TRUE`) during [fit_angmix](#) call), `loo.array` is used; otherwise `loo.function` is called. Computation is much faster if the likelihood contributions are available - however, they are very memory intensive, and by default not returned in [fit_angmix](#).

Examples

```
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1, return_llik_contri = TRUE)

library(loo)
loo(fit.vmsin.20)
```

lpdtrace	<i>Trace and autocorrelation plots of log posterior density or log likelihood from an angmcmc object</i>
----------	--

Description

Trace and autocorrelation plots of log posterior density or log likelihood from an angmcmc object

Usage

```
lpdtrace(object, chain.no, use.llik = FALSE, plot.autocor = FALSE,
          press.enter = TRUE, lag.max = NULL, ...)
```

Arguments

object	angular MCMC object.
chain.no	vector of chain numbers whose samples are to be used. in the estimation. By default all chains are used.
use.llik	logical. Should log likelihood be plotted instead of log posterior? Set to FALSE by default.
plot.autocor	logical. Should the autocorrelations be plotted as well?
press.enter	logical. Should the next plot in the series be shown after you press "Enter"? Ignored if only a single plot is to be created.
lag.max	maximum lag for autocorrelation. Passed to acf . Ignored if plot.autocor = FALSE.
...	unused

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
# log posterior density trace
lpdtrace(fit.vmsin.20)
# log likelihood trace
lpdtrace(fit.vmsin.20, use.llik = TRUE)
```

paramtrace

Trace plot for parameters from an angmcmc object

Description

Trace plot for parameters from an angmcmc object

Usage

```
paramtrace(object, par.name, comp.label, chain.no, press.enter = TRUE, ...)
```

Arguments

object	angular MCMC object.
par.name	vector of names of parameters for which point estimates are to be computed. If NULL, results for all parameters are provided.
comp.label	vector of component labels (positive integers, e.g., 1, 2, ...) for which point estimates are to be computed. If NULL, results for all components are provided.
chain.no	vector of chain numbers whose samples are to be used. in the estimation. By default all chains are used.

press.enter	logical. Should the next plot in the series be shown after you press "Enter"? Ignored if only a single plot is to be created.
...	unused
par	parameter for which trace plot is to be created.

Value

Returns a single plot if a single `par` and a single `comp.label` is supplied. Otherwise, a series of plots is produced.

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
# trace plot for kappa1 in component 1
paramtrace(fit.vmsin.20, "kappa1", 1)
# for kappa1 in all components
paramtrace(fit.vmsin.20, "kappa1", press.enter = FALSE)
# for all parameters in component 1
paramtrace(fit.vmsin.20, comp.label = 1, press.enter = FALSE)
```

plot.angmcmc

Summary plots for angmcmc objects

Description

Summary plots for angmcmc objects

Usage

```
## S3 method for class 'angmcmc'
plot(x, par.name, comp.label, chain.no,
     do.paramtrace = TRUE, do.lpdtrace = TRUE, use.llik = FALSE,
     press.enter = TRUE, ...)
```

Arguments

<code>x</code>	angmcmc object
<code>par.name</code>	vector of names of parameters for which point estimates are to be computed. If NULL, results for all parameters are provided.
<code>comp.label</code>	vector of component labels (positive integers, e.g., 1, 2, ...) for which point estimates are to be computed. If NULL, results for all components are provided.
<code>chain.no</code>	vector of chain numbers whose samples are to be used. in the estimation. By default all chains are used.

<code>do.paramtrace</code>	logical. Should the trace(s) for the parameter(s) be plotted?
<code>do.lpdtrace</code>	logical. Should the log posterior trace be plotted?
<code>use.llik</code>	logical. Should the log likelihood be plotted instead? Ignored if <code>do.lpdtrace == FALSE</code> .
<code>press.enter</code>	logical. Should the next plot in the series be shown after you press "Enter"? Ignored if only a single plot is to be created.
<code>...</code>	unused

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
plot(fit.vmsin.20, press.enter = FALSE)
```

pointest

Point estimates for parameters from an angmcmc object

Description

Point estimates for parameters from an angmcmc object

Usage

```
pointest(object, fn = mean, par.name, comp.label, chain.no, ...)
```

Arguments

<code>object</code>	angular MCMC object.
<code>fn</code>	function, or a single character string specifying its name, to evaluate on MCMC samples to estimate parameters. Defaults to <code>mean</code> , which computes the estimated posterior mean. Note that if <code>fn = "MODE"</code> (warning: not "mode") or <code>fn = "MAP"</code> , then the maximum a posteriori estimate (MAP) is calculated.
<code>par.name</code>	vector of names of parameters for which point estimates are to be computed. If <code>NULL</code> , results for all parameters are provided.
<code>comp.label</code>	vector of component labels (positive integers, e.g., 1, 2, ...) for which point estimates are to be computed. If <code>NULL</code> , results for all components are provided.
<code>chain.no</code>	vector of chain numbers whose samples are to be used. in the estimation. By default all chains are used.
<code>...</code>	additional arguments to be passed to the function.

Value

Returns a matrix of point estimates, or vector of point estimates if `length(par.name)==1` or `length(comp.label)==1`.

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
# estimate parameters by sample mean
(est_mean <- pointest(fit.vmsin.20))
# estimate parameters by sample median
(est_median <- pointest(fit.vmsin.20, fn = median))
# estimate parameters by MAP
(est_median <- pointest(fit.vmsin.20, fn = "MODE"))
```

quantile.angmcmc

Quantile estimates for parameters from an angmcmc object

Description

Quantile estimates for parameters from an angmcmc object

Usage

```
## S3 method for class 'angmcmc'
quantile(x, par.name, comp.label, chain.no, probs = seq(0,
  1, 0.25), ...)
```

