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Author Seongil Jo [aut],

Taeryon Choi [aut],

Beomjo Park [aut, cre],

Peter J. Lenk [ctb]

Maintainer Beomjo Park <beomjop@gmail.com>

Imports MASS, ggplot2, gridExtra

Description Contains functions to perform Bayesian inference using a spectral analysis of Gaussian process priors.

Gaussian processes are represented with a Fourier series based on cosine basis functions. Currently the package includes parametric linear models, partial linear additive models with/without shape restrictions, generalized linear additive models with/without shape restrictions, and density estimation model. To maximize computational efficiency, the actual Markov chain Monte Carlo sampling for each model is done using codes written in FORTRAN 90. This software has been developed using funding supported by Basic Science Research Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Education (no. NRF-2016R1D1A1B03932178 and no. NRF-2017R1D1A3B03035235).

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2 blq

Contents

blq	Bayesian Quantile Regression	
Index		58
	wage.union	56
	traffic	55
	rald	54
	predict.bsamdpm	53
	predict.bsam	51
	predict.blm	50
	plot.fitted.bsamdpm	49
	plot.fitted.bsam	48
	plot.fitted.bsad	48
	plot.bsam	40
	plot.bsad	46
	plot.blm	45
	plasma	44
	London.Mortality	43
	intsim	42
	intgrat	41
	gbsar	37
	gblr	34
	fs	34
	fitted.bsamdpm	33
	fitted.bsam	32
	fitted.bsad	31
	fitted.blm	30
	Elec.demand	29
	cadmium	28
	bsardpm	24
	bsarBig	22
	bsar	17
	bsaqdpm	13
	bsaq	9
	bsad	6
	blr	4
	blq	2

Description

This function fits a Bayesian quantile regression model.

blq 3

Usage

blq(formula, data = NULL, p, mcmc = list(), prior = list(), marginal.likelihood = TRUE)

Arguments

formula an object of class "formula"

data an optional data frame.

g quantile of interest (default=0.5).

a list giving the MCMC parameters. The list includes the following integers mcmc

(with default values in parentheses): nblow (1000) giving the number of MCMC in transition period, nskip (1) giving the thinning interval, smcmc (1000) giv-

ing the number of MCMC for analysis.

a list giving the prior information. The list includes the following parameters prior

> (default values specify the non-informative prior): beta_m0 and beta_v0 giving the hyperparameters of the multivariate normal distribution for parametric part including intercept, sigma2_m0 and sigma2_v0 giving the prior mean and

variance of the inverse gamma prior for the scale parameter of response.

marginal.likelihood

a logical variable indicating whether the log marginal likelihood is calculated. The methods of Gelfand and Dey (1994) is used.

Details

This generic function fits a Bayesian quantile regression model.

Let y_i and w_i be the response and the vector of parametric predictors, respectively. Further, let $x_{i,k}$ be the covariate related to the response, linearly. The model is as follows.

$$y_i = w_i^T \beta + \epsilon_i, \ i = 1, \dots, n,$$

where the error terms $\{\epsilon_i\}$ are a random sample from an asymmetric Laplace distribution, $ALD_p(0,\sigma^2)$, which has the following probability density function:

$$ALD_p(\epsilon; \mu, \sigma^2) = \frac{p(1-p)}{\sigma^2} \exp\left(-\frac{(x-\mu)[p-I(x \le \mu)]}{\sigma^2}\right),$$

where $0 is the skew parameter, <math>\sigma^2 > 0$ is the scale parameter, $-\infty < \mu < \infty$ is the location parameter, and $I(\cdot)$ is the indication function.

The conjugate priors are assumed for β and σ :

$$\beta | \sigma \sim N(m_{0,\beta}, \sigma^2 V_{0,\beta}), \quad \sigma^2 \sim IG\left(\frac{r_{0,\sigma}}{2}, \frac{s_{0,\sigma}}{2}\right)$$

Value

An object of class blm representing the Bayesian parametric linear model fit. Generic functions such as print and fitted have methods to show the results of the fit.

The MCMC samples of the parameters in the model are stored in the list mcmc. draws, the posterior samples of the fitted values are stored in the list fit.draws, and the MCMC samples for the log marginal likelihood are saved in the list loglik. draws. The output list also includes the following objects:

4 blr

post.est posterior estimates for all parameters in the model. lmarg log marginal likelihood using Gelfand-Dey method. rsquarey correlation between y and \hat{y} . the matched call.

call the materied can.

mcmctime running time of Markov chain from system.time().

References

Gelfand, A. E. and Dey, K. K. (1994) Bayesian model choice: asymptotics and exact calculations. *Journal of the Royal Statistical Society. Series B - Statistical Methodology*, **56**, 501-514.

Kozumi, H. and Kobayashi, G. (2011) Gibbs sampling methods for Bayesian quantile regression. *Journal of Statistical Computation and Simulation*, **81**(11), 1565-1578.

See Also

```
blr, gblr
```

Examples

```
# Simulated example #
######################
# Simulate data
set.seed(1)
n <- 100
w <- runif(n)</pre>
y <- 3 + 2*w + rald(n, scale = 0.8, p = 0.5)
# Fit median regression
fout <- blq(y \sim w, p = 0.5)
# Summary
print(fout); summary(fout)
# fitted values
fit <- fitted(fout)</pre>
# Plots
plot(fout)
```

blr

Bayesian Linear Regression

Description

This function fits a Bayesian linear regression model using scale invariant prior.

blr 5

Usage

blr(formula, data = NULL, mcmc = list(), prior = list(), marginal.likelihood = TRUE)

Arguments

formula an object of class "formula"

data an optional data frame.

mcmc a list giving the MCMC parameters. The list includes the following integers

(with default values in parentheses): nblow (1000) giving the number of MCMC in transition period, nskip (1) giving the thinning interval, smcmc (1000) giv-

ing the number of MCMC for analysis.

prior a list giving the prior information. The list includes the following parameters

(default values specify the non-informative prior): beta_m0 and beta_v0 giving the hyperparameters of the multivariate normal distribution for parametric part including intercept, sigma2_m0 and sigma2_v0 giving the prior mean and

variance of the inverse gamma prior for the scale parameter of response.

marginal.likelihood

a logical variable indicating whether the log marginal likelihood is calculated.

