Package 'boxcoxmix'

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```
License GPL (>= 3)
Description Box-Cox-type transformations for linear and logistic models with random effects us-
      ing non-parametric profile maximum likelihood estimation, as introduced in Almo-
      haimeed (2018) <a href="http://etheses.dur.ac.uk/12831/">http://etheses.dur.ac.uk/12831/</a> and Almohaimeed and Ein-
      beck (2022) <doi:10.1177/1471082X20966919>. The main functions are 'optim.boxcox()' for lin-
      ear models with random effects and 'boxcoxtype()' for logistic models with random effects.
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Description

Box-Cox-type transformations for linear and logistic models with random effects using non-parametric profile maximum likelihood estimation. The main functions are optim.boxcox() for linear models with random effects and boxcoxtype() for logistic models with random effects.

Details

Package: boxcoxmix
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Author(s)

Amani Almohaimeed and Jochen Einbeck

References

Box G. and Cox D. (1964). An analysis of transformations. Journal of the Royal Statistical Society. Series B (Methodological), pages 211-252.

Aitkin, M. A., Francis, B., Hinde, J., and Darnell, R. (2009). Statistical modelling in R. Oxford University Press Oxford.

Jochen Einbeck, Ross Darnell and John Hinde (2014). npmlreg: Nonparametric maximum likelihood estimation for random effect models. R package version 0.46-1.

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R Core Team (2016). R: A language and environment for statistical computing. R Foundation for Statistical Computing, Vienna, Austria. URL https://www.R-project.org/.

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boxcoxtype

Box-Cox-type link function for logistic mixed-effects Models

Description

The boxcoxtype() performs a grid search over the parameter Lambda for logistic mixed-effects models and then optimizes over this grid, to calculate the maximum likelihood estimator of the transformation.

Usage

```
boxcoxtype(
  formula,
  random = ~1,
  k = 3,
  trials = 1,
  data,
  find.in.range = c(-2, 2),
  s = 20,
  plot.opt = 1,
  random.distribution = "np",
  ...
)

boxcoxpower(Lambda = 0)

binomial(link = boxcoxpower(0))
```

Arguments

formula	a formula describing the transformed response and the fixed effect model (e.g. $y \sim x$).
random	a formula defining the random model. Set random= ~1 to model logistic-type overdispersion model. For a two-level logistic-type model, set random= ~1 groups, where groups are at the upper level.
k	the number of mass points.
trials	optional prior weights for the data. For Bernoulli distribution, set trials=1.
data	a data frame containing variables used in the fixed and random effect models.
find.in.range	search in a range of Lambda, with default (-2,2) in step of 0.1.
S	number of points in the grid search of Lambda.

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plot.opt Set plot.opt=1, to plot the profile log-likelihood against Lambda. if plot.opt=0,

no plot is printed.

random.distribution

the mixing distribution, Gaussian Quadrature (gq) or NPML (np) can be set.

extra arguments will be ignored.Lambda the power of the transformationlink the link function to be used.

Details

The Box-Cox transformation (Box & Cox, 1964) is applied to the logistic mixed-effects models with an unspecified mixing distribution. The NPML estimate of the mixing distribution is known to be a discrete distribution involving a finite number of mass-points and corresponding masses (Aitkin et al., 2009). An Expectation-Maximization (EM) algorithm is used for fitting the finite mixture distribution, one needs to specify the number of components k of the finite mixture in advance. This algorithm can be implemented using the npmlreg function alldist for the logistic-type overdispersion model and the npmlreg function allvc for the two-level logistic-type model, setting family = binomial(link = boxcoxpower(Lambda)) where Lambda is the value of the power transformation. When k=1, the npmlreg function alldist() fits the logistic regression model without random effects.

boxcoxtype() performs a grid search over the parameter Lambda and then optimizes over this grid, to calculate the maximum likelihood estimator of the transformation. It produces a plot of the profile likelihood function that summarises information concerning Lambda, including a vertical line indicating the best value of Lambda that maximizes the profile log-likelihood.

Value

List with class boxcoxmix containing:

Maximum the best estimate of Lambda found.

objective the value of the profile log-likelihood corresponding to Maximum.

coef the vector of coefficients.

profile.loglik the profile log-likelihood of the fitted regression model.

fit the fitted all dist object from the last EM iteration.

aic the Akaike information criterion of the fitted regression model.

bic the Bayesian information criterion of the fitted regression model.

The other outcomes are not relevant to users and they are intended for internal use only.