Arguments

<code>x</code>	angmcmc object
<code>par.name</code>	vector of names of parameters for which point estimates are to be computed. If NULL, results for all parameters are provided.
<code>comp.label</code>	vector of component labels (positive integers, e.g., 1, 2, ...) for which point estimates are to be computed. If NULL, results for all components are provided.
<code>chain.no</code>	vector of chain numbers whose samples are to be used. in the estimation. By default all chains are used.
<code>probs</code>	numeric vector of probabilities with values in $[0, 1]$. (Values up to '2e-14' outside that range are accepted and moved to the nearby endpoint.)
<code>...</code>	further arguments to pass to <code>quantile</code> . In particular, <code>probs = seq(0, 1, 0.25)</code> is the default vector of quantiles computed for each parameter.

Value

Returns a three dimensional array of quantiles, or a matrix (vector) of quantiles if one (or two) among `par.name`, `comp.label`, `probs` has length 1.

Examples

```
# first fit a vmsin mixture model
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)

# 0.025th quantiles
(quant_025 <- quantile(fit.vmsin.20, prob = 0.025))
# 0.975th quantiles
(quant_975 <- quantile(fit.vmsin.20, prob = 0.975))
# default quantiles
(quant_def <- quantile(fit.vmsin.20))
```

rvm

*The univariate von Mises distribution***Description**

The univariate von Mises distribution

Usage

```
rvm(n, kappa = 1, mu = 0)

dvm(x, kappa = 1, mu = 0, log = FALSE)
```

Arguments

n	number of observations. Ignored if at least one of the other parameters have length $k > 1$, in which case, all the parameters are recycled to length k to produce k random variates.
kappa	vector of concentration (inverse-variance) parameters; $\text{kappa} > 0$.
mu	vector of means.
x	vector of angles (in radians) where the densities are to be evaluated.
log	logical. Should the log density be returned instead?

Details

If μ and kappa are not specified they assume the default values of 0 and 1 respectively.

The univariate von Mises distribution has density

$$f(x) = 1/(2\pi I_0(\kappa)) \exp(\kappa \cos(x - \mu))$$

where $I_0(\kappa)$ denotes the modified Bessel function of the first kind with order 0 evaluated at the point κ .

Value

dvm gives the density and rvm generates random deviates.

Examples

```
kappa <- 1:3
mu <- 0:2
x <- 1:10
n <- 10

# when x and both parameters are scalars, dvm returns a single density
dvm(x[1], kappa[1], mu[1])

# when x is a vector but both the parameters are scalars, dvm returns a vector of
# densities calculated at each entry of x with the same parameters
dvm(x, kappa[1], mu[1])

# if x is scalar and at least one of the two parameters is a vector, both parameters are
# recycled to the same length, and dvm returns a vector of with ith element being the
# density evaluated at x with parameter values kappa[i] and mu[i]
dvm(x[1], kappa, mu)

# if x and at least one of the two parameters is a vector, x and the two parameters are
# recycled to the same length, and dvm returns a vector of with ith element being the
# density at ith element of the (recycled) x with parameter values kappa[i] and mu[i]
dvm(x, kappa, mu)

# when parameters are all scalars, number of observations generated by rvm is n
rvm(n, kappa[1], mu[1])

# when at least one of the two parameters is a vector, both are recycled to the same length,
# n is ignored, and the number of observations generated by rvm is the same as the length of
# the recycled vectors
rvm(n, kappa, mu)
```

rvmcos

The bivariate von Mises cosine model

Description

The bivariate von Mises cosine model

Usage

```
rvmcos(n, kappa1 = 1, kappa2 = 1, kappa3 = 0, mu1 = 0, mu2 = 0,
       method = NULL)
```

```
dvmcos(x, kappa1 = 1, kappa2 = 1, kappa3 = 0, mu1 = 0, mu2 = 0,
log = FALSE, ...)
```

Arguments

n	number of observations. Ignored if at least one of the other parameters have length $k > 1$, in which case, all the parameters are recycled to length k to produce k random variates.
kappa1, kappa2, kappa3	vectors of concentration parameters; $kappa1, kappa2 > 0$.
mu1, mu2	vectors of mean parameters.
method	Rejection sampling method to be used. Available choices are "naive" or "vmprop". See details.
x	bivariate vector or a two-column matrix with each row being a bivariate vector of angles (in radians) where the densities are to be evaluated.
log	logical. Should the log density be returned instead?
...	additional arguments to be passed to dvmcos. See details.

Details

The bivariate von Mises cosine model density at the point $x = (x_1, x_2)$ is given by

$$f(x) = C_c(\kappa_1, \kappa_2, \kappa_3) \exp(\kappa_1 \cos(T_1) + \kappa_2 \cos(T_2) + \kappa_3 \cos(T_1 - T_2))$$

where

$$T_1 = x_1 - \mu_1; T_2 = x_2 - \mu_2$$

and $C_c(\kappa_1, \kappa_2, \kappa_3)$ denotes the normalizing constant for the cosine model.

#' Because C_c involves an infinite series with product of Bessel functions, if $kappa3 < -5$ or $\max(kappa1, kappa2, \text{abs}(kappa3)) > 50$, C_c is evaluated numerically via (quasi) Monte carlo method for numerical stability. These (quasi) random numbers can be provided through the argument `qrnd`, which must be a two column matrix, with each element being a (quasi) random number between 0 and 1. Alternatively, if `n_qrnd` is provided (and `qrnd` is missing), a two dimensional sobol sequence of size `n_qrnd` is generated via the function `sobol` from the R package `qrng`. If none of `qrnd` or `n_qrnd` is available, a two dimensional sobol sequence of size `1e4` is used.