Details

This generic function fits a Bayesian linear regression model using scale invariant prior.

Let y_i and w_i be the response and the vector of parametric predictors, respectively. The model for regression function is as follows.

$$y_i = w_i^T \beta + \epsilon_i, \ i = 1, \dots, n,$$

where the error terms $\{\epsilon_i\}$ are a random sample from a normal distribution, $N(0, \sigma^2)$.

The conjugate priors are assumed for β and σ :

$$\beta | \sigma \sim N(m_{0,\beta}, \sigma^2 V_{0,\beta}), \quad \sigma^2 \sim IG\left(\frac{r_{0,\sigma}}{2}, \frac{s_{0,\sigma}}{2}\right)$$

Value

An object of class blm representing the Bayesian spectral analysis model fit. Generic functions such as print and fitted have methods to show the results of the fit.

The MCMC samples of the parameters in the model are stored in the list mcmc.draws and the posterior samples of the fitted values are stored in the list fit.draws. The output list also includes the following objects:

post.est posterior estimates for all parameters in the model.

lmarg log marginal likelihood. rsquarey correlation between y and \hat{y} .

call the matched call.

mcmctime running time of Markov chain from system.time().

6 bsad

See Also

```
blq, gblr
```

Examples

```
#######################
# Simulated example #
# Simulate data
set.seed(1)
n <- 100
w <- runif(n)</pre>
y < -3 + 2*w + rnorm(n, sd = 0.8)
# Fit the model with default priors and mcmc parameters
fout <- blr(y \sim w)
# Summary
print(fout); summary(fout)
# Fitted values
fit <- fitted(fout)</pre>
# Plots
plot(fout)
```

bsad

Bayesian Semiparametric Density Estimation

Description

This function fits a semiparametric model, which consists of parametric and nonparametric components, for estimating density using a logistic Gaussian process.

Usage

```
bsad(x, xmin, xmax, nint, MaxNCos, mcmc = list(), prior = list(),
smoother = c('geometric', 'algebraic'),
parametric = c('none', 'normal', 'gamma', 'laplace'), marginal.likelihood = TRUE,
verbose = FALSE)
```

Arguments

x a vector giving the data from which the density estimate is to be computed.

xmin minimum value of x. xmax maximum value of x.

bsad 7

nint number of grid points for plots (need to be odd). The default is 201.

MaxNCos maximum number of Fourier coefficients.

mcmc a list giving the MCMC parameters. The list includes the following integers

(with default values in parentheses): kappaloop (5) giving the number of MCMC loops within each choice of kappa, nblow (10000) giving the number of MCMC in transition period, nskip (10) giving the thinning interval, smcmc (1000) giving the number of MCMC for analysis, and ndisp (1000) giving the number of saved draws to be displayed on screen (the function reports on the screen when

every ndisp iterations have been carried out).

prior a list giving the prior information. The list includes the following parameters

(default values specify the non-informative prior): gmax giving maximum value for gamma (default = 5), PriorProbs giving prior probability of parametric and semiparametric models, beta_m0 and beta_v0 giving the hyperparameters for prior distribution of the parametric coefficients, r0 and s0 giving the hyperparameters of σ^2 for the logits, u0 and v0 giving the hyperparameters of τ^2 for Fourier coefficients, PriorKappa and KappaGrid giving prior on the number of

cosine terms.

smoother types of smoothing priors for Fourier coefficients. See Details.

parametric specifying a distribution of the parametric part to be test.

marginal.likelihood

a logical variable indicating whether the log marginal likelihood is calculated.

verbose a logical variable. If TRUE, the iteration number and the Metropolis acceptance

rate are printed to the screen.

Details

This generic function fits a semiparametric model, which consists of parametric and nonparametric, for density estimation (Lenk, 2003):

$$f(x|\beta, Z) = \frac{\exp[h(x)^{\top}\beta + Z(x)]}{\int_{\mathcal{X}} \exp[h(y)^{\top}\beta + Z(y)]dG(y)}$$

where Z is a zero mean, second-order Gaussian process with bounded, continuous covariance function. i.e.,

$$E[Z(x), Z(y)] = \sigma(x, y), \quad \int_{\mathcal{X}} ZdG = 0 \ (a.s.)$$

Using the Karhunen-Loeve Expansion, Z is represented as infinite series with random coefficients

$$Z(x) = \sum_{j=1}^{\infty} \theta_j \varphi_j(x),$$

where $\{\varphi_j\}$ is the cosine basis, $\varphi_j(x) = \sqrt{2}\cos[j\pi G(x)]$.

For the random Fourier coefficients of the expansion, two smoother priors are assumed (optional),

$$\theta_j | \tau, \gamma \sim N(0, \tau^2 \exp[-j\gamma]), \ j \ge 1 \ (geometric \ smoother)$$

 $\theta_j | \tau, \gamma \sim N(0, \tau^2 \exp[-ln(j+1)\gamma]), \ j \ge 1 \ (algebraic \ smoother)$

8 bsad

The coefficient β have the popular normal prior,

$$\beta | m_{0,\beta}, V_{0,\beta} \sim N(m_{0,\beta}, V_{0,\beta})$$

To complete the model specification, independent hyper priors are assumed,

$$\tau^2 | r_0, s_0 \sim IGa(r_0/2, s_0/2)$$
$$\gamma | w_0 \sim Exp(w_0)$$

Note that the posterior algorithm is based on computing a discrete version of the likelihood over a fine mesh on \mathcal{X} .