Author(s)

Amani Almohaimeed and Jochen Einbeck

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References

Box G. and Cox D. (1964). An analysis of transformations. Journal of the Royal Statistical Society. Series B (Methodological), pages 211-252.

Aitkin, M. A., Francis, B., Hinde, J., and Darnell, R. (2009). Statistical modelling in R. Oxford University Press Oxford.

Jochen Einbeck, Ross Darnell and John Hinde (2014). npmlreg: Nonparametric maximum likelihood estimation for random effect models. R package version 0.46-1.

See Also

```
np.boxcoxmix, optim.boxcox, tolfind.boxcox, Kfind.boxcox.
```

Examples

```
#Beta blockers data
data("betablocker", package = "flexmix")
library(npmlreg)
betavc <-allvc(cbind(Deaths, Total - Deaths) ~ Treatment, data = betablocker,random=~1 | Center,
    k=3,random.distribution='np',family = binomial(link = boxcoxpower(0)))
betavc$disparity
#[1] 318.7211
betavc 3 < -boxcoxtype(cbind(Deaths, Total - Deaths) ~ Treatment, random = ~1 | Center, random = ~1 | Center
\label{eq:data} \mbox{data = betablocker, find.in.range = c(-2,0.4),s=40,k=3,random.distribution='np')}
#Maximum Profile Log-likelihood: -158.6025 at lambda= -0.56
betavc3$fit$disparity
#[1] 317.2049
betavc3$aic
#[1] 331.2049
betavc3$bic
#[1] 343.6942
```

Kfind.boxcox

Grid search over K for NPML estimation of random effect and variance component models

Description

A grid search over the parameter K, to set the best number of mass-points.

Usage

```
Kfind.boxcox(
  formula,
  groups = 1,
  data,
  lambda = 1,
  EMdev.change = 1e-04,
```

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```
steps = 500,
find.k = c(2, 10),
model.selection = "aic",
start = "gq",
find.tol = c(0, 1.5),
steps.tol = 15,
...
)
```

Arguments

formula a formula describing the transformed response and the fixed effect model (e.g.

 $y \sim x$).

groups the random effects. To fit overdispersion models, set groups = 1.

data a data frame containing variables used in the fixed and random effect models.

lambda a transformation parameter, setting lambda=1 means 'no transformation'.

EMdev.change a small scalar, with default 0.0001, used to determine when to stop EM algo-

rithm.

steps maximum number of iterations for the EM algorithm.

find.k search in a range of K, with default (2,10) in step of 1.

model.selection

Set model.selection="aic", to use Akaike information criterion as model selection criterion or model.selection="bic", to use Bayesian information cri-

terion as model selection criterion.

start a description of the initial values to be used in the fitted model, Quantile-based

version "quantile" or Gaussian Quadrature "gq" can be set.

find. tol search in a range of tol, with default (0,1.5) in step of 1.

steps.tol number of points in the grid search of tol.

... extra arguments will be ignored.

Details

Not only the shape of the distribution causes the skewness it may due to the use of an insufficient number of classes, K. For this, the Kfind.boxcox() function was created to search over a selected range of K and find the best. For each number of classes, a grid search over tol is performed and the tol with the lowest aic or bic value is considered as the optimal. Having the minimal aic or bic values for a whole range of K that have been specified beforehand, the Kfind.boxcox() function can find the best number of the component as the one with the smallest value. It also plots the aic or bic values against the selected range of K, including a vertical line indicating the best value of K that minimizes the model selection criteria. The full range of classes and their corresponding optimal tol can be printed off from the Kfind.boxcox()'s output and used with other **boxcoxmix** functions as starting points.

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Value

List with class boxcoxmix containing:

MinDisparity the minimum disparity found.

Best.K the value of K corresponding to MinDisparity.

AllMinDisparities

a vector containing all minimum disparities calculated on the grid.

AllMintol list of tol values used in the grid.
All.K list of K values used in the grid.

All.aic the Akaike information criterion of all fitted regression models.

All.bic the Bayesian information criterion of all fitted regression models.

Author(s)

Amani Almohaimeed and Jochen Einbeck

See Also

```
tolfind.boxcox.
```

Examples

```
# Fabric data
data(fabric, package = "npmlreg")
teststr<-Kfind.boxcox(y ~ x, data = fabric, start = "gq", groups=1,
find.k = c(2, 3), model.selection = "aic", steps.tol=5)
# Minimal AIC: 202.2114 at K= 2</pre>
```

np.boxcoxmix Response Transformations for Random Effect and Variance Component Models

Description

The function np.boxcoxmix() fits an overdispersed generalized linear model and variance component models using nonparametric profile maximum likelihood.

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Usage