Value

`dvmcos` gives the density and `rvmcos` generates random deviates.

Examples

```
kappa1 <- c(1, 2, 3)
kappa2 <- c(1, 6, 5)
kappa3 <- c(0, 1, 2)
mu1 <- c(1, 2, 5)
mu2 <- c(0, 1, 3)
x <- diag(2, 2)
```

```

n <- 10

# when x is a bivariate vector and parameters are all scalars,
# dvmcos returns single density
dvmcos(x[1, ], kappa1[1], kappa2[1], kappa3[1], mu1[1], mu2[1])

# when x is a two column matrix and parameters are all scalars,
# dmvsin returns a vector of densities calculated at the rows of
# x with the same parameters
dvmcos(x, kappa1[1], kappa2[1], kappa3[1], mu1[1], mu2[1])

# if x is a bivariate vector and at least one of the parameters is
# a vector, all parameters are recycled to the same length, and
# dvmcos returns a vector with ith element being the density
# evaluated at x with parameter values kappa1[i], kappa2[i],
# kappa3[i], mu1[i] and mu2[i]
dvmcos(x[1, ], kappa1, kappa2, kappa3, mu1, mu2)

# if x is a two column matrix and at least one of the parameters is
# a vector, rows of x and the parameters are recycled to the same
# length, and dvmcos returns a vector with ith element being the
# density evaluated at ith row of x with parameter values kappa1[i],
# kappa2[i], # kappa3[i], mu1[i] and mu2[i]
dvmcos(x, kappa1, kappa2, kappa3, mu1, mu2)

# when parameters are all scalars, number of observations generated
# by rvmcos is n
rvmcos(n, kappa1[1], kappa2[1], kappa3[1], mu1[1], mu2[1])

# when at least one of the parameters is a vector, all parameters are
# recycled to the same length, n is ignored, and the number of
# observations generated by rvmcos is the same as the length of the
# recycled vectors
rvmcos(n, kappa1, kappa2, kappa3, mu1, mu2)

```

rvmcosmix

The bivariate von Mises cosine model mixtures

Description

The bivariate von Mises cosine model mixtures

Usage

```
rvmcosmix(n, kappa1, kappa2, kappa3, mu1, mu2, pmix, method = NULL)
```

```
dvmcosmix(x, kappa1, kappa2, kappa3, mu1, mu2, pmix, log = FALSE, ...)
```

Arguments

n	number of observations.
kappa1, kappa2, kappa3	vectors of concentration parameters; kappa1, kappa2 > 0 for each component.
mu1, mu2	vectors of mean parameters.
pmix	vector of mixture proportions.
method	Rejection sampling method to be used. Available choices are "naive" or "vmprop". See details.
x	matrix of angles (in radians) where the density is to be evaluated, with each row being a single bivariate vector of angles.
log	logical. Should the log density be returned instead?
...	additional arguments to be passed to dvmcos. See details.

Details

All the argument vectors pmix, kappa1, kappa2, kappa3, mu1 and mu2 must be of the same length (= component size of the mixture model), with j -th element corresponding to the j -th component of the mixture distribution.

The bivariate von Mises cosine model mixture distribution with component size $K = \text{length}(\text{pmix})$ has density

$$g(x) = \sum p[j] * f(x; \kappa_1[j], \kappa_2[j], \kappa_3[j], \mu_1[j], \mu_2[j])$$

where the sum extends over j ; $p[j]$; $\kappa_1[j]$, $\kappa_2[j]$, $\kappa_3[j]$; and $\mu_1[j]$, $\mu_2[j]$ respectively denote the mixing proportion, the three concentration parameters and the two mean parameter for the j -th cluster, $j = 1, \dots, K$, and $f(.; \kappa_1, \kappa_2, \kappa_3, \mu_1, \mu_2)$ denotes the density function of the von Mises cosine model with concentration parameters $\kappa_1, \kappa_2, \kappa_3$ and mean parameters μ_1, μ_2 .

Value

dvmcosmix computes the density and rvmcosmix generates random deviates from the mixture density.

Examples

```
kappa1 <- c(1, 2, 3)
kappa2 <- c(1, 6, 5)
kappa3 <- c(0, 1, 2)
mu1 <- c(1, 2, 5)
mu2 <- c(0, 1, 3)
pmix <- c(0.3, 0.4, 0.3)
x <- diag(2, 2)
n <- 10
```

```
# mixture densities calculated at the rows of x
dvmcosmix(x, kappa1, kappa2, kappa3, mu1, mu2, pmix)
```

```
# number of observations generated from the mixture distribution is n
rvmcosmix(n, kappa1, kappa2, kappa3, mu1, mu2, pmix)
```

 rvmmix

The univariate von Mises mixtures

Description

The univariate von Mises mixtures

Usage

```
rvmmix(n, kappa, mu, pmix)
```

```
dvmix(x, kappa, mu, pmix, log = FALSE)
```

Arguments

n	number of observations. Ignored if at least one of the other parameters have length $k > 1$, in which case, all the parameters are recycled to length k to produce k random variates.
kappa	vector of component concentration (inverse-variance) parameters, $\text{kappa} > 0$.
mu	vector of component means.
pmix	vector of mixing proportions.
x	vector of angles (in radians) where the densities are to be evaluated.
log	logical. Should the log density be returned instead?

