Package 'depmixS4'

| May 11, 2025 | | |
|---|--|--|
| Version 1.5-1 | | |
| Date 2025-05-10 | | |
| Title Dependent Mixture Models - Hidden Markov Models of GLMs and Other Distributions in S4 | | |
| Depends R (>= 4.0.0), nnet, MASS, Rsolnp, nlme | | |
| Imports stats, stats4, methods | | |
| Suggests gamlss, gamlss.dist, Rdonlp2 | | |
| Additional_repositories http://R-Forge.R-project.org | | |
| Description Fits latent (hidden) Markov models on mixed categorical and continuous (time series) data, otherwise known as dependent mixture models, see Visser & Speekenbrink (2010, <doi:10.18637 jss.v036.i07="">).</doi:10.18637> | | |
| License GPL (>= 2) | | |
| <pre>URL https://depmix.github.io/</pre> | | |
| RoxygenNote 6.1.0 | | |
| NeedsCompilation yes | | |
| Author Ingmar Visser [aut, cre], Maarten Speekenbrink [aut] | | |
| Maintainer Ingmar Visser <i.visser@uva.nl></i.visser@uva.nl> | | |
| Repository CRAN | | |
| Date/Publication 2025-05-11 07:10:05 UTC | | |
| Contents | | |
| depmixS4-package2balance3depmix4depmix-class8depmix-methods9depmix.fitted-class12depmix.sim-class13 | | |

2 depmixS4-package

| depmixS4-package | | depmixS4 provides classes for specifying and fitting hidden Marko models | | | | | |
|------------------|------------------|---|------|--|--|--|--|
| Index | | | 54 | | | | |
| | viterbi | | . 51 | | | | |
| | | | | | | | |
| | | | | | | | |
| | • | | | | | | |
| | 1 | | | | | | |
| | = | | | | | | |
| | | | | | | | |
| | * | | | | | | |
| | * | | | | | | |
| | * | | | | | | |
| | = | | | | | | |
| | | | | | | | |
| | mix.sim-class | | | | | | |
| | mix.fitted-class | | . 33 | | | | |
| | mix-class | | . 32 | | | | |
| | mix | | . 30 | | | | |
| | makeDepmix | | . 25 | | | | |
| | - | | | | | | |
| | | | | | | | |
| | • | | | | | | |
| | | | | | | | |
| | | | | | | | |
| | em.control | | . 14 | | | | |

Description

depmixS4 is a framework for specifying and fitting dependent mixture models, otherwise known as hidden or latent Markov models. Optimization is done with the EM algorithm or optionally with Rdonlp2 when (general linear (in-)equality) constraints on the parameters need to be incorporated. Models can be fitted on (multiple) sets of observations. The response densities for each state may be chosen from the GLM family, or a multinomial. User defined response densities are easy to add; for the latter an example is given for the ex-gauss distribution as well as the multivariate normal distribution.

Mixture or latent class (regression) models can also be fitted; these are the limit case in which the length of observed time series is 1 for all cases.

Details

Model fitting is done in two steps; first, models are specified through the depmix function (or the mix function for mixture and latent class models), which both use standard glm style arguments

balance 3

to specify the observed distributions; second, the model needs to be fitted by using the fit function; imposing constraints is done through the fit function. Standard output includes the optimized parameters and the posterior densities for the states and the optimal state sequence.

For full control and the possibility to add new response distributions, check the makeDepmix help page.

Author(s)

Ingmar Visser & Maarten Speekenbrink

Maintainer: i.visser@uva.nl

References

Ingmar Visser and Maarten Speekenbrink (2010). depmixS4: An R Package for Hidden Markov Models. *Journal of Statistical Software*, 36(7), p. 1-21.

On hidden Markov models: Lawrence R. Rabiner (1989). A tutorial on hidden Markov models and selected applications in speech recognition. *Proceedings of IEEE*, 77-2, p. 267-295.

On latent class models: A. L. McCutcheon (1987). Latent class analysis. Sage Publications.

See Also

```
depmix, fit
```

Examples

```
# create a 2 state model with one continuous and one binary response
data(speed)
mod <- depmix(list(rt~1,corr~1),data=speed,nstates=2,family=list(gaussian(),multinomial()))
# print the model, formulae and parameter values (ie the starting values)
mod</pre>
```

balance

Balance Scale Data

Description

Balance scale data of four distance items from 779 participants; participants ages are included.

Usage

```
data(balance)
```

Format

A data frame with 779 observations on the following variables. The full dataset is described and analyzed extensively in Jansen & Van der Maas (2002). The trichotomous data are left, balance, right. The dichotomous version of the data is scored correct, incorrect.

```
sex Participants sex.
```

agedays Age in days.

age Age in years.

- t1 Trichotomously scored distance item.
- t2 Trichotomously scored distance item.
- t3 Trichotomously scored distance item.
- t4 Trichotomously scored distance item.
- d1 Dichotomously scored distance item.
- d2 Dichotomously scored distance item.
- d3 Dichotomously scored distance item.
- d4 Dichotomously scored distance item.

Source

Brenda Jansen & Han van der Maas (2002). The development of children's rule use on the balance scale task. *Journal of experimental Child Psychology*, 81, p. 383-416.

Examples

data(balance)

depmix

Dependent Mixture Model Specifiction

Description

depmix creates an object of class depmix, a dependent mixture model, otherwise known as hidden Markov model. For a short description of the package see depmixS4. See the vignette for an introduction to hidden Markov models and the package.

Usage

```
depmix(response, data=NULL, nstates, transition=~1, family=gaussian(),
prior=~1, initdata=NULL, respstart=NULL, trstart=NULL, instart=NULL,
ntimes=NULL,...)
```

Arguments

The response to be modeled; either a formula or a list of formulae (in the multiresponse variate case); this interfaces to the glm and other distributions. See 'Details'. data An optional data. frame to interpret the variables in the response and transition arguments. The number of states of the model. nstates A one-sided formula specifying the model for the transitions. See 'Details'. transition family A family argument for the response. This must be a list of family's if the response is multivariate. A one-sided formula specifying the density for the prior or initial state probabilprior initdata An optional data frame to interpret the variables occuring in prior. The number of rows of this data.frame must be equal to the number of cases being modeled, length(ntimes). See 'Details'. Starting values for the parameters of the response models. respstart trstart Starting values for the parameters of the transition models. instart Starting values for the parameters of the prior or initial state probability model. A vector specifying the lengths of individual, i.e. independent, time series. ntimes If not specified, the responses are assumed to form a single time series, i.e. ntimes=nrow(data). If the data argument has an attribute ntimes, then this is used. The first example in fit uses this argument. Not used currently.

Details

The function depmix creates an S4 object of class depmix, which needs to be fitted using fit to optimize the parameters.

The response model(s) are by default created by call(s) to GLMresponse using the formula and the family arguments, the latter specifying the error distribution. See GLMresponse for possible values of the family argument for glm-type responses (ie a subset of the glm family options, and the multinomial). Alternative response distributions are specified by using the makeDepmix function. Its help page has examples of specifying a model with a multivariate normal response, as well as an example of adding a user-defined response model, in this case for the ex-gauss distribution.

If response is a list of formulae, the response's are assumed to be independent conditional on the latent state.

The transitions are modeled as a multinomial logistic model for each state. Hence, the transition matrix can be modeled using time-varying covariates. The prior density is also modeled as a multinomial logistic. Both of these models are created by calls to transInit.

Starting values for the initial, transition, and response models may be provided by their respective arguments. NB: note that the starting values for the initial and transition models as well as of the multinomial logit response models are interpreted as probabilities, and internally converted to multinomial logit parameters. The order in which parameters must be provided can be easily studied by using the setpars and getpars functions.

Linear constraints on parameters can be provided as argument to the fit function.

The print function prints the formulae for the response, transition and prior models along with their parameter values.

Missing values are allowed in the data, but missing values in the covariates lead to errors.

Value

depmix returns an object of class depmix which has the following slots:

response A list of a list of response models; the first index runs over states; the second

index runs over the independent responses in case a multivariate response is

provided.

transition A list of transInit models, ie multinomial logistic models with length the

number of states.

prior A multinomial logistic model for the initial state probabilities.

dens, trDens, init

See depmix-class help for details. For internal use.

stationary Logical indicating whether the transitions are time-dependent or not; for internal

use.

ntimes A vector containing the lengths of independent time series.

nstates The number of states of the model.

nresp The number of independent responses.

npars The total number of parameters of the model. Note: this is *not* the degrees of

freedom because there are redundancies in the parameters, in particular in the

multinomial models for the transitions and prior probabilities.

Note

Models are not fitted; the return value of depmix is a model specification without optimized parameter values. Use the fit function to optimize parameters, and to specify additional constraints.

Author(s)

Ingmar Visser & Maarten Speekenbrink

References

Ingmar Visser and Maarten Speekenbrink (2010). depmixS4: An R Package for Hidden Markov Models. *Journal of Statistical Software*, *36*(7), p. 1-21.

Lawrence R. Rabiner (1989). A tutorial on hidden Markov models and selected applications in speech recognition. *Proceedings of IEEE*, 77-2, p. 267-295.

See Also

fit, transInit, GLMresponse, depmix-methods for accessor functions to depmix objects.

For full control see the makeDepmix help page and its example section for the possibility to add user-defined response distributions.

Examples

```
# create a 2 state model with one continuous and one binary response
# ntimes is used to specify the lengths of 3 separate series
data(speed)
mod <- depmix(list(rt~1,corr~1),data=speed,nstates=2,</pre>
    family=list(gaussian(),multinomial("identity")),ntimes=c(168,134,137))
# print the model, formulae and parameter values
mod
set.seed(1)
# fit the model by calling fit
fm <- fit(mod)</pre>
# Volatility of S & P 500 returns
# (thanks to Chen Haibo for providing this example)
data(sp500)
# fit some models
msp <- depmix(logret~1,nstates=2,data=sp500)</pre>
set.seed(1)
fmsp <- fit(msp)</pre>
# plot posterior state sequence for the 2-state model
plot(ts(posterior(fmsp, type="smoothing")[,1], start=c(1950,2),deltat=1/12),ylab="probability",
main="Posterior probability of state 1 (volatile, negative markets).",
frame=FALSE)
## Not run:
# this creates data with a single change point with Poisson data
set.seed(3)
y1 <- rpois(50,1)
y2 <- rpois(50,2)
ydf <- data.frame(y=c(y1,y2))</pre>
# fit models with 1 to 3 states
m1 <- depmix(y~1,ns=1,family=poisson(),data=ydf)</pre>
set.seed(1)
fm1 <- fit(m1)
m2 <- depmix(y~1,ns=2,family=poisson(),data=ydf)
set.seed(1)
fm2 <- fit(m2)
m3 \leftarrow depmix(y^1, ns=3, family=poisson(), data=ydf)
set.seed(1)
fm3 <- fit(m3,em=em.control(maxit=500))</pre>
# plot the BICs to select the proper model
plot(1:3,c(BIC(fm1),BIC(fm2),BIC(fm3)),ty="b")
## End(Not run)
```

8 depmix-class

```
## Not run:
# similar to the binomial model, data may also be entered in
# multi-column format where the n for each row can be different
dt <- data.frame(y1=c(0,1,1,2,4,5),y2=c(1,0,1,0,1,0),y3=c(4,4,3,2,1,1))
# specify a mixture model ...
m2 <- mix(cbind(y1,y2,y3)~1,data=dt,ns=2,family=multinomial("identity"))
set.seed(1)
fm2 <- fit(m2)
# ... or dependent mixture model
dm2 <- depmix(cbind(y1,y2,y3)~1,data=dt,ns=2,family=multinomial("identity"))
set.seed(1)
fdm2 <- fit(dm2)
## End(Not run)</pre>
```

depmix-class

Class "depmix"

Description

A depmix model.