```
np.boxcoxmix(
  formula,
  groups = 1,
  data,
  K = 3,
  tol = 0.5,
  lambda = 1,
  steps = 500,
  EMdev.change = 1e-04,
  plot.opt = 1,
  verbose = TRUE,
  start = "gq",
  ...
)
```

Arguments

Tormula	a formula describing the transformed response and the fixed effect model (e.g.
	$y \sim x$).
groups	the random effects. To fit overdispersion models, set $groups = 1$.

data a data frame containing variables used in the fixed and random effect models.

K the number of mass points.

tol a positive scalar (usually, 0 < tol <= 2)

lambda a transformation parameter, setting lambda=1 means 'no transformation'.

steps maximum number of iterations for the EM algorithm.

EMdev.change a small scalar, with default 0.0001, used to determine when to stop EM algo-

rithm.

plot.opt Set plot.opt=1, to plot the disparity against iteration number. Use plot.opt=2

for tolfind.boxcox() and plot.opt=3 for optim.boxcox().

verbose If set to FALSE, no printed output on progress.

start a description of the initial values to be used in the fitted model, Quantile-based

version "quantile" or Gaussian Quadrature "gq" can be set.

... extra arguments will be ignored.

Details

The Box-Cox transformation (Box & Cox, 1964) is applied to the overdispersed generalized linear models and variance component models with an unspecified mixing distribution. The NPML estimate of the mixing distribution is known to be a discrete distribution involving a finite number of mass-points and corresponding masses (Aitkin et al., 2009). An Expectation-Maximization (EM) algorithm is used for fitting the finite mixture distribution, one needs to specify the number of components K of the finite mixture in advance. To stop the EM-algorithm when it reached its convergence point, we need to defined the convergence criteria that is the absolute change in the successive log-likelihood function values being less than an arbitrary parameter such as

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EMdev.change = 0.0001 (Einbeck et at., 2014). This algorithm can be implemented using the function np.boxcoxmix(), which is designed to account for overdispersed generalized linear models and variance component models using the non-parametric profile maximum likelihood (NPPML) estimation.

The ability of the EM algorithm to locate the global maximum in fewer iterations can be affected by the choice of initial values, the function np.boxcoxmix() allows us to choose from two different methods to set the initial value of the mass points. When option "gq" is set, then Gauss-Hermite masses and mass points are used as starting points in the EM algorithm, while setting start= "quantile" uses the Quantile-based version to select the starting points.

Value

List with class being either boxcoxmix or boxcoxmixpure containing:

mass.point the fitted mass points.

p the masses corresponding to the mixing proportions.

beta the vector of coefficients.

sigma the standard deviation of the mixing distribution (the square root of the vari-

ance).

se the standard error of the estimate.

a matrix of posterior probabilities that element i comes from cluster k.

loglik the log-likelihood of the fitted regression model.

complete.loglik

the complete log-likelihood of the fitted regression model.

disparity the disparity of the fitted regression model.

EMiteration provides the number of iterations of the EM algorithm.

EMconverged TRUE means the EM algorithm converged.

call the matched call.

formula the formula provided.

data the data argument.

aic the Akaike information criterion of the fitted regression model.
bic the Bayesian information criterion of the fitted regression model.

fitted the fitted values for the individual observations.

fitted.transformed

the fitted values for the individual transformed observations.

residuals the difference between the observed values and the fitted values.

residuals.transformed

the difference between the transformed observed values and the transformed

fitted values.

predicted.re a vector of predicted residuals.

The other outcomes are not relevant to users and they are intended for internal use only.

Author(s)

Amani Almohaimeed and Jochen Einbeck

References

Box G. and Cox D. (1964). An analysis of transformations. Journal of the Royal Statistical Society. Series B (Methodological), pages 211-252.

Aitkin, M. A., Francis, B., Hinde, J., and Darnell, R. (2009). Statistical modelling in R. Oxford University Press Oxford.

Jochen Einbeck, Ross Darnell and John Hinde (2014). npmlreg: Nonparametric maximum likelihood estimation for random effect models. R package version 0.46-1.

See Also

optim.boxcox, tolfind.boxcox.

Examples

optim.boxcox

Response Transformations for Random Effect and Variance Component Models

Description

The optim.boxcox() performs a grid search over the parameter lambda for overdispersed generalized linear models and variance component models and then optimizes over this grid, to calculate the maximum likelihood estimator of the transformation.

Usage