Value

An object of class bsad representing the Bayesian spectral analysis density estimation model fit. Generic functions such as print, fitted and plot have methods to show the results of the fit.

The MCMC samples of the parameters in the model are stored in the list mcmc.draws, the posterior samples of the fitted values are stored in the list fit.draws, and the MCMC samples for the log marginal likelihood are saved in the list loglik.draws. The output list also includes the following objects:

post.est posterior estimates for all parameters in the model.

lmarg log marginal likelihood.

ProbProbs posterior probability of models.

call the matched call.

mcmctime running time of Markov chain from system.time().

References

Jo, S., Choi, T., Park, B. and Lenk, P. (2019). bsamGP: An R Package for Bayesian Spectral Analysis Models Using Gaussian Process Priors. *Journal of Statistical Software*, **90**, 310-320.

Lenk, P. (2003) Bayesian semiparametric density estimation and model verification using a logistic Gaussian process. *Journal of Computational and Graphical Statistics*, **12**, 548-565.

Examples

bsaq

Bayesian Shape-Restricted Spectral Analysis Quantile Regression

Description

This function fits a Bayesian semiparametric quantile regression model to estimate shape-restricted functions using a spectral analysis of Gaussian process priors.

Usage

```
bsaq(formula, xmin, xmax, p, nbasis, nint, mcmc = list(), prior = list(),
shape = c('Free', 'Increasing', 'Decreasing', 'IncreasingConvex', 'DecreasingConcave',
'IncreasingConcave', 'DecreasingConvex', 'IncreasingS', 'DecreasingS',
'IncreasingRotatedS','DecreasingRotatedS','InvertedU','Ushape',
'IncMultExtreme','DecMultExtreme'), nExtreme = NULL,
marginal.likelihood = TRUE, spm.adequacy = FALSE, verbose = FALSE)
```

Arguments

formula	an object of class "formula"
xmin	a vector or scalar giving user-specific minimum values of x. The default values are minimum values of x.
xmax	a vector or scalar giving user-specific maximum values of x. The default values are maximum values of x.
p	quantile of interest (default=0.5).
nbasis	number of cosine basis functions.
nint	number of grid points where the unknown function is evaluated for plotting. The default is 200.

mcmc

a list giving the MCMC parameters. The list includes the following integers (with default values in parentheses): nblow0 (1000) giving the number of initialization period for adaptive metropolis, maxmodmet (5) giving the maximum number of times to modify metropolis, nblow (10000) giving the number of MCMC in transition period, nskip (10) giving the thinning interval, smcmc (1000) giving the number of MCMC for analysis, and ndisp (1000) giving the number of saved draws to be displayed on screen (the function reports on the screen when every ndisp iterations have been carried out).

prior

a list giving the prior information. The list includes the following parameters (default values specify the non-informative prior): iflagprior choosing a smoothing prior for spectral coefficients (iflagprior=0 assigns T-Smoother prior (default), iflagprior=1 chooses Lasso-Smoother prior), theta0_m0 and theta0_s0 giving the hyperparameters for prior distribution of the spectral coefficients (theta0_m0 and theta0_s0 are used when the functions have shape-restriction), tau2_m0, tau2_s0 and w0 giving the prior mean and standard deviation of smoothing prior (When iflagprior=1, tau2_m0 is only used as the hyperparameter), beta_m0 and beta_v0 giving the hyperparameters of the multivariate normal distribution for parametric part including intercept, sigma2_m0 and sigma2_v0 giving the prior mean and variance of the inverse gamma prior for the scale parameter of response, alpha_m0 and alpha_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the constant of integration, if lagps i determining the prior of slope for logisitic function in S or U shaped (iflagpsi=1 (default), slope ψ is sampled and iflagpsi=0, ψ is fixed), psifixed giving initial value (iflagpsi=1) or fixed value (iflagpsi=0) of slope, omega_m0 and omega_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the inflection point of S or U shaped func-

shape a vector giving types of shape restriction.

nExtreme a vector of extreme points for 'IncMultExtreme', 'DecMultExtreme' shape re-

strictions.

marginal.likelihood

a logical variable indicating whether the log marginal likelihood is calculated. The methods of Gelfand and Dey (1994) and Newton and Raftery (1994) are

used.

spm. adequacy a logical variable indicating whether the log marginal likelihood of linear model

is calculated. The marginal likelihood gives the values of the linear regression

model excluding the nonlinear parts.

verbose a logical variable. If TRUE, the iteration number and the Metropolis acceptance

rate are printed to the screen.

Details

This generic function fits a Bayesian spectral analysis quantile regression model for estimating shape-restricted functions using Gaussian process priors. For enforcing shape-restrictions, the model assumed that the derivatives of the functions are squares of Gaussian processes.

Let y_i and w_i be the response and the vector of parametric predictors, respectively. Further, let $x_{i,k}$ be the covariate related to the response through an unknown shape-restricted function. The model for estimating shape-restricted functions is as follows.

$$y_i = w_i^T \beta + \sum_{k=1}^K f_k(x_{i,k}) + \epsilon_i, \ i = 1, \dots, n,$$

where f_k is an unknown shape-restricted function of the scalar $x_{i,k} \in [0,1]$ and the error terms $\{\epsilon_i\}$ are a random sample from an asymmetric Laplace distribution, $ALD_p(0,\sigma^2)$, which has the following probability density function:

$$ALD_p(\epsilon; \mu, \sigma^2) = \frac{p(1-p)}{\sigma^2} \exp\left(-\frac{(x-\mu)[p-I(x \le \mu)]}{\sigma^2}\right),$$

where $0 is the skew parameter, <math>\sigma^2 > 0$ is the scale parameter, $-\infty < \mu < \infty$ is the location parameter, and $I(\cdot)$ is the indication function.