Slots

response: List of list of response objects. transition List of transInit objects.

prior: transInit object.

dens: Array of dimension sum(ntimes)*nresp*nstates providing the densities of the observed responses for each state.

trDens: Array of dimension sum(ntimes)*nstates providing the probability of a state transition depending on the predictors.

init: Array of dimension length(ntimes)*nstates with the current predictions for the initial state probabilities.

homogeneous: Logical indicating whether the transitions are time-dependent or not; for internal

ntimes: A vector containing the lengths of independent time series; if data is provided, sum(ntimes) must be equal to nrow(data).

nstates: The number of states of the model.

nresp: The number of independent responses.

npars: The total number of parameters of the model. This is not the degrees of freedom, ie there are redundancies in the parameters, in particular in the multinomial models for the transitions and prior.

depmix-methods 9

Accessor Functions

The following functions should be used for accessing the corresponding slots:

npar: The number of parameters of the model.nresp: The number of responses.nstates: The number of states.ntimes: The vector of independent time series lengths.

Author(s)

Ingmar Visser & Maarten Speekenbrink

depmix-methods

'depmix' and 'mix' methods.

Description

Various methods for depmix and mix objects.

Usage

```
## S4 method for signature 'depmix'
logLik(object,method=c("fb","lystig","classification"),na.allow=TRUE)
## S4 method for signature 'mix'
logLik(object,method=c("fb","lystig","classification"),na.allow=TRUE)
## S4 method for signature 'depmix.fitted.classLik'
logLik(object,method=c("classification","fb","lystig"),na.allow=TRUE)
## S4 method for signature 'mix.fitted.classLik'
logLik(object,method=c("classification","fb","lystig"),na.allow=TRUE)
## S4 method for signature 'depmix'
nobs(object, ...)
## S4 method for signature 'mix'
nobs(object, ...)
## S4 method for signature 'depmix'
npar(object)
## S4 method for signature 'mix'
npar(object)
## S4 method for signature 'depmix'
freepars(object)
## S4 method for signature 'mix'
freepars(object)
```

10 depmix-methods

```
## S4 method for signature 'depmix'
setpars(object, values, which="pars",...)
## S4 method for signature 'mix'
setpars(object, values, which="pars",...)
## S4 method for signature 'depmix'
getpars(object, which="pars",...)
## S4 method for signature 'mix'
getpars(object, which="pars",...)
## S4 method for signature 'depmix'
getmodel(object, which="response", state=1, number=1)
## S4 method for signature 'mix'
getmodel(object, which="response", state=1, number=1)
```

Arguments

object A depmix or mix object.

values To be used in setpars to set new parameter values; see the example.

method The log likelihood can be computed by either the forward backward algorithm

(Rabiner, 1989), or by the method of Lystig and Hughes, 2002. The former is the default and implemented in a fast C routine. The forward-backward routine also computes the state and transition smoothed probabilities, which are not directly neccessary for the log likelihood. Those smoothed variables, and the forward and backward variables are accessible through the forwardbackward function. When method="classification", the classification likelihood is computed, which is the likelihood of the data assuming the state sequence is known and equal to the maximum a posteriori state sequence. The MAP state sequence is available through the viterbi function. The classification likelihood is comuted by default when calling the logLik method on an a model fitted by maximising the

classification likelihood.

Allow missing observations? When set to FALSE, the logLik method will return NA in the presence of missing observations. When set to TRUE, missing values will be ignored when computing the likelihood. When observations are partly

missing (when a multivariate observation has missing values on only some of its

dimensionis), this may give unexpected results.

getpars function: The default "pars" returns a vector of all parameters of a depmix object; the alternative value "fixed" returns a logical vector of the same length indicating which parameters are fixed. The setpars functions sets parameters to new values; setpars also recomputes the dens, trans and init slots of depmix objects. Note that the getpars and setpars functions for depmix objects simply call the functions of the same name for the response and transition

models.

getmodel function: possible values are "response" (the default), "prior" and

"transition" to return the corresponding submodels.

In getmodel this determines the submodel to be returned (together with number in the case of response models); when which="transition", getmodel returns the

transition submodel for state=state.

na.allow

which

state

depmix-methods 11

number In getmodel this determines the "response" model to be returned from state

state.

... Not used currently.

Value

logLik returns a logLik object with attributes df and nobs.

nobs returns the number of observations (used in computing the BIC).

npar returns the number of paramaters of a model.

freepars returns the number of non-redundant parameters.

setpars returns a (dep-)mix object with new parameter values.

getpars returns a vector with the current parameter values.

getmodel returns a submodel of a (dep-)mix model; the prior model, one of the transition

models (determined by argument state) or one of the response models (deter-

mined by arguments state and number).

Author(s)

Ingmar Visser & Maarten Speekenbrink

Examples

```
# create a 2 state model with one continuous and one binary response
data(speed)
mod <- depmix(list(rt~1,corr~1),data=speed,nstates=2,family=list(gaussian(),multinomial()))
getmodel(mod,"response",2,1)
getmodel(mod,"prior")

# get the loglikelihood of the model
logLik(mod)

# to see the ordering of parameters to use in setpars
mod <- setpars(mod, value=1:npar(mod))
mod

# to see which parameters are fixed (by default only baseline parameters in
# the multinomial logistic models for the transition models and the initial
# state probabilities model)
mod <- setpars(mod, getpars(mod,which="fixed"))
mod</pre>
```

12 depmix.fitted-class

Description

A fitted depmix model.

Slots

A depmix fitted object is a depmix object with three additional slots, here is the complete list:

response: List of list of response objects.

transition List of transInit objects.

prior: transInit object.

dens: Array of dimension sum(ntimes)*nresp*nstates providing the densities of the observed responses for each state.

trDens: Array of dimension sum(ntimes)*nstates providing the probability of a state transition depending on the predictors.

init: Array of dimension length(ntimes)*nstates with the current predictions for the initial state probabilities.

stationary: Logical indicating whether the transitions are time-dependent or not; for internal use.

ntimes: A vector containing the lengths of independent time series; if data is provided, sum(ntimes) must be equal to nrow(data).

nstates: The number of states of the model.

nresp: The number of independent responses.

npars: The total number of parameters of the model. This is not the degrees of freedom, ie there are redundancies in the parameters, in particular in the multinomial models for the transitions and prior.

message: This provides some information on convergence, either from the EM algorithm or from Rdonlp2.

conMat: The linear constraint matrix, which has zero rows if there were no constraints.

lin.lower The lower bounds on the linear constraints.

lin.upper The upper bounds on the linear constraints.

posterior: Posterior (Viterbi) state sequence.

Details

The print function shows some convergence information, and the summary method shows the parameter estimates.

depmix.sim-class 13

Extends

depmix.fitted extends the "depmix" class directly. depmix.fitted.classLik is similar to depmix.fitted, the only difference being that the model is fitted by maximising the classification likelihood.

Author(s)

Ingmar Visser & Maarten Speekenbrink

depmix.sim-class

Class "depmix.sim"

Description

A depmix.sim model. The depmix.sim class directly extends the depmix class, and has an additional slot for the true states. A depmix.sim model can be generated by simulate(mod,...), where mod is a depmix model.

Slots

response: List of list of response objects.

transition List of transInit objects.

prior: transInit object.

dens: Array of dimension sum(ntimes)*nresp*nstates providing the densities of the observed responses for each state.

trDens: Array of dimension sum(ntimes)*nstates providing the probability of a state transition depending on the predictors.

init: Array of dimension length(ntimes)*nstates with the current predictions for the initial state probabilities.

homogeneous: Logical indicating whether the transitions are time-dependent or not; for internal use.

ntimes: A vector containing the lengths of independent time series; if data is provided, sum(ntimes) must be equal to nrow(data).

nstates: The number of states of the model.

nresp: The number of independent responses.

npars: The total number of parameters of the model. This is not the degrees of freedom, ie there are redundancies in the parameters, in particular in the multinomial models for the transitions and prior.

states: A matrix with the true states.

14 em.control

Accessor Functions

The following functions should be used for accessing the corresponding slots:

npar: The number of parameters of the model.

nresp: The number of responses. nstates: The number of states.

ntimes: The vector of independent time series lengths.

Author(s)

Maarten Speekenbrink & Ingmar Visser

em.control

Control parameters for the EM algorithm

Description

Set control parameters for the EM algorithm.

Usage

```
em.control(maxit = 500, tol = 1e-08, crit = c("relative", "absolute"),
random.start = TRUE, classification = c("soft", "hard"))
```

Arguments

maxit The maximum number of iterations.

tol The tolerance level for convergence. See Details.

crit Sets the convergence criterion to "relative" or "absolute" change of the log-

likelihood. See Details.

random.start This is used for a (limited) random initialization of the parameters. See Details.

classification Type of classification to states used. See Details.

Details

The argument crit sets the convergence criterion to either the relative change in the log-likelihood or the absolute change in the log-likelihood. The relative likelihood criterion (the default) assumes convergence on iteration i when $\frac{\log L(i) - \log L(i-1)}{\log L(i-1)} < tol$. The absolute likelihood criterion assumes convergence on iteration i when $\log L(i) - \log L(i-1) < tol$. Use crit="absolute" to invoke the latter convergence criterion. Note that in that case, optimal values of the tolerance parameter tol scale with the value of the log-likelihood (and these are not changed automagically).

Argument random.start This is used for a (limited) random initialization of the parameters. In particular, if random.start=TRUE, the (posterior) state probabilities are randomized at iteration 0 (using a uniform distribution), i.e. the γ variables (Rabiner, 1989) are sampled from the Dirichlet

em.control 15

distribution with a (currently fixed) value of $\alpha=0.1$; this results in values for each row of γ that are quite close to zero and one; note that when these values are chosen at zero and one, the initialization is similar to that used in kmeans. Random initialization is useful when no initial parameters can be given to distinguish between the states. It is also useful for repeated estimation from different starting values.

Argument classification is used to choose either soft (default) or hard classification of observations to states. When using soft classification, observations are assigned to states with a weight equal to the posterior probability of the state. When using hard classification, observations are assigned to states according to the maximum a posteriori (MAP) states (i.e., each observation is assigned to one state, which is determined by the Viterbi algorithm in the case of depmix models). As a result, the EM algorithm will find a local maximum of the classification likelihood (Celeux & Govaert, 1992). Warning: hard classification is an experimental feature, especially for hidden Markov models, and its use is currently not advised.

Value

em. control returns a list of the control parameters.

Author(s)

Maarten Speekenbrink & Ingmar Visser

References

Lawrence R. Rabiner (1989). A tutorial on hidden Markov models and selected applications in speech recognition. *Proceedings of IEEE*, 77-2, p. 267-295.