```
optim.boxcox(
  formula,
  groups = 1,
  data,
  K = 3,
  steps = 500,
  tol = 0.5,
  start = "gq",
  EMdev.change = 1e-04,
  find.in.range = c(-3, 3),
  s = 60,
  plot.opt = 3,
  verbose = FALSE,
  noformat = FALSE,
  ...
)
```

Arguments

formula	a formula describing the transformed response and the fixed effect model (e.g. $y \sim x$).
groups	the random effects. To fit overdispersion models, set groups = 1 .
data	a data frame containing variables used in the fixed and random effect models.
K	the number of mass points.
steps	maximum number of iterations for the EM algorithm.
tol	a positive scalar (usually, 0 <to1 <="2)</td"></to1>
start	a description of the initial values to be used in the fitted model, Quantile-based version "quantile" or Gaussian Quadrature "gq" can be set.
EMdev.change	a small scalar, with default 0.0001 , used to determine when to stop EM algorithm.
find.in.range	search in a range of lambda, with default (-3,3) in step of 0.1.
S	number of points in the grid search of lambda.
plot.opt	Set plot.opt=3, to plot the disparity against iteration number and the profile log-likelihood against lambda. Use plot.opt=0, to only plot the profile log-likelihood against lambda.
verbose	If set to FALSE, no printed output on progress.
noformat	Set noformat = TRUE, to change the formatting of the plots.
	extra arguments will be ignored.

Details

The Box-Cox transformation (Box & Cox, 1964) is applied to the overdispersed generalized linear models and variance component models with an unspecified mixing distribution. The NPML

estimate of the mixing distribution is known to be a discrete distribution involving a finite number of mass-points and corresponding masses (Aitkin et al., 2009). An Expectation-Maximization (EM) algorithm is used for fitting the finite mixture distribution, one needs to specify the number of components K of the finite mixture in advance. To stop the EM-algorithm when it reached its convergence point, we need to defined the convergence criteria that is the absolute change in the successive log-likelihood function values being less than an arbitrary parameter such as EMdev.change = 0.0001 (Einbeck et at., 2014). This algorithm can be implemented using the function np.boxcoxmix(), which is designed to account for overdispersed generalized linear models and variance component models using the non-parametric profile maximum likelihood (NPPML) estimation.

The ability of the EM algorithm to locate the global maximum in fewer iterations can be affected by the choice of initial values, the function optim.boxcox() allows us to choose from two different methods to set the initial value of the mass points. When option "gq" is set, then Gauss-Hermite masses and mass points are used as starting points in the EM algorithm, while setting start= "quantile" uses the Quantile-based version to select the starting points.

optim.boxcox() performs a grid search over the parameter lambda and then optimizes over this grid, to calculate the maximum likelihood estimator of the transformation. It produces a plot of the non-parametric profile likelihood function that summarises information concerning lambda, including a vertical line indicating the best value of lambda that maximizes the non-parametric profile log-likelihood.

Value

List with class boxcoxmix containing:

All.lambda list of lambda values used in the grid.

Maximum the best estimate of lambda found.

objective the value of the profile log-likelihood corresponding to Maximum.

EMconverged 1 is TRUE, means the EM algorithm converged.

EMiteration provides the number of iterations of the EM algorithm.

mass.point the fitted mass points.

p the masses corresponding to the mixing proportions.

beta the vector of coefficients.

sigma the standard deviation of the mixing distribution (the square root of the vari-

ance).

se the standard error of the estimate.

w a matrix of posterior probabilities that element i comes from cluster k.

loglik the profile log-likelihood of the fitted regression model.

profile.loglik the profile complete log-likelihood of the fitted regression model.

disparity the disparity of the fitted regression model.

call the matched call.
formula the formula provided.
data the data argument.

```
aic the Akaike information criterion of the fitted regression model.

fitted the fitted values for the individual observations.

fitted.transformed the fitted values for the individual transformed observations.

residuals the difference between the observed values and the fitted values.

residuals.transformed the difference between the transformed observed values and the transformed fitted values.

predicted.re a vector of predicted residuals.
```

The other outcomes are not relevant to users and they are intended for internal use only.

Author(s)

Amani Almohaimeed and Jochen Einbeck

References

Box G. and Cox D. (1964). An analysis of transformations. Journal of the Royal Statistical Society. Series B (Methodological), pages 211-252.

Aitkin, M. A., Francis, B., Hinde, J., and Darnell, R. (2009). Statistical modelling in R. Oxford University Press Oxford.

Jochen Einbeck, Ross Darnell and John Hinde (2014). npmlreg: Nonparametric maximum likelihood estimation for random effect models. R package version 0.46-1.

See Also