The prior of function without shape restriction is:

$$f(x) = Z(x),$$

where Z is a second-order Gaussian process with mean function equal to zero and covariance function $\nu(s,t)=E[Z(s)Z(t)]$ for $s,t\in[0,1]$. The Gaussian process is expressed with the spectral representation based on cosine basis functions:

$$Z(x) = \sum_{j=0}^{\infty} \theta_j \varphi_j(x)$$

$$\varphi_0(x) = 1$$
 and $\varphi_j(x) = \sqrt{2}\cos(\pi jx), j \ge 1, 0 \le x \le 1$

The shape-restricted functions are modeled by assuming the qth derivatives of f are squares of Gaussian processes:

$$f^{(q)}(x) = \delta Z^2(x) h(x), \ \delta \in \{1, -1\}, \ q \in \{1, 2\},$$

where h is the squish function. For monotonic, monotonic convex, and concave functions, h(x) = 1, while for S and U shaped functions, h is defined by

$$h(x) = \frac{1 - \exp[\psi(x - \omega)]}{1 + \exp[\psi(x - \omega)]}, \ \psi > 0, \ 0 < \omega < 1$$

For the spectral coefficients of functions without shape constraints, the scale-invariant prior is used (The intercept is included in β):

$$\theta_j | \sigma, \tau, \gamma \sim N(0, \sigma^2 \tau^2 \exp[-j\gamma]), \ j \ge 1$$

The priors for the spectral coefficients of shape restricted functions are:

$$\theta_0|\sigma \sim N(m_{\theta_0}, \sigma v_{\theta_0}^2), \quad \theta_j|\sigma, \tau, \gamma \sim N(m_{\theta_j}, \sigma \tau^2 \exp[-j\gamma]), \ j \ge 1$$

To complete the model specification, the conjugate priors are assumed for β and σ :

$$\beta | \sigma \sim N(m_{0,\beta}, \sigma^2 V_{0,\beta}), \quad \sigma^2 \sim IG\left(\frac{r_{0,\sigma}}{2}, \frac{s_{0,\sigma}}{2}\right)$$

Value

An object of class beam representing the Bayesian spectral analysis model fit. Generic functions such as print, fitted and plot have methods to show the results of the fit.

The MCMC samples of the parameters in the model are stored in the list mcmc.draws, the posterior samples of the fitted values are stored in the list fit.draws, and the MCMC samples for the log marginal likelihood are saved in the list loglik.draws. The output list also includes the following objects:

References

Jo, S., Choi, T., Park, B. and Lenk, P. (2019). bsamGP: An R Package for Bayesian Spectral Analysis Models Using Gaussian Process Priors. *Journal of Statistical Software*, **90**, 310-320.

Lenk, P. and Choi, T. (2017) Bayesian Analysis of Shape-Restricted Functions using Gaussian Process Priors. *Statistica Sinica*, **27**: 43-69.

Gelfand, A. E. and Dey, K. K. (1994) Bayesian model choice: asymptotics and exact calculations. *Journal of the Royal Statistical Society. Series B - Statistical Methodology*, **56**, 501-514.

Kozumi, H. and Kobayashi, G. (2011) Gibbs sampling methods for Bayesian quantile regression. *Journal of Statistical Computation and Simulation*, **81**(11), 1565-1578.

Newton, M. A. and Raftery, A. E. (1994) Approximate Bayesian inference with the weighted likelihood bootstrap (with discussion). *Journal of the Royal Statistical Society. Series B - Statistical Methodology*, **56**, 3-48.

See Also

bsar, gbsar

Examples

```
x <- runif(n)</pre>
y < - \log(1 + 10*x) + rald(n, scale = 0.5, p = 0.5)
# Number of cosine basis functions
nbasis <- 50
# Fit the model with default priors and mcmc parameters
fout1 <- bsaq(y \sim fs(x), p = 0.25, nbasis = nbasis,
              shape = 'IncreasingConcave')
fout2 <- bsaq(y \sim fs(x), p = 0.5, nbasis = nbasis,
              shape = 'IncreasingConcave')
fout3 <- bsaq(y \sim fs(x), p = 0.75, nbasis = nbasis,
              shape = 'IncreasingConcave')
# fitted values
fit1 <- fitted(fout1)</pre>
fit2 <- fitted(fout2)</pre>
fit3 <- fitted(fout3)</pre>
# plots
plot(x, y, lwd = 2, xlab = 'x', ylab = 'y')
lines(fit1$xgrid, fit1$wbeta$mean[1] + fit1$fxgrid$mean, lwd=2, col=2)
lines(fit2$xgrid, fit2$wbeta$mean[1] + fit2$fxgrid$mean, lwd=2, col=3)
lines(fit3$xgrid, fit3$wbeta$mean[1] + fit3$fxgrid$mean, lwd=2, col=4)
legend('topleft', legend = c('1st Quartile', '2nd Quartile', '3rd Quartile'),
       1wd = 2, col = 2:4, 1ty = 1)
## End(Not run)
```

bsagdpm

Bayesian Shape-Restricted Spectral Analysis Quantile Regression with Dirichlet Process Mixture Errors

Description

This function fits a Bayesian semiparametric quantile regression model to estimate shape-restricted functions using a spectral analysis of Gaussian process priors. The model assumes that the errors follow a Dirichlet process mixture model.