Gilles Celeux and Gerard Govaert (1992). A classification EM algorithm for clustering and two stochastic versions. *Computational Statistics and Data Analysis*, 14, p. 315-332.

Examples

fit

Fit 'depmix' or 'mix' models

Description

fit optimizes parameters of depmix or mix models, optionally subject to general linear (in)equality constraints.

Usage

```
## S4 method for signature 'mix'
fit(object, fixed=NULL, equal=NULL,
conrows=NULL, conrows.upper=NULL, conrows.lower=NULL,
method=NULL, verbose=FALSE,
emcontrol=em.control(),
solnpcntrl=list(rho = 1, outer.iter = 400, inner.iter = 800,
delta = 1e-7, tol = 1e-8),
donlpcntrl=donlp2Control(),
...)
## S4 method for signature 'mix.fitted'
summary(object,which="all")
## S4 method for signature 'depmix.fitted'
summary(object,which="all")
```

Arguments

| object | An object of class (dep-)mix. |
|----------------|--|
| fixed | Vector of mode logical indicating which parameters should be fixed. |
| equal | Vector indicating equality constraints; see Details. |
| conrows | Rows of a general linear constraint matrix; see Details. |
| conrows.upper, | conrows.lower |
| | Upper and lower bounds for the linear constraints; see Details. |
| method | The optimization method; mostly determined by constraints. |
| verbose | Should optimization information be displayed on screen? |
| emcontrol | Named list with control parameters for the EM algorithm (see em.control). |
| solnpcntrl | Control parameters passed to the 'rsolnp' optimizer; see solnp for explanation and defaults used there. |
| donlpcntrl | Control parameters passed to 'donlp' optimizer; see ?donlp2Control for explanation and defaults used there; this can be used to tweak optimization but note that extra output is not returned. |
| which | Should summaries be provided for "all" submodels? Options are "prior", "response", and for fitted depmix models also "transition". |
| | Further arguments passed on to the optimization methods. |

Details

Models are fitted by the EM algorithm if there are no constraints on the parameters. Aspects of the EM algorithm can be controlled through the emcontrol argument; see details in em. control. Otherwise the general optimizers solnp, the default (from package Rsolnp) or donlp2 (from package Rdonlp2) are used which handle general linear (in-)equality constraints. These optimizers are selected by setting method='rsolnp' or method='donlp' respectively.

Three types of constraints can be specified on the parameters: fixed, equality, and general linear (in)equality constraints. Constraint vectors should be of length npar(object); note that this hence includes redundant parameters such as the base category parameter in multinomial logistic models which is always fixed at zero. See help on getpars and setpars about the ordering of parameters.

The equal argument is used to specify equality constraints: parameters that get the same integer number in this vector are estimated to be equal. Any integers can be used in this way except 0 and 1, which indicate fixed and free parameters, respectively.

Using solnp (or donlp2), a Newton-Raphson scheme is employed to estimate parameters subject to linear constraints by imposing:

```
bl \le A*x \le bu,
```

where x is the parameter vector, bl is a vector of lower bounds, bu is a vector of upper bounds, and A is the constraint matrix.

The conrows argument is used to specify rows of A directly, and the conrows.lower and conrows.upper arguments to specify the bounds on the constraints. conrows must be a matrix of npar(object) columns and one row for each constraint (a vector in the case of a single constraint). Examples of these three ways of constraining parameters are provided below.

Note that when specifying constraints that these should respect the fixed constraints inherent in e.g. the multinomial logit models for the initial and transition probabilities. For example, the baseline category coefficient in a multinomial logit model is fixed on zero.

llratio performs a log-likelihood ratio test on two fit'ted models; the first object should have the largest degrees of freedom (find out by using freepars).

Value

fit returns an object of class depmix. fitted which contains the original depmix object, and further has slots:

message: Convergence information.

conMat: The constraint matrix A, see Details.

posterior: The posterior state sequence (computed with the viterbi algorithm), and the posterior probabilities (delta probabilities in Rabiner, 1989, notation).

The print method shows the message along with the likelihood and AIC and BIC; the summary method prints the parameter estimates.

Posterior densities and the viterbi state sequence can be accessed through posterior.

As fitted models are depmixS4 models, they can be used as starting values for new fits, for example with constraints added. Note that when refitting already fitted models, the constraints, if any, are not added automatically, they have to be added again.

Author(s)

Ingmar Visser & Maarten Speekenbrink

References

Some of the below models for the speed data are reported in:

Ingmar Visser, Maartje E. J. Raijmakers and Han L. J. van der Maas (2009). Hidden Markov Models for Invdividual Time Series. In: Jaan Valsiner, Peter C. M. Molenaar, M. C. D. P. Lyra, and N. Chaudhary (editors). *Dynamic Process Methodology in the Social and Developmental Sciences*, chapter 13, pages 269–289. New York: Springer.

Examples

```
data(speed)
# 2-state model on rt and corr from speed data set
# with Pacc as covariate on the transition matrix
# ntimes is used to specify the lengths of 3 separate time-series
mod1 <- depmix(list(rt~1,corr~1),data=speed,transition=~Pacc,nstates=2,</pre>
family=list(gaussian(),multinomial("identity")),ntimes=c(168,134,137))
# fit the model
set.seed(3)
fmod1 <- fit(mod1)</pre>
fmod1 # to see the logLik and optimization information
# to see the parameters
summary(fmod1)
# to obtain the posterior most likely state sequence, as computed by the
# Viterbi algorithm
pst_global <- posterior(fmod1, type = "global")</pre>
# local decoding provides a different method for state classification:
pst_local <- posterior(fmod1, type="local")</pre>
identical(pst_global, pst_local)
# smoothing probabilities are used for local decoding, and may be used as
# easily interpretable posterior state probabilities
pst_prob <- posterior(fmod1, type = "smoothing")</pre>
# testing viterbi states for new data
df <- data.frame(corr=c(1,0,1),rt=c(6.4,5.5,5.3),Pacc=c(0.6,0.1,0.1))
# define model with new data like above
modNew <- depmix(list(rt~1,corr~1),data=df,transition=~Pacc,nstates=2,</pre>
family=list(gaussian(),multinomial("identity")))
# get parameters from estimated model
modNew <- setpars(modNew,getpars(fmod1))</pre>
# check the state sequence and probabilities
pst_new <- posterior(modNew, type="global")</pre>
# same model, now with missing data
## Not run:
speed[2,1] \leftarrow NA
speed[3,2] \leftarrow NA
```

```
# 2-state model on rt and corr from speed data set
# with Pacc as covariate on the transition matrix
# ntimes is used to specify the lengths of 3 separate series
mod1ms <- depmix(list(rt~1,corr~1),data=speed,transition=~Pacc,nstates=2,</pre>
family=list(gaussian(),multinomial("identity")),ntimes=c(168,134,137))
# fit the model
set.seed(3)
fmod1ms <- fit(mod1ms)</pre>
## End(Not run)
# instead of the normal likelihood, we can also maximise the "classification" likelihood
# this uses the maximum a posteriori state sequence to assign observations to states
# and to compute initial and transition probabilities.
fmod1b <- fit(mod1,emcontrol=em.control(classification="hard"))</pre>
fmod1b # to see the logLik and optimization information
# FIX SOME PARAMETERS
# get the starting values of this model to the optimized
# values of the previously fitted model to speed optimization
pars <- c(unlist(getpars(fmod1)))</pre>
# constrain the initial state probs to be 0 and 1
# also constrain the guessing probs to be 0.5 and 0.5
# (ie the probabilities of corr in state 1)
# change the ones that we want to constrain
pars[1]=0
pars[2]=1 # this means the process will always start in state 2
pars[13]=0.5
pars[14]=0.5 # the corr parameters are now both 0.5
mod2 <- setpars(mod1,pars)</pre>
# fix the parameters by setting:
free <- c(0,0,rep(c(0,1),4),1,1,0,0,1,1,1,1)
# fit the model
fmod2 <- fit(mod2,fixed=!free)</pre>
# likelihood ratio insignificant, hence fmod2 better than fmod1
llratio(fmod1,fmod2)
# ADDING SOME GENERAL LINEAR CONSTRAINTS
# set the starting values of this model to the optimized
# values of the previously fitted model to speed optimization
## Not run:
pars <- c(unlist(getpars(fmod2)))</pre>
```

```
pars[4] <- pars[8] <- -4
pars[6] <- pars[10] <- 10
mod3 <- setpars(mod2,pars)</pre>
# start with fixed and free parameters
conpat <- c(0,0,rep(c(0,1),4),1,1,0,0,1,1,1,1)
# constrain the beta's on the transition parameters to be equal
conpat[4] <- conpat[8] <- 2</pre>
conpat[6] \leftarrow conpat[10] \leftarrow 3
fmod3 <- fit(mod3,equal=conpat)</pre>
llratio(fmod2,fmod3)
# above constraints can also be specified using the conrows argument as follows
conr <- matrix(0,2,18)
# parameters 4 and 8 have to be equal, otherwise stated, their diffence should be zero,
# and similarly for parameters 6 & 10
conr[1,4] <- 1
conr[1,8] <- -1
conr[2,6] <- 1
conr[2,10] <- -1
# note here that we use the fitted model fmod2 as that has appropriate
# starting values
fmod3b <- fit(mod3,conrows=conr,fixed=!free) # using free defined above</pre>
## End(Not run)
data(balance)
# four binary items on the balance scale task
mod4 \leftarrow mix(list(d1~1,d2~1,d3~1,d4~1), data=balance, nstates=2,
family=list(multinomial("identity"), multinomial("identity"),
multinomial("identity"), multinomial("identity")))
set.seed(1)
fmod4 <- fit(mod4)</pre>
## Not run:
# add age as covariate on class membership by using the prior argument
mod5 \leftarrow mix(list(d1~1,d2~1,d3~1,d4~1), data=balance, nstates=2,
family=list(multinomial("identity"), multinomial("identity"),
multinomial("identity"), multinomial("identity")),
prior=~age, initdata=balance)
set.seed(1)
fmod5 <- fit(mod5)</pre>
# check the likelihood ratio; adding age significantly improves the goodness-of-fit
llratio(fmod5,fmod4)
```

formatperc 21

```
## End(Not run)
```

formatperc

Format percentage for level in printing confidence interval

Description

See title.

Usage

```
formatperc(x,digits)
```

Arguments

x a vector of probabilities to be formatted as percentages.

digits the number of required digits in the percentages.

Author(s)

Ingmar Visser

forwardbackward

Forward and backward variables

Description

Compute the forward and backward variables of a depmix object.

Usage

```
## S4 method for signature 'mix'
forwardbackward(object, return.all=TRUE, useC=TRUE, ...)
```

Arguments

object A depmix object.

return.all If FALSE, only gamma and xi and the log likelihood are returned (which are the

only variables needed in using EM).

useC Flag used to set whether the C-code is used to compute the forward, backward,

gamma and xi variables or not; the R-code is basically obsolete (but retained for

now for debugging purposes).

... Not currently used.

22 GLMresponse

Value

forwardbackward returns a list of the following (the variables are named after the notation from Rabiner, 1989):

alpha The forward variables.
beta The backward variables.

gamma The smoothed state probabilities.

xi The smoothed transition probabilities.

sca The scale factors (called lambda in Rabiner, 1989).

logLike The log likelihood (computed as -sum(log(sca)).