Details

pmix, mu and kappa must be of the same length, with j -th element corresponding to the j -th component of the mixture distribution.

The univariate von Mises mixture distribution with component size $K = \text{length}(\text{pmix})$ has density

$$g(x) = p[1] * f(x; \kappa[1], \mu[1]) + \dots + p[K] * f(x; \kappa[K], \mu[K])$$

where $p[j]$, $\kappa[j]$, $\mu[j]$ respectively denote the mixing proportion, concentration parameter and the mean parameter for the j -th component and $f(\cdot; \kappa, \mu)$ denotes the density function of the (univariate) von Mises distribution with mean parameter μ and concentration parameter κ .

Value

dvmix computes the density and rvmmix generates random deviates from the mixture density.

Examples

```

kappa <- 1:3
mu <- 0:2
pmix <- c(0.3, 0.3, 0.4)
x <- 1:10
n <- 10

# mixture densities calculated at each point in x
dvmmix(x, kappa, mu, pmix)

# number of observations generated from the mixture distribution is n
rvmmix(n, kappa, mu, pmix)

```

rvmsin

The bivariate von Mises sine model

Description

The bivariate von Mises sine model

Usage

```
rvmsin(n, kappa1 = 1, kappa2 = 1, kappa3 = 0, mu1 = 0, mu2 = 0,
       method = NULL)
```

```
dvmsin(x, kappa1 = 1, kappa2 = 1, kappa3 = 0, mu1 = 0, mu2 = 0,
       log = FALSE)
```

Arguments

n	number of observations. Ignored if at least one of the other parameters have length $k > 1$, in which case, all the parameters are recycled to length k to produce k random variates.
kappa1, kappa2, kappa3	vectors of concentration parameters; $kappa1, kappa2 > 0$.
mu1, mu2	vectors of mean parameters.
method	Rejection sampling method to be used. Available choices are "naive" or "vmprop". See details.
x	bivariate vector or a two-column matrix with each row being a bivariate vector of angles (in radians) where the densities are to be evaluated.
log	logical. Should the log density be returned instead?

Details

The bivariate von Mises sine model density at the point $x = (x_1, x_2)$ is given by

$$f(x) = C_s(\kappa_1, \kappa_2, \kappa_3) \exp(\kappa_1 \cos(T_1) + \kappa_2 \cos(T_2) + \kappa_3 \sin(T_1) \sin(T_2))$$

where

$$T_1 = x_1 - \mu_1; T_2 = x_2 - \mu_2$$

and $C_s(\kappa_1, \kappa_2, \kappa_3)$ denotes the normalizing constant for the sine model.

Two different rejection sampling methods are implemented for random generation. If `method = "vmprop"`, then first the y-marginal is drawn from the associated marginal density, and then x is generated from the conditional distributio of x given y. The marginal generation of y is implemented in a rejection sampling scheme with proposal being either von Mises (if the target marginal density is unimodal), or a mixture of von Mises (if bimodal), with optimally chosen concentration. This the method suggested in Mardia et al. (2007). On the other hand, when `method = "naive"` a (naive) bivariate rejection sampling scheme with (bivariate) uniform propsal is used.

Note that although `method = "vmprop"` is expected to provide better efficiency, especially when the density is highly concentrated, it does have an (often substantial) overhead due to the optimization step required to find a reasonable proposal concentration parameter. This can compensate the efficiency gains of this method, especially when n is not large (≤ 100) or $\max(\kappa_1, \kappa_2, \text{abs}(\kappa_3))$ is small (< 0.1). As such, `method = "naive"` by default in such cases. Otherwise, method defaults to "vmprop".

Value

`dvmsin` gives the density and `rvmsin` generates random deviates.

Examples

```
kappa1 <- c(1, 2, 3)
kappa2 <- c(1, 6, 5)
kappa3 <- c(0, 1, 2)
mu1 <- c(1, 2, 5)
mu2 <- c(0, 1, 3)
x <- diag(2, 2)
n <- 10

# when x is a bivariate vector and parameters are all scalars,
# dvmsin returns single density
dvmsin(x[1, ], kappa1[1], kappa2[1], kappa3[1], mu1[1], mu2[1])

# when x is a two column matrix and parameters are all scalars,
# dmvsin returns a vector of densities calculated at the rows of
# x with the same parameters
dvmsin(x, kappa1[1], kappa2[1], kappa3[1], mu1[1], mu2[1])

# if x is a bivariate vector and at least one of the parameters is
# a vector, all parameters are recycled to the same length, and
# dvmsin returns a vector of with ith element being the density
# evaluated at x with parameter values kappa1[i], kappa2[i],
# kappa3[i], mu1[i] and mu2[i]
```

```

dvmsin(x[, ], kappa1, kappa2, kappa3, mu1, mu2)

# if x is a two column matrix and at least one of the parameters is
# a vector, rows of x and the parameters are recycled to the same
# length, and dvmsin returns a vector of with ith element being the
# density evaluated at ith row of x with parameter values kappa1[i],
# kappa2[i], # kappa3[i], mu1[i] and mu2[i]
dvmsin(x[, ], kappa1, kappa2, kappa3, mu1, mu2)

# when parameters are all scalars, number of observations generated
# by rvmsin is n
rvmsin(n, kappa1[1], kappa2[1], kappa3[1], mu1[1], mu2[1])

# when at least one of the parameters is a vector, all parameters are
# recycled to the same length, n is ignored, and the number of
# observations generated by rvmsin is the same as the length of the
# recycled vectors
rvmsin(n, kappa1, kappa2, kappa3, mu1, mu2)