```
np.boxcoxmix, tolfind.boxcox.
```

Examples

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plot.boxcoxmix	Plot diagnostics for boxcoxmix functions	
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Description

plot() is a generic function used to produce some useful diagnostic plotting of the functions: np.boxcoxmix(), optim.boxcox() and tolfind.boxcox().

Usage

```
## S3 method for class 'boxcoxmix'
plot(x, plot.opt = 1, ...)
```

Arguments

x an object for which a plot is desired.plot.opt an integer value between 1 and 8.additional arguments.

Value

The plots to be printed depend on the number given in plot.opt, for the np.boxcoxmix(), optim.boxcox() and tolfind.boxcox() functions:

1	the disparities with the iteration number against the mass points
2	the fitted value against the response of the original and the transformed Data.
3	probability plot of residuals of the original against the transformed data.
4	individual posterior probabilities.
5	control charts of residuals of the original against the transformed data.
6	The histograms of residuals of the original against the transformed data.
7	works only for the tolfind.boxcox() function and plots the specified range of tol against the disparities
8	works only for the optim.boxcox() function and gives the profile likelihood function that summarises information concerning lambda.
9	works only for the Kfind.boxcox() function and plots the specified range of K against the AIC or BIC information criteria
10	works only for the boxcoxtype() function and gives the profile likelihood function that summarises information concerning lambda for generalized linear Mixedeffects Models.

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print.boxcoxmix	Summary of boxcoxmix functions

Description

summary() and print() are generic functions used to produce the results of the functions: np.boxcoxmix(),
optim.boxcox() and tolfind.boxcox().

Usage

```
## S3 method for class 'boxcoxmix'
print(x, digits = max(3, getOption("digits") - 3), na.print = "", ...)
## S3 method for class 'boxcoxmixpure'
print(x, digits = max(3, getOption("digits") - 3), na.print = "", ...)
## S3 method for class 'boxcoxmix'
summary(object, digits = max(3, getOption("digits") - 3), ...)
## S3 method for class 'boxcoxmixpure'
summary(object, digits = max(3, getOption("digits") - 3), ...)
```

Arguments

X	an object for which a summary is desired.
digits	an integer number format.
na.print	a character string which is used to indicate NA values output format.
	additional arguments.
object	an object for which a summary is desired.

Value

Return invisibly the main object provided, while print a summary of its content.

tolfind.boxcox	Grid search over tol for NPPML estimation of random effect and variance component models
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Description

A grid search over the parameter to1, to set the initial values of the EM algorithm.

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Usage

```
tolfind.boxcox(
  formula,
 groups = 1,
 data,
 K = 3,
 lambda = 1,
 EMdev.change = 1e-04,
 plot.opt = 2,
 s = 15,
  steps = 500,
  find.in.range = c(0, 1.5),
 start = "gq",
 verbose = FALSE,
 noformat = FALSE,
)
```

Arguments

formula

	$y \sim x$).
groups	the random effects. To fit overdispersion models , set $groups = 1$.
data	a data frame containing variables used in the fixed and random effect models.
K	the number of mass points.
lambda	a transformation parameter, setting lambda=1 means 'no transformation'.
EMdev.change	a small scalar, with default 0.0001 , used to determine when to stop EM algorithm.
plot.opt	Set plot.opt=2, to plot the EM trajectories and the development of the disparity over iteration number. And plot.opt=0, for none of them.
S	number of points in the grid search of tol.
steps	maximum number of iterations for the EM algorithm.
find.in.range	search in a range of tol, with default $(0,1.5)$ in step of 0.1 .
start	a description of the initial values to be used in the fitted model, Quantile-based version "quantile" or Gaussian Quadrature "gq" can be set.
verbose	If set to FALSE, no printed output on progress.
noformat	Set noformat = TRUE, to change the formatting of the plots.
	extra arguments will be ignored.

a formula describing the transformed response and the fixed effect model (e.g.

Details

A grid search over tol can be performed using tolfind.boxcox() function, which works for np.boxcoxmix() to find the optimal solution.

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Value

List with class boxcoxmix containing:

MinDisparity the minimum disparity found.

Mintol the value of tol corresponding to MinDisparity.

AllDisparities

a vector containing all disparities calculated on the grid.

Alltol list of tol values used in the grid.

AllEMconverged

1 is TRUE, means the EM algorithm converged.

aic the Akaike information criterion of the fitted regression model.
bic the Bayesian information criterion of the fitted regression model.

Author(s)

Amani Almohaimeed and Jochen Einbeck

See Also

```
np.boxcoxmix.
```

Examples

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