Usage

```
bsaqdpm(formula, xmin, xmax, p, nbasis, nint,
mcmc = list(), prior = list(), egrid, ngrid = 500,
shape = c('Free', 'Increasing', 'Decreasing', 'IncreasingConvex', 'DecreasingConcave',
'IncreasingConcave', 'DecreasingConvex', 'IncreasingS', 'DecreasingS',
'IncreasingRotatedS', 'DecreasingRotatedS', 'InvertedU', 'Ushape'),
verbose = FALSE)
```

Arguments

ngrid

shape

verbose

formula an object of class "formula"

xmin a vector or scalar giving user-specific minimum values of x. The default values

are minimum values of x.

xmax a vector or scalar giving user-specific maximum values of x. The default values

are maximum values of x.

p quantile of interest (default=0.5).

nbasis number of cosine basis functions.

nint number of grid points where the unknown function is evaluated for plotting. The

default is 200.

mcmc a list giving the MCMC parameters. The list includes the following integers

(with default values in parentheses): nblow0 (1000) giving the number of initialization period for adaptive metropolis, maxmodmet (5) giving the maximum number of times to modify metropolis, nblow (10000) giving the number of MCMC in transition period, nskip (10) giving the thinning interval, smcmc (1000) giving the number of MCMC for analysis, and ndisp (1000) giving the number of saved draws to be displayed on screen (the function reports on

the screen when every ndisp iterations have been carried out).

prior a list giving the prior information. The list includes the following parame-

ters (default values specify the non-informative prior): iflagprior choosing a smoothing prior for spectral coefficients (iflagprior=0 assigns T-Smoother prior (default), iflagprior=1 chooses Lasso-Smoother prior), theta0_m0 and theta0_s0 giving the hyperparameters for prior distribution of the spectral coefficients (theta0_m0 and theta0_s0 are used when the functions have shape-restriction), tau2_m0, tau2_s0 and w0 giving the prior mean and standard deviation of smoothing prior (When iflagprior=1, tau2_m0 is only used as the hyperparameter), beta_m0 and beta_v0 giving the hyperparameters of the multivariate normal distribution for parametric part including intercept, sigma2_m0 and sigma2_v0

giving the prior mean and variance of the inverse gamma prior for the scale parameter of response, alpha_m0 and alpha_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the constant of integration, iflagpsi determining the prior of slope for logisitic function in S or U shaped (iflagpsi=1 (default), slope ψ is sampled and iflagpsi=0, ψ is fixed), psifixed giving initial value (iflagpsi=1) or fixed value (iflagpsi=0) of slope,

omega_m0 and omega_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the inflection point of S or U shaped function.

egrid a vector giving grid points where the residual density estimate is evaluated. The default range is from -10 to 10.

a vector giving number of grid points where the residual density estimate is

evaluated. The default value is 500.

a vector giving types of shape restriction.

a logical variable. If TRUE, the iteration number and the Metropolis acceptance

rate are printed to the screen.

Details

This generic function fits a Bayesian spectral analysis quantile regression model for estimating shape-restricted functions using Gaussian process priors. For enforcing shape-restrictions, the model assumes that the derivatives of the functions are squares of Gaussian processes. The model also assumes that the errors follow a Dirichlet process mixture model.

Let y_i and w_i be the response and the vector of parametric predictors, respectively. Further, let $x_{i,k}$ be the covariate related to the response through an unknown shape-restricted function. The model for estimating shape-restricted functions is as follows.

$$y_i = w_i^T \beta + \sum_{k=1}^K f_k(x_{i,k}) + \epsilon_i, \ i = 1, \dots, n,$$

where f_k is an unknown shape-restricted function of the scalar $x_{i,k} \in [0,1]$ and the error terms $\{\epsilon_i\}$ are a random sample from a Dirichlet process mixture of an asymmetric Laplace distribution, $ALD_p(0,\sigma^2)$, which has the following probability density function:

$$\epsilon_i \sim f(\epsilon) = \int ALD_p(\epsilon; 0, \sigma^2) dG(\sigma^2),$$

$$G \sim DP(M, G0), \ G0 = Ga\left(\sigma^{-2}; \frac{r_{0,\sigma}}{2}, \frac{s_{0,\sigma}}{2}\right).$$

The prior of function without shape restriction is:

$$f(x) = Z(x),$$

where Z is a second-order Gaussian process with mean function equal to zero and covariance function $\nu(s,t)=E[Z(s)Z(t)]$ for $s,t\in[0,1]$. The Gaussian process is expressed with the spectral representation based on cosine basis functions:

$$Z(x) = \sum_{j=0}^{\infty} \theta_j \varphi_j(x)$$

$$\varphi_0(x) = 1$$
 and $\varphi_j(x) = \sqrt{2}\cos(\pi j x), j \ge 1, 0 \le x \le 1$

The shape-restricted functions are modeled by assuming the qth derivatives of f are squares of Gaussian processes:

$$f^{(q)}(x) = \delta Z^2(x)h(x), \ \delta \in \{1, -1\}, \ q \in \{1, 2\},$$

where h is the squish function. For monotonic, monotonic convex, and concave functions, h(x) = 1, while for S and U shaped functions, h is defined by

$$h(x) = \frac{1 - \exp[\psi(x - \omega)]}{1 + \exp[\psi(x - \omega)]}, \ \psi > 0, \ 0 < \omega < 1$$

For the spectral coefficients of functions without shape constraints, the scale-invariant prior is used (The intercept is included in β):

$$\theta_j | \tau, \gamma \sim N(0, \tau^2 \exp[-j\gamma]), j \ge 1$$

The priors for the spectral coefficients of shape restricted functions are:

$$\theta_0 \sim N(m_{\theta_0}, v_{\theta_0}^2), \quad \theta_j | \tau, \gamma \sim N(m_{\theta_j}, \tau^2 \exp[-j\gamma]), \ j \ge 1$$

To complete the model specification, the popular normal prior is assumed for β :

$$\beta | \sim N(m_{0,\beta}, V_{0,\beta})$$

Value

An object of class beam representing the Bayesian spectral analysis model fit. Generic functions such as print, fitted and plot have methods to show the results of the fit.