```

rvmsinmix

The bivariate von Mises sine model mixtures

Description

The bivariate von Mises sine model mixtures

Usage

```
rvmsinmix(n, kappa1, kappa2, kappa3, mu1, mu2, pmix, method = NULL)
```

```
dvmsinmix(x, kappa1, kappa2, kappa3, mu1, mu2, pmix, log = FALSE)
```

Arguments

n	number of observations.
kappa1, kappa2, kappa3	vectors of concentration parameters; kappa1, kappa2 > 0 for each component.
mu1, mu2	vectors of mean parameters.
pmix	vector of mixture proportions.
method	Rejection sampling method to be used. Available choices are "naive" or "vmprop". See details.
x	matrix of angles (in radians) where the density is to be evaluated, with each row being a single bivariate vector of angles.
log	logical. Should the log density be returned instead?

Details

All the argument vectors `pmix`, `kappa1`, `kappa2`, `kappa3`, `mu1` and `mu2` must be of the same length (= component size of the mixture model), with j -th element corresponding to the j -th component of the mixture distribution.

The bivariate von Mises sine model mixture distribution with component size $K = \text{length}(p.mix)$ has density

$$g(x) = \sum p[j] * f(x; \kappa_1[j], \kappa_2[j], \kappa_3[j], \mu_1[j], \mu_2[j])$$

where the sum extends over j ; $p[j]$; $\kappa_1[j]$, $\kappa_2[j]$, $\kappa_3[j]$; and $\mu_1[j]$, $\mu_2[j]$ respectively denote the mixing proportion, the three concentration parameters and the two mean parameter for the j -th component, $j = 1, \dots, K$, and $f(.; \kappa_1, \kappa_2, \kappa_3, \mu_1, \mu_2)$ denotes the density function of the von Mises sine model with concentration parameters $\kappa_1, \kappa_2, \kappa_3$ and mean parameters μ_1, μ_2 .

Value

`dvmsinmix` computes the density (vector if `x` is a two column matrix with more than one row) and `rvmsinmix` generates random deviates from the mixture density.

Examples

```
kappa1 <- c(1, 2, 3)
kappa2 <- c(1, 6, 5)
kappa3 <- c(0, 1, 2)
mu1 <- c(1, 2, 5)
mu2 <- c(0, 1, 3)
pmix <- c(0.3, 0.4, 0.3)
x <- diag(2, 2)
n <- 10

# mixture densities calculated at the rows of x
dvmsinmix(x, kappa1, kappa2, kappa3, mu1, mu2, pmix)

# number of observations generated from the mixture distribution is n
rvmsinmix(n, kappa1, kappa2, kappa3, mu1, mu2, pmix)
```

rwnorm

The univariate Wrapped Normal distribution

Description

The univariate Wrapped Normal distribution

Usage

```
rwnorm(n = 1, kappa = 1, mu = 0)

dwnorm(x, kappa = 1, mu = 0, int.displ, log = FALSE)
```

Arguments

n	number of observations. Ignored if at least one of the other parameters have length $k > 1$, in which case, all the parameters are recycled to length k to produce k random variates.
kappa	vector of concentration (inverse-variance) parameters; $\text{kappa} > 0$.
mu	vector of means.
x	vector of angles (in radians) where the densities are to be evaluated.
int.displ	integer displacement. The allowed values are 1, 2, 3, 4 and 5. Default is 3.
log	logical. Should the log density be returned instead?

Details

If μ and kappa are not specified they assume the default values of 0 and 1 respectively.

The univariate wrapped normal distribution has density

$$f(x) = \sqrt{\kappa/(2\pi)} \sum \exp(-\kappa/2(x - \mu(2\pi\omega))^2)$$

where the sum extends over all integers ω , and is approximated by a sum over ω in $\{-M, -M + 1, \dots, M - 1, M\}$ if $\text{int.displ} = M$.

Value

dwnorm gives the density and rwnorm generates random deviates.

Examples

```
kappa <- 1:3
mu <- 0:2
x <- 1:10
n <- 10

# when x and both parameters are scalars, dwnorm returns a single density
dwnorm(x[1], kappa[1], mu[1])

# when x is a vector but both the parameters are scalars, dmv returns a vector of
# densities calculated at each entry of x with the same parameters
dwnorm(x, kappa[1], mu[1])

# if x is scalar and at least one of the two parameters is a vector, both parameters are
# recycled to the same length, and dwnorm returns a vector of with ith element being the
# density evaluated at x with parameter values kappa[i] and mu[i]
dwnorm(x[1], kappa, mu)

# if x and at least one of the two parameters is a vector, x and the two parameters are
# recycled to the same length, and dwnorm returns a vector of with ith element being the
# density at ith element of the (recycled) x with parameter values kappa[i] and mu[i]
dwnorm(x, kappa, mu)
```

```
# when parameters are all scalars, number of observations generated by rwnorm is n
rwnorm(n, kappa[1], mu[1])

# when at least one of the two parameters is a vector, both are recycled to the same length,
# n is ignored, and the number of observations generated by rwnorm is the same as the length
# of the recycled vectors
rwnorm(n, kappa, mu)
```

rwnorm2

The bivariate Wrapped Normal distribution

Description

The bivariate Wrapped Normal distribution

Usage

```
rwnorm2(n, kappa1 = 1, kappa2 = 1, kappa3 = 0, mu1 = 0, mu2 = 0, ...)

dwnorm2(x, kappa1 = 1, kappa2 = 1, kappa3 = 0, mu1 = 0, mu2 = 0,
        int.displ, log = FALSE)
```

Arguments

n	number of observations. Ignored if at least one of the other parameters have length $k > 1$, in which case, all the parameters are recycled to length k to produce k random variates.
kappa1, kappa2, kappa3	vectors of concentration parameters; $kappa1, kappa2 > 0$, and $kappa3^2 < kappa1 * kappa2$.
mu1, mu2	vectors of mean parameters.
...	additional arguments passed to rmvnorm from package mvtnorm
x	bivariate vector or a two-column matrix with each row being a bivariate vector of angles (in radians) where the densities are to be evaluated.
int.displ	integer displacement. The allowed values are 1, 2, 3, 4 and 5. Default is 3.
log	logical. Should the log density be returned instead?