If return.all=FALSE, only gamma, xi and the log likelihood are returned.

Author(s)

Maarten Speekenbrink & Ingmar Visser

References

Lawrence R. Rabiner (1989). A tutorial on hidden Markov models and selected applications in speech recognition. *Proceedings of IEEE*, 77-2, p. 267-295.

Examples

```
data(speed)
# 2-state model on rt and corr from speed data set
# with Pacc as covariate on the transition matrix
# ntimes is used to specify the lengths of 3 separate series
mod1 <- depmix(list(rt~1,corr~1),data=speed,transition=~Pacc,nstates=2,family=list(gaussian(),multinomial("identity")),ntimes=c(168,134,137))
fb <- forwardbackward(mod1)
all.equal(-sum(log(fb$sca)),fb$logLike)</pre>
```

GLMresponse

Methods for creating depmix response models

Description

Create GLMresponse objects for depmix models using formulae and family objects.

GLMresponse 23

Usage

```
GLMresponse(formula, data=NULL, family=gaussian(), pstart=NULL,
fixed=NULL, prob=TRUE, ...)
## S4 method for signature 'response'
getdf(object)
```

Arguments

| formula | A model formula. |
|---------|--|
| data | An optional data.frame to interpret the variables from the formula argument in. |
| family | A family object; |
| pstart | Starting values for the coefficients and other parameters, e.g. the standard deviation for the gaussian() family. |
| fixed | Logical vector indicating which paramters are to be fixed. |
| prob | Logical indicating whether the starting values for multinomial() family models are probabilities or logistic parameters (see details). |
| object | Object of class response. |
| | Not used currently. |
| | |

Details

GLMresponse is the default driver for specifying response distributions of depmix models. It uses the familiar formula interface from glm to specify how responses depend on covariates/predictors.

Currently available options for the family argument are binomial, gaussian, poisson, Gamma, and multinomial. Except for the latter option, the GLMresponse model is an interface to the glm functions of which the functionality is used: predict, fit and density functions.

The multinomial model takes as link functions mlogit, the default, and then uses functionality from the nnet package to fit multinomial logistic models; using mlogit as link allows only n=1 models to be specified, i.e. a single observation for each occasion; it also takes identity as a link function. The latter is typically faster and is hence preferred when no covariates are present.

See the responses help page for examples.

Value

GLMresponse returns an object of class GLMresponse which extends the response-class. getdf returns the number of free parameters of a response model.

Author(s)

Ingmar Visser & Maarten Speekenbrink

See Also

makeDepmix has an example of specifying a model with a multivariate normal response and an example of how to add a user-defined response model, in particular an ex-gauss distribution used for the speed data.

24 Ilratio

llratio

Log likelihood ratio test on two fitted models

Description

Performs a log likelihood ratio test on two fitted depmix models.

Usage

```
llratio(basemodel, constrainedmodel, ...)
```

Arguments

```
basemodel Fitted model with a logLik method.

constrainedmodel Fitted model with a logLik method.

... Not currently used.
```

Details

See the fit help page for an example.

Value

llratio returns an object of class llratio which has slots:

value : Minus twice the loglikelihood difference.

df : The degrees of freedom, ie the difference in number of freely estimated paraemters

between the models.

The print method shows the value, the degrees of freedom and the corresponding p-value under the chisquared distribution.

Author(s)

Ingmar Visser

| makeDepmix | Dependent Mixture Model Specifiction: full control and adding response models |
|------------|---|
| | |

Description

makeDepmix creates an object of class depmix. This function is meant for full control, e.g. specifying each response model and the transition and prior models 'by hand'. For the default easier specification of models, please see depmix. This function is meant for specifying one's own response models.

Usage

```
makeDepmix(response, transition, prior, ntimes = NULL, homogeneous = TRUE,
stationary = NULL, ...)
makeMix(response, prior, ...)
```

Arguments

| ě | guments | | |
|---|-------------|--|--|
| | response | A two-dimensional list of response models. See 'Details'. | |
| | transition | A list of transition models, each created by a call to transInit. The length of this list should be the number of states of the model. | |
| | prior | The initial state probabilities model; created through a call to transInit. | |
| | ntimes | A vector specifying the lengths of individual, ie independent, time series. If not specified, the responses are assumed to form a single time series. | |
| | homogeneous | Logical indicating whether the transition models include time-varying covariates; used internally to determine the dimensions of certain arrays, notably trDens. | |
| | stationary | This argument should no longer be used; if not NULL, the value of stationary is copied to the homogeneous argument, with a warning. In future versions this argument may be dropped or used for different purposes, i.e., for specifying models in which the initial state probabilities are constrained to be the stationary distribution of the transition matrix. | |
| | | Not used currently. | |

Details

The function makeDepmix creates an S4 object of class depmix, which needs to be fitted using fit to optimize the parameters. This function is provided to have full control, eg by specifying one's own response models with distributions that are not provided.

The response model(s) should be created by call(s) to GLMresponse, MVNresponse (see example below) or user-defined response models (see example below) that should extend the response-class and have the following methods: dens, predict and optionally fit. The fit function should have an argument w, providing the weights. If the fit function is not provided, optimization should be done

by using Rdonlp (use method="donlp" in calling fit on the depmix model, note that this is *not* the default). The first index of response models runs over the states of the model, and the second index over the responses to be modeled.

Value

See the depmix help page for the return value, a depmix object.

Author(s)

Ingmar Visser & Maarten Speekenbrink

See Also

fit, transInit, GLMresponse, depmix-methods for accessor functions to depmix objects.

Examples

```
# below example recreates the same model as on the fit help page in a roundabout way
# there we had:
# mod1 <- depmix(list(rt~1,corr~1),data=speed,transition=~Pacc,nstates=2,</pre>
# family=list(gaussian(),multinomial("identity")),ntimes=c(168,134,137))
data(speed)
rModels <- list(
GLMresponse(formula=rt~1,data=speed,family=gaussian()),
GLMresponse(formula=corr~1,data=speed,family=multinomial("identity"))
),
list(
GLMresponse(formula=rt~1, data=speed, family=gaussian()),
GLMresponse(formula=corr~1,data=speed,family=multinomial("identity"))
)
transition <- list()</pre>
transition[[1]] <- transInit(~Pacc,nstates=2,data=speed)</pre>
transition[[2]] <- transInit(~Pacc,nstates=2,data=speed)</pre>
inMod <- transInit(~1,ns=2,data=data.frame(rep(1,3)),family=multinomial("identity"))</pre>
mod <- makeDepmix(response=rModels,transition=transition,prior=inMod,</pre>
ntimes=c(168,134,137),homogeneous=FALSE)
set.seed(3)
fm1 <- fit(mod)
summary(fm1)
# generate data from two different multivariate normal distributions
m1 < -c(0,1)
```

```
sd1 \leftarrow matrix(c(1,0.7,.7,1),2,2)
m2 < -c(1,0)
sd2 \leftarrow matrix(c(2,.1,.1,1),2,2)
set.seed(2)
y1 <- mvrnorm(50,m1,sd1)
y2 <- mvrnorm(50, m2, sd2)
# this creates data with a single change point
y <- rbind(y1,y2)</pre>
# now use makeDepmix to create a depmix model for this bivariate normal timeseries
rModels <- list()
rModels[[1]] <- list(MVNresponse(y~1))</pre>
rModels[[2]] <- list(MVNresponse(y~1))
trstart=c(0.9,0.1,0.1,0.9)
transition <- list()</pre>
transition[[1]] <- transInit(~1,nstates=2,data=data.frame(1),pstart=c(trstart[1:2]))</pre>
transition[[2]] <- transInit(~1,nstates=2,data=data.frame(1),pstart=c(trstart[3:4]))</pre>
instart=runif(2)
inMod <- transInit(~1,ns=2,ps=instart,data=data.frame(1))</pre>
mod <- makeDepmix(response=rModels,transition=transition,prior=inMod)</pre>
fm2 <- fit(mod,emc=em.control(random=FALSE))</pre>
# where is the switch point?
plot(as.ts(posterior(fm2, type="smoothing")[,1]))
# in below example we add the exgaus distribution as a response model and fit
# this instead of the gaussian distribution to the rt slot of the speed data
# most of the actual computations for the exgaus distribution is done by calling
# functions from the gamlss family of packages; see their help pages for
# interpretation of the mu, nu and sigma parameters that are fitted below
## Not run:
require(gamlss)
require(gamlss.dist)
data(speed)
rt <- speed$rt
# define a response class which only contains the standard slots, no additional slots
setClass("exgaus", contains="response")
# define a generic for the method defining the response class
setGeneric("exgaus", function(y, pstart = NULL, fixed = NULL, ...) standardGeneric("exgaus"))
# define the method that creates the response class
```

```
setMethod("exgaus",
    signature(y="ANY"),
    function(y,pstart=NULL,fixed=NULL, ...) {
        y <- matrix(y,length(y))</pre>
x <- matrix(1)</pre>
parameters <- list()</pre>
npar <- 3
if(is.null(fixed)) fixed <- as.logical(rep(0,npar))</pre>
if(!is.null(pstart)) {
if(length(pstart)!=npar) stop("length of 'pstart' must be ",npar)
 parameters$mu <- pstart[1]</pre>
 parameters$sigma <- log(pstart[2])</pre>
 parameters$nu <- log(pstart[3])</pre>
        }
        mod <- new("exgaus",parameters=parameters,fixed=fixed,x=x,y=y,npar=npar)</pre>
        mod
}
)
setMethod("show", "exgaus",
    function(object) {
        cat("Model of type exgaus (see ?gamlss for details) \n")
        cat("Parameters: \n")
        cat("mu: ", object@parameters$mu, "\n")
        cat("sigma: ", object@parameters$sigma, "\n")
        cat("nu: ", object@parameters$nu, "\n")
   }
)
setMethod("dens","exgaus",
function(object,log=FALSE) {
   dexGAUS(object@y, mu = predict(object),
sigma = exp(object@parameters$sigma), nu = exp(object@parameters$nu), log = log)
 }
)
setMethod("getpars","response",
    function(object,which="pars",...) {
        switch(which,
            "pars" = {
                 parameters <- numeric()</pre>
                 parameters <- unlist(object@parameters)</pre>
                 pars <- parameters</pre>
            },
            "fixed" = {
                 pars <- object@fixed
        )
        return(pars)
    }
)
setMethod("setpars", "exgaus",
```

```
function(object, values, which="pars", ...) {
        npar <- npar(object)</pre>
        if(length(values)!=npar) stop("length of 'values' must be",npar)
        # determine whether parameters or fixed constraints are being set
nms <- names(object@parameters)</pre>
switch(which,
  "pars"= {
      object@parameters$mu <- values[1]</pre>
      object@parameters$sigma <- values[2]</pre>
      object@parameters$nu <- values[3]</pre>
      },
  "fixed" = {
      object@fixed <- as.logical(values)</pre>
  }
  )
        names(object@parameters) <- nms</pre>
        return(object)
    }
)
setMethod("fit","exgaus",
    function(object,w) {
        if(missing(w)) w <- NULL</pre>
        y <- object@y
        fit <- gamlss(y~1,weights=w,family=exGAUS(),</pre>
control=gamlss.control(n.cyc=100,trace=FALSE),
mu.start=object@parameters$mu,
sigma.start=exp(object@parameters$sigma),
nu.start=exp(object@parameters$nu))
pars <- c(fit$mu.coefficients,fit$sigma.coefficients,fit$nu.coefficients)</pre>
object <- setpars(object,pars)</pre>
object
}
)
setMethod("predict","exgaus",
    function(object) {
        ret <- object@parameters$mu
        return(ret)
    }
)
rModels <- list(
  list(
  exgaus(rt,pstart=c(5,.1,.1)),
GLMresponse(formula=corr~1, data=speed,
family=multinomial("identity"), pstart=c(0.5,0.5))
),
list(
exgaus(rt,pstart=c(6,.1,.1)),
GLMresponse(formula=corr~1, data=speed,
family=multinomial("identity"), pstart=c(.1,.9))
)
```