The MCMC samples of the parameters in the model are stored in the list mcmc.draws, the posterior samples of the fitted values are stored in the list fit.draws, and the MCMC samples for the log marginal likelihood are saved in the list loglik.draws. The output list also includes the following objects:

post.est posterior estimates for all parameters in the model.

lpml log pseudo marginal likelihood using Mukhopadhyay and Gelfand method.

rsquarey correlation between y and \hat{y} .

imodmet the number of times to modify Metropolis.

pmet proportion of θ accepted after burn-in.

call the matched call.

mcmctime running time of Markov chain from system. time().

References

Jo, S., Choi, T., Park, B. and Lenk, P. (2019). bsamGP: An R Package for Bayesian Spectral Analysis Models Using Gaussian Process Priors. *Journal of Statistical Software*, **90**, 310-320.

Kozumi, H. and Kobayashi, G. (2011) Gibbs sampling methods for Bayesian quantile regression. *Journal of Statistical Computation and Simulation*, **81**(11), 1565-1578.

Lenk, P. and Choi, T. (2017) Bayesian Analysis of Shape-Restricted Functions using Gaussian Process Priors. *Statistica Sinica*, **27**, 43-69.

MacEachern, S. N. and Müller, P. (1998) Estimating mixture of Dirichlet process models. *Journal of Computational and Graphical Statistics*, **7**, 223-238.

Mukhopadhyay, S. and Gelfand, A. E. (1997) Dirichlet process mixed generalized linear models. *Journal of the American Statistical Association*, **92**, 633-639.

Neal, R. M. (2000) Markov chain sampling methods for Dirichlet process mixture models. *Journal of Computational and Graphical Statistics*, **9**, 249-265.

See Also

bsaq, bsardpm

Examples

```
## Not run:
#######################
# Increasing-concave #
##############################
# Simulate data
set.seed(1)
n <- 500
x <- runif(n)</pre>
e <- c(rald(n/2, scale = 0.5, p = 0.5),
       rald(n/2, scale = 3, p = 0.5))
y < - \log(1 + 10*x) + e
# Number of cosine basis functions
nbasis <- 50
# Fit the model with default priors and mcmc parameters
fout1 <- bsaqdpm(y \sim fs(x), p = 0.25, nbasis = nbasis,
                  shape = 'IncreasingConcave')
fout2 <- bsaqdpm(y \sim fs(x), p = 0.5, nbasis = nbasis,
                  shape = 'IncreasingConcave')
fout3 <- bsaqdpm(y \sim fs(x), p = 0.75, nbasis = nbasis,
                  shape = 'IncreasingConcave')
# fitted values
fit1 <- fitted(fout1)</pre>
fit2 <- fitted(fout2)</pre>
fit3 <- fitted(fout3)</pre>
# plots
plot(x, y, lwd = 2, xlab = 'x', ylab = 'y')
lines(fit1$xgrid, fit1$wbeta$mean[1] + fit1$fxgrid$mean, lwd=2, col=2)
lines(fit2$xgrid, fit2$wbeta$mean[1] + fit2$fxgrid$mean, lwd=2, col=3)
lines(fit3$xgrid, fit3$wbeta$mean[1] + fit3$fxgrid$mean, lwd=2, col=4)
legend('topleft',legend=c('1st Quartile','2nd Quartile','3rd Quartile'),
       lwd=2, col=2:4, lty=1)
## End(Not run)
```

bsar

Bayesian Shape-Restricted Spectral Analysis Regression

Description

This function fits a Bayesian semiparametric regression model to estimate shape-restricted functions using a spectral analysis of Gaussian process priors.

Usage

```
bsar(formula, xmin, xmax, nbasis, nint, mcmc = list(), prior = list(),
shape = c('Free', 'Increasing', 'Decreasing', 'IncreasingConvex', 'DecreasingConcave',
'IncreasingConcave', 'DecreasingConvex', 'IncreasingS', 'DecreasingS',
'IncreasingRotatedS','DecreasingRotatedS','InvertedU','Ushape',
'IncMultExtreme','DecMultExtreme'), nExtreme = NULL,
marginal.likelihood = TRUE, spm.adequacy = FALSE, verbose = FALSE)
```

Arguments

formula an object of class "formula"

xmin a vector or scalar giving user-specific minimum values of x. The default values

are minimum values of x.

xmax a vector or scalar giving user-specific maximum values of x. The default values

are maximum values of x.

nbasis number of cosine basis functions.

nint number of grid points where the unknown function is evaluated for plotting. The

default is 200.

mcmc a list giving the MCMC parameters. The list includes the following integers

(with default values in parentheses): nblow0 (1000) giving the number of initialization period for adaptive metropolis, maxmodmet (5) giving the maximum number of times to modify metropolis, nblow (10000) giving the number of MCMC in transition period, nskip (10) giving the thinning interval, smcmc (1000) giving the number of MCMC for analysis, and ndisp (1000) giving the number of saved draws to be displayed on screen (the function reports on

the screen when every ndisp iterations have been carried out).