Details

The bivariate wrapped normal density at the point $x = (x_1, x_2)$ is given by,

$$f(x) = \sqrt{((\kappa_1 \kappa_2 - (\kappa_3)^2)) / (2\pi)} \sum \exp(-1/2 * (\kappa_1(T_1)^2 + \kappa_2(T_2)^2 + 2\kappa_3(T_1)(T_2)))$$

where

$$T_1 = T_1(x, \mu, \omega) = (x_1 - \mu_1(2\pi\omega_1))$$

$$T_2 = T_2(x, \mu, \omega) = (x_2 - \mu_1(2\pi\omega_2))$$

the sum extends over all pairs of integers $\omega = (\omega_1, \omega_2)$, and is approximated by a sum over (ω_1, ω_2) in $\{-M, -M+1, \dots, M-1, M\}^2$ if `int.displ = M`.

Note that above density is essentially the "wrapped" version of a bivariate normal density with mean

$$\mu = (\mu_1, \mu_2)$$

and dispersion matrix $\Sigma = \Delta^{-1}$, where

$$\Delta = \begin{array}{cc} \kappa_1 & \kappa_3 \\ \kappa_3 & \kappa_2 \end{array}$$

Value

`dwnorm2` gives the density and `rwnorm2` generates random deviates.

Examples

```
kappa1 <- c(1, 2, 3)
kappa2 <- c(1, 6, 5)
kappa3 <- c(0, 1, 2)
mu1 <- c(1, 2, 5)
mu2 <- c(0, 1, 3)
x <- diag(2, 2)
n <- 10

# when x is a bivariate vector and parameters are all scalars,
# dwnorm2 returns single density
dwnorm2(x[1, ], kappa1[1], kappa2[1], kappa3[1], mu1[1], mu2[1])

# when x is a two column matrix and parameters are all scalars,
# dwnorm2 returns a vector of densities calculated at the rows of
# x with the same parameters
dwnorm2(x, kappa1[1], kappa2[1], kappa3[1], mu1[1], mu2[1])

# if x is a bivariate vector and at least one of the parameters is
# a vector, all parameters are recycled to the same length, and
# dwnorm2 returns a vector of with ith element being the density
# evaluated at x with parameter values kappa1[i], kappa2[i],
# kappa3[i], mu1[i] and mu2[i]
dwnorm2(x[1, ], kappa1, kappa2, kappa3, mu1, mu2)

# if x is a two column matrix and at least one of the parameters is
# a vector, rows of x and the parameters are recycled to the same
# length, and dwnorm2 returns a vector of with ith element being the
# density evaluated at ith row of x with parameter values kappa1[i],
# kappa2[i], # kappa3[i], mu1[i] and mu2[i]
dwnorm2(x, kappa1, kappa2, kappa3, mu1, mu2)

# when parameters are all scalars, number of observations generated
```



```
# by rwnorm2 is n
rwnorm2(n, kappa1[1], kappa2[1], kappa3[1], mu1[1], mu2[1])

# when at least one of the parameters is a vector, all parameters are
# recycled to the same length, n is ignored, and the number of
# observations generated by rwnorm2 is the same as the length of the
# recycled vectors
rwnorm2(n, kappa1, kappa2, kappa3, mu1, mu2)
```

rwnorm2mix

The bivariate Wrapped Normal mixtures

Description

The bivariate Wrapped Normal mixtures

Usage

```
rwnorm2mix(n, kappa1, kappa2, kappa3, mu1, mu2, pmix, ...)

dwnorm2mix(x, kappa1, kappa2, kappa3, mu1, mu2, pmix, int.displ, log = FALSE)
```

Arguments

n	number of observations.
kappa1, kappa2, kappa3	vectors of concentration parameters; kappa1, kappa2 > 0, kappa3^2 < kappa1*kappa2 for each component.
mu1, mu2	vectors of mean parameters.
pmix	vector of mixture proportions.
...	additional arguments passed to rmvnorm from package <code>mvtnorm</code>
x	matrix of angles (in radians) where the density is to be evaluated, with each row being a single bivariate vector of angles.
int.displ	integer displacement. The allowed values are 1, 2, 3, 4 and 5. Default is 3.
log	logical. Should the log density be returned instead?

Details

All the argument vectors `pmix`, `kappa1`, `kappa2`, `kappa3`, `mu1` and `mu2` must be of the same length, with j -th element corresponding to the j -th component of the mixture distribution.

The bivariate wrapped normal mixture distribution with component size $K = \text{length}(\text{pmix})$ has density

$$g(x) = \sum p[j] * f(x; \kappa_1[j], \kappa_2[j], \kappa_3[j], \mu_1[j], \mu_2[j])$$

where the sum extends over j ; $p[j]$; $\kappa_1[j]$, $\kappa_2[j]$, $\kappa_3[j]$; and $\mu_1[j]$, $\mu_2[j]$ respectively denote the mixing proportion, the three concentration parameters and the two mean parameter for the j -th component, $j = 1, \dots, K$, and $f(\cdot; \kappa_1, \kappa_2, \kappa_3, \mu_1, \mu_2)$ denotes the density function of the wrapped normal distribution with concentration parameters $\kappa_1, \kappa_2, \kappa_3$ and mean parameters μ_1, μ_2 .