30 mix

```
trstart=c(0.9,0.1,0.1,0.9)
transition <- list()
transition[[1]] <- transInit(~Pacc,nstates=2,data=speed,pstart=c(trstart[1:2],0,0))
transition[[2]] <- transInit(~Pacc,nstates=2,data=speed,pstart=c(trstart[3:4],0,0))
instart=c(0.5,0.5)
inMod <- transInit(~1,ns=2,ps=instart,family=multinomial("identity"), data=data.frame(rep(1,3)))
mod <- makeDepmix(response=rModels,transition=transition,prior=inMod,ntimes=c(168,134,137),
homogeneous=FALSE)
fm3 <- fit(mod,emc=em.control(rand=FALSE))
summary(fm3)
## End(Not run)</pre>
```

mix

Mixture Model Specifiction

Description

mix creates an object of class mix, an (independent) mixture model (as a limit case of dependent mixture models in which all observed time series are of length 1), otherwise known latent class or mixture model. For a short description of the package see depmixS4.

Usage

```
mix(response, data=NULL, nstates, family=gaussian(),
prior=~1, initdata=NULL, respstart=NULL, instart=NULL,...)
```

Arguments

| response | The response to be modeled; either a formula or a list of formulae in the multivariate case; this interfaces to the glm distributions. See 'Details'. |
|----------|--|
| data | An optional data.frame to interpret the variables in the response and transition arguments. |
| nstates | The number of states of the model. |
| family | A family argument for the response. This must be a list of family's if the response is multivariate. |
| prior | A one-sided formula specifying the density for the prior or initial state probabilities. |
| initdata | An optional data.frame to interpret the variables occurring in prior. The number of rows of this data.frame must be equal to the number of cases being modeled. See 'Details'. |

mix 31

respstart Starting values for the parameters of the response models.

instart Starting values for the parameters of the prior or initial state probability model.

... Not used currently.

Details

The function mix creates an S4 object of class mix, which needs to be fitted using fit to optimize the parameters.

The response model(s) are by default created by call(s) to GLMresponse using the formula and the family arguments, the latter specifying the error distribution. See GLMresponse for possible values of the family argument for glm-type responses (ie a subset of the glm family options, and the multinomial). Alternative response distributions are specified by using the makeDepmix function. Its help page has examples of specifying a model with a multivariate normal response, as well as an example of adding a user-defined response model, in this case for the ex-gauss distribution.

If response is a list of formulae, the response's are assumed to be independent conditional on the latent state.

The prior density is modeled as a multinomial logistic. This model is created by a call to transInit.

Starting values may be provided by the respective arguments. The order in which parameters must be provided can be easily studied by using the setpars and getpars functions.

Linear constraints on parameters can be provided as argument to the fit function.

The print function prints the formulae for the response and prior models along with their parameter values.

Value

mix returns an object of class mix which has the following slots:

response A list of a list of response models; the first index runs over states; the second

index runs over the independent responses in case a multivariate response is

provided.

prior A multinomial logistic model for the initial state probabilities.

dens, init See mix-class help for details. For internal use.

ntimes A vector made by rep(1,nrow(data)); for internal use only.

nstates The number of states of the model.

nresp The number of independent responses.

npars The total number of parameters of the model. Note: this is *not* the degrees of

freedom because there are redundancies in the parameters, in particular in the

multinomial models for the transitions and prior probabilities.

Author(s)

Ingmar Visser & Maarten Speekenbrink

References

A. L. McCutcheon (1987). Latent class analysis. Sage Publications.

32 mix-class

See Also

fit, transInit, GLMresponse, depmix-methods for accessor functions to depmix objects.

Examples

```
# four binary items on the balance scale task
data(balance)

# define a latent class model
instart=c(0.5,0.5)
set.seed(1)
respstart=runif(16)
# note that ntimes argument is used to make this a mixture model
mod <- mix(list(d1~1,d2~1,d3~1,d4~1), data=balance, nstates=2,
family=list(multinomial(),multinomial(),multinomial()),
respstart=respstart,instart=instart)
# to see the model
mod</pre>
```

mix-class

Class "mix"

Description

A mix model.

Objects from the Class

Objects can be created by calls to mix.

Slots

response: List of list of response objects.

prior: transInit object; model for the prior probabilities, also unconditional probabilities

dens: Array of dimension sum(ntimes)*nresp*nstates providing the densities of the observed responses for each state.

init: Array of dimension length(ntimes)*nstates with the current predictions for the initial state probabilities.

nstates: The number of states (classes) of the model.

nresp: The number of independent responses.

ntimes: A vector of 1's for each case; for internal use.

npars: The total number of parameters of the model. This is not the degrees of freedom, ie there are redundancies in the parameters, in particular in the multinomial models for the transitions and prior.

mix.fitted-class 33

Accessor Functions

The following functions should be used for accessing the corresponding slots:

npar: The number of parameters of the model.

nresp: The number of responses. nstates: The number of states.

ntimes: The vector of independent time series lengths.

Author(s)

Ingmar Visser & Maarten Speekenbrink

Examples

showClass("mix")

mix.fitted-class

Class "mix.fitted" (and "mix.fitted.classLik")

Description

A fitted mix model.

Slots

A mix. fitted object is a mix object with three additional slots, here is the complete list:

response: List of list of response objects.

prior: transInit object.

dens: Array of dimension sum(ntimes)*nresp*nstates providing the densities of the observed responses for each state.

init: Array of dimension length(ntimes)*nstates with the current predictions for the initial state probabilities.

ntimes: A vector containing the lengths of independent time series; if data is provided, sum(ntimes) must be equal to nrow(data).

nstates: The number of states of the model.

nresp: The number of independent responses.

npars: The total number of parameters of the model. This is not the degrees of freedom, ie there are redundancies in the parameters, in particular in the multinomial models for the transitions and prior.

message: This provides some information on convergence, either from the EM algorithm or from Rdonlp2.

conMat: The linear constraint matrix, which has zero rows if there were no constraints.

lin.lower The lower bounds on the linear constraints.

lin.upper The upper bounds on the linear constraints.

posterior: Posterior (Viterbi) state sequence.

34 mix.sim-class

Details

The print function shows some convergence information, and the summary method shows the parameter estimates.

Extends

Class "mix" directly. mix.fitted.classLik is similar to mix.fitted, the only difference being that the model is fitted by maximising the classification likelihood.

Author(s)

Ingmar Visser & Maarten Speekenbrink

Examples

```
showClass("mix.fitted")
```

mix.sim-class

Class "mix.sim"

Description

A mix.sim model. The mix.sim class directly extends the mix class, and has an additional slot for the true states. A mix.sim model can be generated by simulate(mod,...), where mod is a mix model.

Slots

response: List of list of response objects.

prior: transInit object.

dens: Array of dimension sum(ntimes)*nresp*nstates providing the densities of the observed responses for each state.

init: Array of dimension length(ntimes)*nstates with the current predictions for the initial state probabilities.

ntimes: A vector containing the lengths of independent time series; not applicable for mix objects, i.e. this is a vector of 1's.

nstates: The number of states/classes of the model.

nresp: The number of independent responses.

npars: The total number of parameters of the model. This is not the degrees of freedom, ie there are redundancies in the parameters, in particular in the multinomial models for the transitions and prior.

states: A matrix with the true states/classes.

multistart 35

Accessor Functions

The following functions should be used for accessing the corresponding slots:

npar: The number of parameters of the model.

nresp: The number of responses.nstates: The number of states.

ntimes: The vector of independent time series lengths.

Author(s)

Maarten Speekenbrink & Ingmar Visser

multistart

Methods to fit a (dep-)mix model using multiple sets of starting values

Description

Fit a model using multiple sets of starting values.

Usage

```
## S4 method for signature 'mix'
multistart(object, nstart=10, initIters=10, ...)
```

Arguments

object An object of class mix or depmix.

nstart The number of sets of starting values that are used.

initIters The number of EM iterations that each set of starting values is run.

... Not used currently.

Details

Starting values in the EM algorithm are generated by randomly assigning posterior state probabilities for each observation using a Dirichlet distribution. This is done nstart times. The EM algorithm is run initIters times for each set of starting values. The then best fitting model is then optimized until convergence. A warning is provided about the number of sets of starting values that are infeasible, e.g. due to non-finite log likelihood, if that number is larger than zero. Note that the number of iterations reported in the final fitted model does not include the initial number of iterations that EM was run for.

Value

A fitted (dep)mix object.

36 posterior

Author(s)

Ingmar Visser & Maarten Speekenbrink

Examples

```
data(speed)
# this example is from ?fit with fit now replaced by multistart and the
# set.seed statement is left out
mod1 <- depmix(list(rt~1,corr~1),data=speed,transition=~Pacc,nstates=2,
family=list(gaussian(),multinomial("identity")),ntimes=c(168,134,137))
set.seed(3)
fmod1 <- fit(mod1)
fmod2 <- multistart(mod1)
fmod1
fmod2</pre>
```

posterior

Posterior state/class probabilities and classification

Description

Return posterior state classifications and/or probabilities for a fitted (dep-)mix object. In the case of a latent class or mixture model, states refer to the classes/mixture components.

There are different ways to define posterior state probabilities and the resulting classifications. The 'type' argument can be used to specify the desired definition. The default is currently set to 'viterbi'. Other options are 'global' and 'local' for state classification, and 'filtering' and 'smoothing' for state probabilities. See Details for more information.

Usage

```
## S4 method for signature 'depmix'
posterior(object, type = c("viterbi", "global", "local", "filtering", "smoothing"))
## S4 method for signature 'depmix.fitted'
posterior(object, type = c("viterbi", "global", "local", "filtering", "smoothing"))
## S4 method for signature 'mix'
posterior(object, type = c("viterbi", "global", "local", "filtering", "smoothing"))
## S4 method for signature 'mix.fitted'
posterior(object, type = c("viterbi", "global", "local", "filtering", "smoothing"))
```

Arguments

object A (fitted)(dep-)mix object.

type character, partial matching allowed. The type of classification or posterior prob-

ability desired.

posterior 37

Details

After fitting a mix or depmix model, one is often interested in determining the most probable mixture components or hidden states at each time-point t. This is also called decoding the hidden states from the observed data. There are at least two general ways to consider state classification: 'global' decoding means determining the most likely state sequence, whilst 'local' decoding means determining the most likely state at each time point whilst not explicitly considering the identity of the hidden states at other time points. For mixture models, both forms of decoding are identical.