prior a list giving the prior information. The list includes the following parame-

ters (default values specify the non-informative prior): iflagprior choosing a smoothing prior for spectral coefficients (iflagprior=0 assigns T-Smoother prior (default), iflagprior=1 chooses Lasso-Smoother prior), theta0_m0 and theta0_s0 giving the hyperparameters for prior distribution of the spectral coefficients (theta0_m0 and theta0_s0 are used when the functions have shape-restriction), tau2_m0, tau2_s0 and w0 giving the prior mean and standard deviation of smoothing prior (When iflagprior=1, tau2_m0 is only used as the hyperparameter), beta_m0 and beta_v0 giving the hyperparameters of the multivariate normal distribution for parametric part including intercept, sigma2_m0 and sigma2_v0 giving the prior mean and variance of the inverse gamma prior for the scale parameter of response, alpha_m0 and alpha_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the constant of integration, iflagpsi determining the prior of slope for logisitic function in S or U shaped (iflagpsi=1 (default), slope ψ is sampled and iflagpsi=0, ψ is fixed), psifixed giving initial value (iflagpsi=1) or fixed value (iflagpsi=0) of slope,

omega_m0 and omega_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the inflection point of S or U shaped func-

tion.

shape a vector giving types of shape restriction.

nExtreme a vector of extreme points for 'IncMultExtreme', 'DecMultExtreme' shape restrictions.

marginal.likelihood

a logical variable indicating whether the log marginal likelihood is calculated. The methods of Gelfand and Dey (1994) and Newton and Raftery (1994) are used.

spm.adequacy a

a logical variable indicating whether the log marginal likelihood of linear model is calculated. The marginal likelihood gives the values of the linear regression model excluding the nonlinear parts.

verbose

a logical variable. If TRUE, the iteration number and the Metropolis acceptance rate are printed to the screen.

Details

This generic function fits a Bayesian spectral analysis regression model (Lenk and Choi, 2015) for estimating shape-restricted functions using Gaussian process priors. For enforcing shape-restrictions, they assumed that the derivatives of the functions are squares of Gaussian processes.

Let y_i and w_i be the response and the vector of parametric predictors, respectively. Further, let $x_{i,k}$ be the covariate related to the response through an unknown shape-restricted function. The model for estimating shape-restricted functions is as follows.

$$y_i = w_i^T \beta + \sum_{k=1}^K f_k(x_{i,k}) + \epsilon_i, \ i = 1, \dots, n,$$

where f_k is an unknown shape-restricted function of the scalar $x_{i,k} \in [0,1]$ and the error terms $\{\epsilon_i\}$ are a random sample from a normal distribution, $N(0, \sigma^2)$.

The prior of function without shape restriction is:

$$f(x) = Z(x),$$

where Z is a second-order Gaussian process with mean function equal to zero and covariance function $\nu(s,t)=E[Z(s)Z(t)]$ for $s,t\in[0,1]$. The Gaussian process is expressed with the spectral representation based on cosine basis functions:

$$Z(x) = \sum_{j=0}^{\infty} \theta_j \varphi_j(x)$$

$$\varphi_0(x) = 1$$
 and $\varphi_j(x) = \sqrt{2}\cos(\pi j x), j \ge 1, 0 \le x \le 1$

The shape-restricted functions are modeled by assuming the qth derivatives of f are squares of Gaussian processes:

$$f^{(q)}(x) = \delta Z^2(x)h(x), \ \delta \in \{1, -1\}, \ q \in \{1, 2\},$$

where h is the squish function. For monotonic, monotonic convex, and concave functions, h(x) = 1, while for S and U shaped functions, h is defined by

$$h(x) = \frac{1 - \exp[\psi(x - \omega)]}{1 + \exp[\psi(x - \omega)]}, \ \psi > 0, \ 0 < \omega < 1$$

For the spectral coefficients of functions without shape constraints, the scale-invariant prior is used (The intercept is included in β):

$$\theta_j | \sigma, \tau, \gamma \sim N(0, \sigma^2 \tau^2 \exp[-j\gamma]), \ j \ge 1$$

The priors for the spectral coefficients of shape restricted functions are:

$$\theta_0|\sigma \sim N(m_{\theta_0}, \sigma v_{\theta_0}^2), \quad \theta_j|\sigma, \tau, \gamma \sim N(m_{\theta_j}, \sigma \tau^2 \exp[-j\gamma]), \ j \ge 1$$

To complete the model specification, the conjugate priors are assumed for β and σ :

$$\beta | \sigma \sim N(m_{0,\beta}, \sigma^2 V_{0,\beta}), \quad \sigma^2 \sim IG\left(\frac{r_{0,\sigma}}{2}, \frac{s_{0,\sigma}}{2}\right)$$

Value

An object of class beam representing the Bayesian spectral analysis model fit. Generic functions such as print, fitted and plot have methods to show the results of the fit.

The MCMC samples of the parameters in the model are stored in the list mcmc.draws, the posterior samples of the fitted values are stored in the list fit.draws, and the MCMC samples for the log marginal likelihood are saved in the list loglik.draws. The output list also includes the following objects:

post.est posterior estimates for all parameters in the model. lmarg.lm log marginal likelihood for linear regression model. lmarg.gd log marginal likelihood using Gelfand-Dey method. log marginal likelihood using Netwon-Raftery method, which is biased. rsquarey correlation between y and \hat{y} . the matched call. running time of Markov chain from system.time().

References

Jo, S., Choi, T., Park, B. and Lenk, P. (2019). bsamGP: An R Package for Bayesian Spectral Analysis Models Using Gaussian Process Priors. *Journal of Statistical Software*, **90**, 310-320.

Lenk, P. and Choi, T. (2017) Bayesian Analysis of Shape-Restricted Functions using Gaussian Process Priors. *Statistica Sinica*, **27**, 43-69.

Gelfand, A. E. and Dey, K. K. (1994) Bayesian model choice: asymptotics and exact calculations. *Journal of the Royal Statistical Society. Series B - Statistical Methodology*, **56**, 501-514.