Value

dwnorm2mix computes the density and rwnorm2mix generates random deviates from the mixture density.

Examples

```
kappa1 <- c(1, 2, 3)
kappa2 <- c(1, 6, 5)
kappa3 <- c(0, 1, 2)
mu1 <- c(1, 2, 5)
mu2 <- c(0, 1, 3)
pmix <- c(0.3, 0.4, 0.3)
x <- diag(2, 2)
n <- 10

# mixture densities calculated at the rows of x
dwnorm2mix(x, kappa1, kappa2, kappa3, mu1, mu2, pmix)

# number of observations generated from the mixture distribution is n
rwnorm2mix(n, kappa1, kappa2, kappa3, mu1, mu2, pmix)
```

rwnormmix

The univariate Wrapped Normal mixtures

Description

The univariate Wrapped Normal mixtures

Usage

```
rwnormmix(n = 1, kappa, mu, pmix)

dwnormmix(x, kappa, mu, pmix, int.displ = 3, log = FALSE)
```

Arguments

n	number of observations. Ignored if at least one of the other parameters have length $k > 1$, in which case, all the parameters are recycled to length k to produce k random variates.
kappa	vector of component concentration (inverse-variance) parameters, $\text{kappa} > 0$.
mu	vector of component means.
pmix	vector of mixing proportions.
x	vector of angles (in radians) where the densities are to be evaluated.
int.displ	integer displacement. The allowed values are 1, 2, 3, 4 and 5. Default is 3.
log	logical. Should the log density be returned instead?

Details

pmix, mu and kappa must be of the same length, with j -th element corresponding to the j -th component of the mixture distribution.

The univariate wrapped normal mixture distribution with component size $K = \text{length}(\text{pmix})$ has density

$$g(x) = p[1] * f(x; \kappa[1], \mu[1]) + \dots + p[K] * f(x; \kappa[K], \mu[K])$$

where $p[j]$, $\kappa[j]$, $\mu[j]$ respectively denote the mixing proportion, concentration parameter and the mean parameter for the j -th component and $f(\cdot; \kappa, \mu)$ denotes the density function of the (univariate) wrapped normal distribution with mean parameter μ and concentration parameter κ .

Value

dwnormmix computes the density and rwnormmix generates random deviates from the mixture density.

Examples

```
kappa <- 1:3
mu <- 0:2
pmix <- c(0.3, 0.3, 0.4)
x <- 1:10
n <- 10

# mixture densities calculated at each point in x
dwnormmix(x, kappa, mu, pmix)

# number of observations generated from the mixture distribution is n
rwnormmix(n, kappa, mu, pmix)
```

<code>select_chains</code>	<i>Select chains from angmcmc objects</i>
----------------------------	---

Description

Select chains from angmcmc objects

Usage

```
select_chains(object, chain.no, ...)
```

Arguments

<code>object</code>	angular MCMC object.
<code>chain.no</code>	labels of chains to be retained in the final sample
<code>...</code>	unused

Value

Returns another angmcmc object with only selected chains passed through chain.no

Examples

```
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           L = c(10, 12), chains_parallel = FALSE,
                           n.chains = 2)

fit.vmsin.20
fit.vmsin.20.1 <- select_chains(fit.vmsin.20, 1)
fit.vmsin.20.1
```

summary.angmcmc

Summary statistics for parameters from an angmcmc object

Description

Summary statistics for parameters from an angmcmc object

Usage

```
## S3 method for class 'angmcmc'
summary(object, par.name, comp.label, chain.no, ...)
```

Arguments

object	angular MCMC object.
par.name	vector of names of parameters for which point estimates are to be computed. If NULL, results for all parameters are provided.
comp.label	vector of component labels (positive integers, e.g., 1, 2, ...) for which point estimates are to be computed. If NULL, results for all components are provided.
chain.no	vector of chain numbers whose samples are to be used. in the estimation. By default all chains are used.
...	additional arguments affecting the summary produced.

Details

Computes (after thinning and discarding burn-in) point estimates with 95% posterior credible sets for all components and all parameters, together with the sample averages of log likelihood and log posterior density.

Value

Returns a list with elements estimate, lower, upper, llik and lpd. estimate is itself a list with three elements: mean, median and mode providing the sample mean, sample median and (sample) MAP estimates.

Note that `summary.angmcmc` has its own print method, providing a table the estimated mean and 95% credible intervals for each parameter

Examples

```
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1)
summary(fit.vmsin.20)
```

surface_model

Densitysurface for bivariate angular mixture model densities

Description

Densitysurface for bivariate angular mixture model densities

Usage

```
surface_model(model = "vmsin", kappa1, kappa2, kappa3, mu1, mu2,
              pmix = rep(1/length(kappa1), length(kappa1)), xpoints = seq(0, 2 * pi,
              length.out = 50), ypoints = seq(0, 2 * pi, length.out = 50), xlab = "x",
              ylab = "y", zlab = "Density", main, theta = 30, phi = 30,
              shade = 0.01, expand = 0.5, ...)
```