Global decoding is based on the conditional probability $p(S_1, ..., S_T \mid Y_1, ..., Y_T)$, and consists of determining, at each time point t = 1, ..., T:

$$s*_t = \arg \max_{i=1}^N p(S_1 = s*_1, \dots, S_{t-1} = s*_{t-1}, S_t = i, S_{t+1} = s*_{t+1}, \dots, S_T = s*_T \mid Y_1, \dots, Y_T)$$

where N is the total number of states. These probabilities and the resulting classifications, are computed through the viterbi algorithm. Setting type = 'viterbi' returns a data.frame with the Viterbi-decoded global state sequence in the first column, and the normalized "delta" probabilities in the remainining columns. These "delta" probabilities are defined as the joint probability of the most likely state sequence ending in state i at time t, and all the observations up to time t. The normalization of these joint probabilities is done on a time-point basis (i.e., dividing the delta probability by the sum of the delta probabilities for that time point for all possible states j (including state i)). These probabilities are not straightforward to interpret. Setting type = "global" returns just a vector with the Viterbi-decoded global state sequence.

Local decoding is based on the smoothing probabilities $p(S_t \mid Y_1, \dots, Y_T)$, which are the "gamma" probabilities computed with the forwardbackward algorithm. Local decoding then consists of determining, at each time point $t = 1, \dots, T$

$$s*_t = \arg\max_{i=1}^N p(S_t = i \mid Y_1, \dots, Y_T)$$

where N is the total number of states. Setting type = "local" returns a vector with the local decoded states. Setting type = "smoothing" returns the smoothing probabilities which underlie this classification. When considering the posterior probability of each state, the values returned by type = "smoothing" are most likely what is wanted by the user.

The option type = "filtering" returns a matrix with the so-called filtering probabilities, defined as $p(S_t \mid Y_1, \ldots, Y_t)$, i.e. the probability of a hidden state at time t considering the observations up to and including time t.

See the fit help page for an example.

Value

The return value of posterior depends on the value of the type argument:

type = 'viterbi'

Returns a data.frame with nstates(object) + 1 columns; the first column contains the states decoded through the Viterbi algorithm, the remaining columns contain the (normalized) delta probabilities.

type = 'global' Returns a vector which contains the states decoded through the Viterbi algorithm.

38 posterior

```
type = 'local' Returns a vector which contains the states decoded as the maximum of the smoothing probabilities.
```

```
type = 'filtering'
```

Returns a matrix which contains the posterior probabilities of each state, conditional upon the responses observed thus far.

```
type = 'smoothing'
```

Returns a matrix which contains the posterior probabilities of each state, conditional upon all the responses observed.

See Details for more information.

Note

The initial version of this function was a simple wrapper to return the value of the posterior slot in a mix-fitted or depmix-fitted object. The value of this slot is set by a call of the viterbi method. For backwards compatibility, the default value of the type argument is set to "viterbi", which returns the same. As the "delta" probabilities returned as part of this may be misinterpreted, and may not be the desired posterior probabilities, the updated version of this method now allows for other return values, and the type = "viterbi" option should be considered depreciated.

Author(s)

Maarten Speekenbrink & Ingmar Visser

References

Lawrence R. Rabiner (1989). A tutorial on hidden Markov models and selected applications in speech recognition. *Proceedings of IEEE*, 77-2, p. 267-295.

Examples

```
data(speed)
# 2-state model on rt and corr from speed data set
# with Pacc as covariate on the transition matrix
# ntimes is used to specify the lengths of 3 separate series
mod <- depmix(list(rt~1,corr~1),data=speed,transition=~Pacc,nstates=2,
family=list(gaussian(),multinomial("identity")),ntimes=c(168,134,137))
fmod <- fit(mod)

# Global decoding:
pst_global <- posterior(fmod, type = "global")

# Local decoding:
pst_local <- posterior(fmod,type="local")

# Global and local decoding provide different results:
identical(pst_global, pst_local)

# smoothing probabilities are used for local decoding, and may be used as
# easily interpretable posterior state probabilities</pre>
```

response-class 39

```
pst_prob <- posterior(fmod, type = "smoothing")

# "delta" probabilities from the Viterbi algorithm
pst_delta <- posterior(fmod, type="viterbi")[,-1]

# The smoothing and "delta" probabilities are different:
identical(pst_prob, pst_delta)

# Filtering probabilities are an alternative to smoothing probabilities:
pst_filt <- posterior(fmod, type = "filtering")

# The smoothing and filtering probabilities are different:
identical(pst_prob, pst_filt)</pre>
```

response-class

Class "response"

Description

A generic response model for depmix models.

Arguments

object

An object of class "response".

Details

This class offers a framework from which to build specific response models such as glm based responses or multinomial responses. For extensibility, objects with class response should have at least methods: dens to return the dens'ity of responses, and getpars and setpars methods to get and set parameters.

The constr slot is used for information on constraints that are inherently part of a model; the only such constraints which are currently used are 1) the sum constraint in multinomial models with identity link, and 2) a lower bound of zero of sd parameters in gaussian distributions. Such constraints are only used in fitting models with general optimization routines such as Rsolnp; the EM algorithm automagically respects the sum constraint.

lin: Derivative of linear constraint.

linup: Upper bounds for linear constraints.

linlow: Lower bounds for linear constraints.

parup: Upper bounds on parameters.
parlow: Lower bounds on parameters.

40 response-classes

Slots

parameters: A (named) list of parameters.

fixed: A logical vector indicating which parameters are fixed.

y: A matrix with the actual response; possibly multivariate.

x: A design matrix; possibly only an intercept term.

npar: The number of parameters.

constr: Information on constraints.

Accessor Functions

The following functions should be used for accessing the corresponding slots:

npar: The number of parameters of the model.

getdf: The number of non-fixed parameters.

Author(s)

Ingmar Visser & Maarten Speekenbrink

response-classes

Class "GLMresponse" and class "transInit"

Description

Specific instances of response models for depmix models.

Details

The GLMresponse-class offers an interface to the glm functions that are subsequently used in fitting the depmix model of which the response is a part.

The transInit is an extension of response that is used to model the transition matrix and the initial state probabilities by the use of a multinomial logistic model, the difference being that in fact the response is missing as the transitions between states are not observed. This class has its own fit function which is an interface to the multinom function in nnet.

Slots

Both GLMresponse and transInit contain the response-class. In addition to the slots of that class, these classes have the following slots:

formula: A formula that specifies the model.

family: A family object specifying the link function. See the GLMresponse help page for possible options.

responses 41

Accessor Functions

The following functions should be used for accessing the corresponding slots:

npar: The number of parameters of the model.

getdf: The number of non-fixed parameters.

Author(s)

Ingmar Visser & Maarten Speekenbrink

responses

Response models currently implemented in depmix.

Description

Depmix contains a number of default response models. We provide a brief description of these here.

BINOMresponse

BINOMresponse is a binomial response model. It derives from the basic GLMresponse class.

- y: The dependent variable can be either a binary vector, a factor, or a 2-column matrix, with successes and misses.
- **x:** The design matrix.

Parameters: A named list with a single element "coefficients", which contains the GLM coefficients.

GAMMAresponse

GAMMAresponse is a model for a Gamma distributed response. It extends the basic GLMresponse class directly.

- y: The dependent variable.
- x: The design matrix.

Parameters: A named list with a single element "coefficients", which contains the GLM coefficients.

MULTINOMresponse

MULTINOMresponse is a model for a multinomial distributed response. It extends the basic GLMresponse class, although the functionality is somewhat different from other models that do so.

- **y:** The dependent variable. This is a binary matrix with N rows and Y columns, where Y is the total number of categories.
- **x:** The design matrix.

Parameters: A named list with a single element "coefficients", which is an ncol(x) by ncol(y) matrix which contains the GLM coefficients.

42 responses

MVNresponse

MVNresponse is a model for a multivariate normal distributed response. See makeDepmix for an example of how to use this and other non-glm like distributions.

- **y:** The dependent variable. This is a matrix.
- **x:** The design matrix.

Parameters: A named list with a elements "coefficients", which contains the GLM coefficients, and "Sigma", which contains the covariance matrix.

NORMresponse

NORMresponse is a model for a normal (Gaussian) distributed response. It extends the basic GLMresponse class directly.

- y: The dependent variable.
- **x:** The design matrix.

Parameters: A named list with elements "coefficients", which contains the GLM coefficients, and "sd", which contains the standard deviation.

POISSONresponse

POISSONresponse is a model for a Poisson distributed response. It extends the basic GLMresponse class directly.

- y: The dependent variable.
- x: The design matrix.

Parameters: A named list with a single element "coefficients", which contains the GLM coefficients.

Author(s)

Maarten Speekenbrink & Ingmar Visser

Examples

```
# binomial response model
x <- rnorm(1000)
p <- plogis(x)
ss <- rbinom(1000,1,p)
mod <- GLMresponse(cbind(ss,1-ss)~x,family=binomial())
fit(mod)
glm(cbind(ss,1-ss)~x, family=binomial)

# gamma response model
x=runif(1000,1,5)
res <- rgamma(1000,x)
## note that gamma needs proper starting values which are not
## provided by depmixS4 (even with them, this may produce warnings)
mod <- GLMresponse(res~x,family=Gamma(),pst=c(0.8,1/0.8))</pre>
```

responses 43

```
fit(mod)
glm(res~x,family=Gamma)
# multinomial response model
x <- sample(0:1,1000,rep=TRUE)</pre>
mod <- GLMresponse(sample(1:3,1000,rep=TRUE)~x,family=multinomial(),pstart=c(0.33,0.33,0.33,0,0,1))</pre>
mod@y <- simulate(mod)</pre>
fit(mod)
colSums(mod@y[which(x==0),])/length(which(x==0))
colSums(mod@y[which(x==1),])/length(which(x==1))
# note that the response is treated as factor here, internal representation is in
# dummy coded format:
head(mod@y)
# similar to the binomial model, data may also be entered in multi-column format
# where the n for each row can be different
dt \leftarrow data.frame(y1=c(0,1,1,2,4,5),y2=c(1,0,1,0,1,0),y3=c(4,4,3,2,1,1))
m2 \leftarrow mix(cbind(y1,y2,y3)^1,data=dt,ns=2,family=multinomial("identity"))
fm2 <- fit(m2)
summary(fm2)
# multivariate normal response model
mn < -c(1,2,3)
sig \leftarrow matrix(c(1,.5,0,.5,1,0,0,0,2),3,3)
y <- mvrnorm(1000,mn,sig)
mod <- MVNresponse(y~1)</pre>
fit(mod)
colMeans(y)
var(y)
# normal (gaussian) response model
y <- rnorm(1000)
mod <- GLMresponse(y~1)</pre>
fm <- fit(mod)</pre>
cat("Test gaussian fit: ", all.equal(getpars(fm),c(mean(y),sd(y)),check.attributes=FALSE))
# poisson response model
x <- abs(rnorm(1000,2))
res <- rpois(1000,x)
mod <- GLMresponse(res~x,family=poisson())</pre>
glm(res~x, family=poisson)
# this creates data with a single change point with Poisson distributed data
set.seed(3)
y1 <- rpois(50,1)
y2 <- rpois(50,2)
ydf <- data.frame(y=c(y1,y2))</pre>
# fit models with 1 to 3 states
m1 \leftarrow depmix(y^1, ns=1, family=poisson(), data=ydf)
fm1 <- fit(m1)
m2 \leftarrow depmix(y^1, ns=2, family=poisson(), data=ydf)
fm2 <- fit(m2)
```

44 simulate

```
m3 <- depmix(y~1,ns=3,family=poisson(),data=ydf)
fm3 <- fit(m3,em=em.control(maxit=500))

# plot the BICs to select the proper model
plot(1:3,c(BIC(fm1),BIC(fm2),BIC(fm3)),ty="b")</pre>
```

simulate

Methods to simulate from (dep-)mix models

Description

Random draws from (dep-)mix objects.

Usage

```
## S4 method for signature 'depmix'
simulate(object, nsim=1, seed=NULL, ...)

## S4 method for signature 'mix'
simulate(object, nsim=1, seed=NULL, ...)

## S4 method for signature 'response'
simulate(object, nsim=1, seed=NULL, times, ...)

## S4 method for signature 'GLMresponse'
simulate(object, nsim=1, seed=NULL, times, ...)

## S4 method for signature 'transInit'
simulate(object, nsim=1, seed=NULL, times, is.prior=FALSE, ...)
```

Arguments

| object | Object to generate random draws. An object of class mix, depmix, response or transInit |
|----------|--|
| nsim | The number of draws (one draw simulates a data set of the size that is defined by ntimes); defaults to 1. |
| seed | Set the seed. |
| times | (optional) An indicator vector indicating for which times in the complete series to generate the data. For internal use. |
| is.prior | For transInit objects, indicates whether it is a prior (init) model, or not (i.e., it is a transition model) |
| | Not used currently. |

sp500 45

Details

For a depmix model, simulate generates nsim random state sequences, each of the same length as the observation sequence in the depmix model (i.e., sum(ntimes(object)). The state sequences are then used to generate nsim observation sequences of thee same length.

For a mix model, simulate generates nsim random class assignments for each case. Those assigments are then used to generate observation/response values from the appropriate distributions.

Setting the times option selects the time points in the total state/observation sequence (i.e., counting is continued over ntimes). Direct calls of simulate with the times option are not recommended.

Value

For a depmix object, a new object of class depmix.sim.

For a transInit object, a state sequence.

For a response object, an observation sequence.

Author(s)

Maarten Speekenbrink & Ingmar Visser

Examples

```
y <- rnorm(1000)
respst <- c(0,1,2,1)
trst <- c(0.9,0.1,0.1,0.9)

df <- data.frame(y=y)

mod <- depmix(y~1,data=df,respst=respst,trst=trst,inst=c(0.5,0.5),nti=1000,nst=2)

mod <- simulate(mod)</pre>
```

sp500

Standard & Poor's 500 index

Description

This data set consists of (monthly) values of the S&P 500 stock exchange index. The variable of interest is the logarithm of the return values, i.e., the logarithm of the ratio of indices, in this case the closing index is used.

Usage

```
data(speed)
```

speed speed

Format

```
A data frame with 744 observations and 6 variables.

Open Index at the start of trading.

High Highest index.

Low Lowest index.

Close Index at the close of trading.

Volume The volume of trading.

logret The log return of the closing index.
```

Source

Yahoo Data.

Examples

```
data(sp500)
# the data can be made with the following code (eg to include a longer or
# shorter time span)
## Not run:
require(TTR)
# load SP500 returns
Sys.setenv(tz='UTC')

sp500 <- getYahooData('^GSPC',start=19500101,end=20120228,freq='daily')
ep <- endpoints(sp500, on="months", k=1)
sp500 <- sp500[ep[2:(length(ep)-1)]]
sp500$sp500_ret <- log(sp500$Close) - lag(log(sp500$Close))
sp500 <- na.exclude(sp500)
## End(Not run)</pre>
```

speed

Speed Accuracy Switching Data

Description

This data set is a bivariate series of response times and accuracy scores of a single participant switching between slow/accurate responding and fast guessing on a lexical decision task. The slow and accurate responding, and the fast guessing can be modelled using two states, with a switching regime between them. The dataset further contains a third variable called Pacc, representing the

stationary 47

relative pay-off for accurate responding, which is on a scale of zero to one. The value of Pacc was varied during the experiment to induce the switching. This data set is a from participant A in experiment 1a from Dutilh et al (2011).

Usage

```
data(speed)
```

Format

A data frame with 439 observations on the following 4 variables.

```
rt a numeric vector of response times (log ms)
corr a numeric vector of accuracy scores (0/1)
Pacc a numeric vector of the pay-off for accuracy
prev a numeric vector of accuracy scores (0/1) on the previous trial
```

Source

Gilles Dutilh, Eric-Jan Wagenmakers, Ingmar Visser, & Han L. J. van der Maas (2011). A phase transition model for the speed-accuracy trade-off in response time experiments. *Cognitive Science*, 35:211-250.

Corresponding author: g.dutilh@uva.nl

Examples

```
data(speed)
## maybe str(speed) ; plot(speed) ...
```

stationary

Compute the stationary distribution of a transition probability matrix.

Description

See title.

Usage

```
stationary(tpm)
```

Arguments

tpm

a transition probability matrix.

Value

A vector with the stationary distribution such that p=tpm*p.

48 transInit

Author(s)

Ingmar Visser

transInit

Methods for creating depmix transition and initial probability models

Description

Create transInit objects for depmix models using formulae and family objects.

Usage

```
transInit(formula, nstates, data=NULL, family=multinomial(),
pstart=NULL, fixed=NULL, prob=TRUE, ...)
## S4 method for signature 'transInit'
getdf(object)
```

Arguments

| formula | A model formula. |
|---------|--|
| data | An optional data.frame to interpret the variables from the formula argument in. |
| family | A family object; see details. |
| pstart | Starting values for the coefficients. |
| fixed | Logical vector indicating which paramters are to be fixed. |
| prob | Logical indicating whether the starting values for multinomial() family models are probabilities or logistic parameters (see details). |
| nstates | The number of states of the model. |
| object | An object of class transInit. |
| | Not used currently. |

Details

The transInit model provides functionality for the multinomial probabilities of the transitions between states, as well as for the prior or initial probabilities. These probabilities may depend on (time-varying) covariates. The model can be used with link functions mlogit and identity; the latter is the default when no covariates are. With the mlogit link function, the transition probabilities are modeled as baseline logistic multinomials (see Agresti, 2002, p. 272 ff.).

Start values for the parameters may be provided using the pstart argument; these can be provided as probabilities, the default option, or as baseline logistic parameters, use the prob argument to specify the chosen option. The default baseline category is set to 1, which can be modified through calling, say, family=multinomial(base=2).

Note that the transInit model extends the response-class, but that it actually lacks a reponse, i.e. the y-slot is empty, at the time of construction, as the transitions are not observed.

getdf returns the number of free parameters of a transInit model.

vcov 49

Value

transInit return objects of class transInit; this class extends the response-class.

Author(s)

Ingmar Visser & Maarten Speekenbrink

References

Agresti, A. (2002). *Categorical Data Analysis*. Wiley series in probability and mathematical statistics. Wiley-Interscience, Hoboken, NJ, 2 edition.

vcov

Parameter standard errors

Description

These functions provide standard errors for parameters of (dep-)mix models.

Usage

```
## S4 method for signature 'mix'
vcov(object, fixed=NULL, equal=NULL,
conrows=NULL, conrows.upper=NULL, conrows.lower=NULL, tolerance=1e-6,
method="finiteDifferences", ...)

## S4 method for signature 'mix'
standardError(object, fixed=NULL, equal=NULL,
conrows=NULL, conrows.upper=NULL, conrows.lower=NULL, tolerance=1e-6,
method="finiteDifferences", ...)

## S4 method for signature 'mix'
confint(object, level=0.95, fixed=NULL, equal=NULL,
conrows=NULL, conrows.upper=NULL, conrows.lower=NULL, tolerance=1e-6,
method="finiteDifferences", ...)

## S4 method for signature 'mix'
hessian(object, tolerance=1e-6,
method="finiteDifferences", ...)
```

Arguments

object A (dep-)mix object; see depmix for details.

fixed, equal These arguments are used to specify constraints on a model; see usage details

here: fit.

conrows These arguments are used to specify constraints on a model; see usage details

here: fit.

50 vcov

conrows.upper These arguments are used to specify constraints on a model; see usage details

here: fit.

conrows.lower These arguments are used to specify constraints on a model; see usage details

here: fit.

tolerance Threshold used for testing whether parameters are estimated on the boundary of

the parameter space; if so, they are ignored in these functions.

method The method used for computing the Hessian matrix of the parameters; currently

only a finite differences method (using fdHess from package nlme) is imple-

mented and hence used by default.

level The desired significance level for the confidence intervals.

... Further arguments passed to other methods; currently not in use.

Details

vcov computes the variance-covariance matrix of a (dep-)mix object, either fitted or not. It does so by first constructing a Hessian matrix through the use of hessian and then transforming this as described in Visser et al (2000), taking into account the linear constraints that are part of the model. Currently, hessian has a single method using finite differences to arrive at an approximation of the second order derivative matrix of the parameters.

confint and standardError use vcov to compute confidence intervals (the confidence level can be set through an argument) and standard errors respectively. The latter are computed first by using sqrt(diag(vcov)) and the confidence intervals are computed through the normal approximation.

If and when these methods are applied to fit'ted models, the linear constraint matrix is obtained from the mix.fitted or depmix.fitted slot lincon (supplemented with additional constraints if those are provided through the equal and other arguments to these functions).

All four functions exclude parameters that are estimated on or near (this can be controlled using the tolerance argument) their boundary values. Setting this argument to zero can result in error as the fdHess function requires an environment around the parameter estimate that provides proper log-likelihood values, which parameter on or over their boundary values are not guaranteed to provided. Fixed parameters are similarly ignored in these four functions.

Value

vcov returns a named list with elements vcov, elements, and lincon. standardError returns a data.frame with columns par, elements, and se. confint returns a data.frame with columns par, elements, and two columns for the lower and upper bounds of the confidence intervals (with the column names indicating the level of the interval.)

vcov : The variance-covariance matrix of the parameters.

elements : Vector of length npar(object) indicating which elements of the parameter

vector are included in computing the hessian, the variance-covariance matrix,

the standard errors and/or the confidence intervals.

inc : 'inc'luded parameter.
fix : 'fix'ed parameter.

bnd : parameter estimated on the boundary.

viterbi 51

par : The values of the parameters.

se : The values of the standard errors of the parameters.

lower/upper : The lower and upper bounds of the confidence intervals; column names indi-

cate the as in 0.5+/-level/2, using the level argument.

Note

Note that the quality of the resulting standard errors is similar to those reported in Visser et al (2000) for both bootstrap and the profile likelihood methods. In Visser et al (2000), the finite differences standard errors were somewhat less precise as they relied on a very parsimonious but indeed less precise method for computing the finite differences approximation (computation time was a much scarcer resource at the time then it is now).

Author(s)

Ingmar Visser

References

Ingmar Visser, Maartje E. J. Raijmakers, and Peter C. M. Molenaar (2000). Confidence intervals for hidden Markov model parameters. *British journal of mathematical and statistical psychology*, 53, p. 317-327.