Arguments

model	bivariate angular model whose mixture is of interest. Must be one of "vmsin", "vmcos" and "wnorm2".
kappa1, kappa2, kappa3, mu1, mu2, pmix	model parameters and mixing proportions. See the respective mixture model densities (dvmsinmix , dvmcosmix , dwnorm2mix) for more details.
xpoints	Points on the first (x-) coordinate where the density is to be evaluated. Default to <code>seq(0, 2*pi, length.out=100)</code> .
ypoints	Points on the first (x-) coordinate where the density is to be evaluated. Default to <code>seq(0, 2*pi, length.out=100)</code> .
xlab, ylab, zlab, main, theta, phi, shade, expand	graphical parameters passed to persp
...	additional model specific argument

tim8

*Backbone Dihedral Angles of Triose Phosphate Isomerase (8TIM)***Description**

A dataset consisting of 490 pairs of backbone dihedral angles (in radian scale $[0, 2\pi)$) (ϕ, ψ) for the protein Triose Phosphate Isomerase (8TIM). The angles were obtained first by using the DSSP software on the PDB file for 8TIM to get the backbone angles (in degrees), and then by converting all angles into radians. Due to the presence of different secondary structures (helices, sheets and loops) in the protein, the angular data show considerable variability, and is multimodal with noticeably distinct clusters.

Usage

```
data(tim8)
```

Format

A data frame with 490 rows and 2 variables (backbone dihedral angles) phi and psi.

Source

8TIM PDB file: <http://www.rcsb.org/pdb/explore.do?structureId=8tim>.

DSSP software: <http://swift.cmbi.ru.nl/gv/dssp/>.

waic.angmcmc

*Watanabe-Akaike Information Criterion (WAIC) for angmcmc objects***Description**

Watanabe-Akaike Information Criterion (WAIC) for angmcmc objects

Usage

```
## S3 method for class 'angmcmc'
waic(x, ...)
```

Arguments

x angmcmc object.

... additional model specific arguments to be passed to `waic` from `loo`. For example, `int.displ` specifies integer displacement in `wnorm` and `wnorm2` models. See [fit_wnormmix](#) and [fit_wnorm2mix](#) for more details.

Details

Given a deviance function $D(\eta) = -2 \log(p(y|\eta))$, and an estimate $\eta^* = (\sum \eta_i)/n$ of the posterior mean $E(\eta|y)$, where $y = (y_1, \dots, y_n)$ denote the data, η is the unknown parameter vector of the model, η_1, \dots, η_N are MCMC samples from the posterior distribution of η given y and $p(y|\eta)$ is the likelihood function, the Watanabe-Akaike Information Criterion (WAIC) is defined as

$$WAIC = LPPD - p_W$$

where

$$LPPD = \sum_{i=1}^n \log(N^{-1} \sum_{s=1}^N p(y_i|\eta_s))$$

and (form 1 of)

$$p_W = 2 \sum_{i=1}^n [\log(N^{-1} \sum_{s=1}^N p(y_i|\eta_s)) - N^{-1} \sum_{s=1}^N \log p(y_i|\eta_s)].$$

An alternative form (form 2) for p_W is given by

$$p_W = \sum_{i=1}^n \hat{v}ar \log p(y_i|\eta)$$

where for $i = 1, \dots, n$, $\hat{v}ar \log p(y_i|\eta)$ denotes the estimated variance of $\log p(y_i|\eta)$ based on the realizations η_1, \dots, η_N .

Note that `waic.angmcmc` calls `waic` for computation. If the likelihood contribution of each data point for each MCMC iteration is available in object (can be returned by setting `return_llik_contri = TRUE`) during `fit_angmix` call), `waic.array` is used; otherwise `waic.function` is called. Computation is much faster if the likelihood contributions are available - however, they are very memory intensive, and by default not returned in `fit_angmix`.

Value

Computes the WAIC for a given `angmcmc` object.

Examples

```
# illustration only - more iterations needed for convergence
fit.vmsin.20 <- fit_vmsinmix(tim8, ncomp = 3, n.iter = 20,
                           n.chains = 1, return_llik_contri = TRUE)

library(loo)
waic(fit.vmsin.20)
```

wind	<i>Saturna Island wind directions</i>
------	---------------------------------------

Description

A dataset consisting of 239 observations on wind direction in radians (original measurements were in 10s of degrees), measured at Saturna Island, British Columbia, Canada during October 1-10, 2016 (obtained from Environment Canada website). There was a severe storm during October 4-7, which caused significant fluctuations among the wind directions. As a result the angular data show a clear multimodality.

Usage

```
data(wind)
```

Format

A data frame with 239 rows and 2 columns; the column "angle" provides the angular direction (in radian) and the column day provides the days on which the data points were collected (ranges between 1-10, corresponding to October 1-10, 2016).

Source

Environment Canada: http://climate.weather.gc.ca/climate_data/data_quality_e.html.

CBC news on the storm: <http://www.cbc.ca/news/canada/british-columbia/storm-bc-1.3795204>.

zero_to_2pi	<i>Wrap angles into $[-\pi, \pi]$ or $[0, 2\pi]$</i>
-------------	--

Description

Wrap angles into $[-\pi, \pi]$ or $[0, 2\pi]$

Usage

```
zero_to_2pi(x)
```

```
minuspi_to_pi(x)
```

Arguments

x numeric vector or matrix or data.frame.

Details

minuspi_to_pi wraps x into $[-\pi, \pi]$, while zero_to_pi wraps x into $[0, 2\pi]$.

Examples

```
dat <- matrix(runif(100, -pi, pi), ncol=2)
dat1 <- zero_to_2pi(dat)
dat2 <- minuspi_to_pi(dat1)
all.equal(dat, dat2)
```

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