Examples

```
data(speed)
# 2-state model on rt and corr from speed data set
# with Pacc as covariate on the transition matrix
# ntimes is used to specify the lengths of 3 separate series
mod1 <- depmix(list(rt~1,corr~1),data=speed,transition=~Pacc,nstates=2,
family=list(gaussian(),multinomial("identity")),ntimes=c(168,134,137))
# fit the model
set.seed(3)
fmod1 <- fit(mod1)
vcov(fmod1)$vcov # $
standardError(fmod1)
confint(fmod1)</pre>
```

viterbi

Viterbi algorithm for decoding the most likely state sequence

Description

Apply the Viterbi algorithm to compute the maximum a posteriori state sequence for a mix or depmix object.

52 viterbi

Usage

```
viterbi(object, na.allow=TRUE)
```

Arguments

object A mix or depmix object.

na.allow logical. If TRUE, the density of missing responses is set to 1, similar as in the

forwardbackward algorithm. If FALSE, missing values have NA as density

values, and will result in an error.

Details

The Viterbi algorithm is used for global decoding of the hidden state sequence. Global decoding is based on the conditional probability $p(S_1, \ldots, S_T \mid Y_1, \ldots, Y_T)$, and consists of determining, at each time point $t = 1, \ldots, T$:

$$s*_t = \arg\max_{i=1}^{N} p(S_1 = s*_1, \dots, S_{t-1} = s*_{t-1}, S_t = i, S_{t+1} = s*_{t+1}, \dots, S_T = s*_T \mid Y_1, \dots, Y_T)$$

where N is the total number of states.

The Viterbi algorithm is a dynamic programming algorithm that relies on "delta" probabilities (see Rabiner, 1989), which are defined as the joint probability of the most likely state sequence ending in state i at time t, and all the observations up to time t. The implementation here normalizes these probabilities on a time-point basis, dividing the delta probability by the sum of the delta probabilities for that time point for all possible states j (including state i)). The normalized delta probabilities for each state are returned in columns 2: (nstates(object) + 1), whilst column 1 contains the indices of the maximum a posteriori states.

Value

viterbi returns a data. frame with in the first column the maximum a posteriori state sequence. This is a vector with integers corresponding to the index of the most likely hidden states. The remaining columns contain the normalized "delta" probabilities (see Details).

Author(s)

Maarten Speekenbrink

References

Lawrence R. Rabiner (1989). A tutorial on hidden Markov models and selected applications in speech recognition. *Proceedings of IEEE*, 77-2, p. 267-295.

Examples

```
data(speed)
```

```
# 2-state model on rt and corr from speed data set
```

with Pacc as covariate on the transition matrix

viterbi 53

```
# ntimes is used to specify the lengths of 3 separate series
mod <- depmix(list(rt~1,corr~1),data=speed,transition=~Pacc,nstates=2,
family=list(gaussian(),multinomial("identity")),ntimes=c(168,134,137))
fmod <- fit(mod)
# result of viterbi is stored in a depmix-fitted object in slot "posterior"
identical(viterbi(fmod),fmod@posterior)</pre>
```

Index

| * classes | depmix, ANY-method (depmix), 4 |
|---|--|
| depmix-class, 8 | depmix-class, 8 |
| depmix.fitted-class, 12 | depmix-methods, 9 |
| depmix.sim-class, 13 | depmix.fit (fit), 16 |
| mix-class, 32 | depmix.fitted, 17 |
| mix.fitted-class, 33 | <pre>depmix.fitted, 17 depmix.fitted (depmix.fitted-class), 12</pre> |
| mix.sim-class, 34 | depmix.fitted-class, 12 |
| response-class, 39 | depmix.fitted.classLik |
| * datasets | (depmix.fitted-class), 12 |
| balance, 3 | depmix.fitted.classLik-class |
| sp500, 45 | (depmix.fitted-class), 12 |
| speed, 46 | depmix.sim (depmix.sim-class), 13 |
| * methods | depmix.sim-class, 13 |
| depmix, 4 | depmixS4, 4, 30 |
| depmix-methods, 9 | depmixS4 (depmixS4-package), 2 |
| em.control, 14 | depmixS4-package, 2 |
| fit, 16 | depilition package, 2 |
| forwardbackward, 21 | em.control, 14, <i>16</i> , <i>17</i> |
| GLMresponse, 22 | |
| llratio, 24 | fit, 3, 5, 6, 16, 24–26, 31, 32, 37, 49, 50 |
| makeDepmix, 25 | fit, depmix-method (fit), 16 |
| mix, 30 | fit, mix-method (fit), 16 |
| multistart, 35 | formatperc, 21 |
| posterior, 36 | formula, 23, 48 |
| response-classes, 40 | forwardbackward, <i>10</i> , 21, <i>37</i> , <i>52</i> |
| simulate, 44 | forwardbackward,depmix-method |
| transInit, 48 | (forwardbackward), 21 |
| vcov, 49 | forwardbackward,mix-method |
| * models | (forwardbackward), 21 |
| responses, 41 | freepars, 17 |
| * package | freepars (depmix-methods), 9 |
| depmixS4-package, 2 | freepars,depmix-method |
| | (depmix-methods), 9 |
| balance, 3 | freepars,depmix.fitted-method |
| BINOMresponse (responses), 41 | (depmix-methods), 9 |
| confint (vcov), 49 | freepars, mix-method (depmix-methods), 9 |
| confint, mix-method (vcov), 49 | freepars,mix.fitted-method |
| , ,, | (depmix-methods), 9 |
| depmix, 2, 3, 4, 8, 12, 13, 16, 22, 25, 26, 39, | |
| 40, 48, 49 | GAMMAresponse (responses), 41 |
| | |

INDEX 55

| getdf (GLMresponse), 22 | MVNresponse (responses), 41 |
|---|---|
| getdf,MULTINOMresponse-method | MVNresponse-class (response-classes), 40 |
| (GLMresponse), 22 | |
| getdf,response-method(GLMresponse),22 | nlme, 50 |
| <pre>getdf,transInit-method(transInit),48</pre> | nnet, 40 |
| <pre>getmodel (depmix-methods), 9</pre> | nobs (depmix-methods), 9 |
| <pre>getmodel,depmix-method</pre> | nobs, depmix-method (depmix-methods), 9 |
| (depmix-methods), 9 | nobs, mix-method(depmix-methods), 9 |
| <pre>getmodel, mix-method (depmix-methods), 9</pre> | NORMresponse (responses), 41 |
| getpars, <i>5</i> , <i>17</i> , <i>31</i> | npar (depmix-methods), 9 |
| getpars (depmix-methods), 9 | npar, depmix-method (depmix-methods), 9 |
| <pre>getpars,depmix-method(depmix-methods),</pre> | npar, mix-method (depmix-methods), 9 |
| 9 | nresp(depmix-class), 8 |
| getpars, mix-method (depmix-methods), 9 | <pre>nresp,depmix-method(depmix-class), 8</pre> |
| glm, 2, 23, 40 | nresp,depmix.sim-method |
| GLMresponse, 5, 6, 22, 25, 26, 31, 32, 40–42 | (depmix.sim-class), 13 |
| GLMresponse, formula-method | <pre>nresp,mix-method(mix-class), 32</pre> |
| (GLMresponse), 22 | <pre>nresp,mix.sim-method(mix.sim-class), 34</pre> |
| GLMresponse-class (response-classes), 40 | nstates (depmix-class), 8 |
| • | <pre>nstates,depmix-method(depmix-class), 8</pre> |
| hessian (vcov), 49 | nstates,depmix.sim-method |
| hessian, mix-method (vcov), 49 | (depmix.sim-class), 13 |
| | nstates, mix-method (mix-class), 32 |
| llratio, <i>17</i> , 24 | <pre>nstates,mix.sim-method(mix.sim-class),</pre> |
| logLik (depmix-methods), 9 | 34 |
| <pre>logLik,depmix-method(depmix-methods),9</pre> | <pre>ntimes (depmix-class), 8</pre> |
| <pre>logLik,depmix.fitted.classLik-method</pre> | <pre>ntimes,depmix-method(depmix-class), 8</pre> |
| (depmix-methods), 9 | ntimes,depmix.sim-method |
| <pre>logLik,mix-method (depmix-methods), 9</pre> | (depmix.sim-class), 13 |
| <pre>logLik,mix.fitted.classLik-method</pre> | ntimes, mix-method (mix-class), 32 |
| (depmix-methods), 9 | <pre>ntimes,mix.sim-method(mix.sim-class),</pre> |
| loglikelihoodratio (llratio), 24 | 34 |
| | DOTCCON and a contract of the |
| makeDepmix, 3, 5, 6, 23, 25, 31, 42 | POISSONresponse (responses), 41 |
| makeMix (makeDepmix), 25 | posterior, 17, 36 |
| mix, 2, 16, 30, 32–34 | posterior, depmix-method (posterior), 36 |
| mix, ANY-method (mix), 30 | posterior, depmix. fitted-method |
| mix-class, 32 | (posterior), 36 |
| mix.fit(fit), 16 | posterior, mix-method (posterior), 36 |
| mix.fitted-class, 33 | posterior, mix. fitted-method |
| mix.fitted.classLik-class | (posterior), 36 |
| (mix.fitted-class), 33 | response-class, 39 |
| mix.sim(mix.sim-class), 34 | response-classes, 40 |
| mix.sim-class, 34 | responses, 23, 41 |
| MULTINOMresponse (responses), 41 | 1 C3p0113C3, 23, 41 |
| multistart, 35 | setpars, <i>5</i> , <i>17</i> , <i>31</i> |
| multistart, depmix-method (multistart), | setpars (depmix-methods), 9 |
| 35 | setpars, depmix-method (depmix-methods), |
| multistart, mix-method (multistart), 35 | 9 |

56 INDEX

```
setpars, mix-method (depmix-methods), 9
show (depmix), 4
show, depmix-method (depmix), 4
show, depmix.fitted-method(fit), 16
show, GLMresponse-method (GLMresponse),
show, llratio-method (llratio), 24
show, mix-method (mix), 30
show, mix. fitted-method (fit), 16
show, MVNresponse-method (responses), 41
simulate, 44
simulate,BINOMresponse-method
        (simulate), 44
simulate, depmix-method (simulate), 44
simulate, GAMMAresponse-method
        (simulate), 44
simulate,GLMresponse-method(simulate),
        44
simulate, mix-method (simulate), 44
simulate, MULTINOMresponse-method
        (simulate), 44
simulate, MVNresponse-method (simulate),
        44
simulate, NORMresponse-method
        (simulate), 44
simulate, POISSONresponse-method
        (simulate), 44
simulate, response-method (simulate), 44
simulate, transInit-method (simulate), 44
solnp, 16
sp500, 45
speed, 46
standardError (vcov), 49
standardError, mix-method (vcov), 49
stationary, 47
summary (depmix), 4
summary, depmix-method (depmix), 4
summary, depmix. fitted-method (fit), 16
summary, mix-method (mix), 30
summary, mix.fitted-method (fit), 16
transInit, 5, 6, 8, 13, 25, 26, 31, 32, 34, 48
transInit, formula-method(transInit), 48
transInit-class (response-classes), 40
vcov, 49
vcov, mix-method (vcov), 49
viterbi, 10, 37, 51
viterbi2 (viterbi), 51
```