Newton, M. A. and Raftery, A. E. (1994) Approximate Bayesian inference with the weighted likelihood bootstrap (with discussion). *Journal of the Royal Statistical Society. Series B - Statistical Methodology*, **56**, 3-48.

See Also

bsardpm

Examples

```
## Not run:
# Increasing Convex to Concave (S-shape) #
# simulate data
f \leftarrow function(x) 5*exp(-10*(x - 1)^4) + 5*x^2
set.seed(1)
n <- 100
x <- runif(n)</pre>
y \leftarrow f(x) + rnorm(n, sd = 1)
# Number of cosine basis functions
nbasis <- 50
# Fit the model with default priors and mcmc parameters
fout <- bsar(y \sim fs(x), nbasis = nbasis, shape = 'IncreasingConvex',
           spm.adequacy = TRUE)
# Summary
print(fout); summary(fout)
# Trace plots
plot(fout)
# fitted values
fit <- fitted(fout)</pre>
# Plot
plot(fit, ask = TRUE)
# Additive Model
# Monotone-Increasing and Increasing-Convex #
# Simulate data
f1 <- function(x) 2*pi*x + sin(2*pi*x)</pre>
f2 \leftarrow function(x) \exp(6*x - 3)
n <- 200
x1 <- runif(n)</pre>
x2 <- runif(n)</pre>
x \leftarrow cbind(x1, x2)
y < -5 + f1(x1) + f2(x2) + rnorm(n, sd = 0.5)
```

22 bsarBig

```
# Number of cosine basis functions
nbasis <- 50
# MCMC parameters
mcmc <- list(nblow0 = 1000, nblow = 10000, nskip = 10,
             smcmc = 5000, ndisp = 1000, maxmodmet = 10)
# Prior information
xmin \leftarrow apply(x, 2, min)
xmax <- apply(x, 2, max)
xrange <- xmax - xmin</pre>
prior <- list(iflagprior = 0, theta0_m0 = 0, theta0_s0 = 100,</pre>
              tau2_m0 = 1, tau2_v0 = 100, w0 = 2,
              beta_m0 = numeric(1), beta_v0 = diag(100,1),
              sigma2_m0 = 1, sigma2_v0 = 1000,
              alpha_m0 = 3, alpha_s0 = 50, iflagpsi = 1,
              psifixed = 1000, omega_m0 = (xmin + xmax)/2,
              omega_s0 = (xrange)/8)
# Fit the model with user specific priors and mcmc parameters
fout <- bsar(y \sim fs(x1) + fs(x2), nbasis = nbasis, mcmc = mcmc, prior = prior,
             shape = c('Increasing', 'IncreasingS'))
# Summary
print(fout); summary(fout)
## End(Not run)
```

bsarBig

Bayesian Spectral Analysis Regression for Big data

Description

This function fits a Bayesian spectral analysis regression model for Big data.

Usage

```
bsarBig(formula, nbasis, nint, mcmc = list(), prior = list(), verbose = FALSE)
```

Arguments

formula an object of class "formula" nbasis number of cosine basis functions.

nint number of grid points where the unknown function is evaluated for plotting. The

default is 500.

mcmc a list giving the MCMC parameters. The list includes the following integers

(with default values in parentheses): nblow (10000) giving the number of MCMC in transition period, nskip (10) giving the thinning interval, smcmc (1000) giving the number of MCMC for analysis, and ndisp (1000) giving the number of

bsarBig 23

saved draws to be displayed on screen (the function reports on the screen when

every ndisp iterations have been carried out).

prior a list giving the prior information. The list includes the following parameters

(default values specify the non-informative prior): $sigma2_m0$ and $sigma2_v0$ giving the prior mean and variance of the inverse gamma prior for the scale parameter of response, $tau2_m0$, $tau2_s0$ and w0 giving the prior mean and

standard deviation of smoothing prior.

verbose a logical variable. If TRUE, the iteration number and the Metropolis acceptance

rate are printed to the screen.

Value

The MCMC samples of the parameters in the model are stored in the list mcmc.draws and the posterior samples of the fitted values are stored in the list fit.draws. The output list also includes the following objects:

post.est posterior estimates for all parameters in the model.

call the matched call.

mcmctime running time of Markov chain from system.time().

See Also

bsar

Examples

```
# Ttrue function
ftrue <- function(x){</pre>
  ft < -7*exp(-3*x) + 2*exp(-70*(x-.6)^2) - 2 + 5*x
  return(ft)
# Generate data
set.seed(1)
nobs <- 100000 # Number of observations
sigmat <- .5 # True sigma
nxgrid <- 500 # number of grid points: approximate likelihood & plots
xdata <- runif(nobs) # Generate x values</pre>
fobst <- ftrue(xdata) # True f at observations</pre>
ydata <- fobst + sigmat*rnorm(nobs)</pre>
# Compute grid on 0 to 1
xdelta <- 1/nxgrid
xgrid <- seq(xdelta/2, 1-xdelta/2, xdelta)
xgrid <- matrix(xgrid,nxgrid)</pre>
fxgridt <- ftrue(xgrid) # True f on xgrid</pre>
# Fit data
```

```
fout <- bsarBig(ydata ~ xdata, nbasis = 50, nint = nxgrid, verbose = TRUE)
# Plots
smcmc <- fout$mcmc$smcmc</pre>
t <- 1:smcmc
par(mfrow=c(2,2))
matplot(t, fout$mcmc.draws$theta, type = "1", main = "Theta", xlab = "Iteration", ylab = "Draw")
plot(t, fout$mcmc.draws$sigma, type = "1", main = "Sigma", xlab = "Iteration", ylab = "Draw")
matplot(t, fout$mcmc.draws$tau, type = "l", main = "Tau", xlab = "Iteration", ylab = "Draw")
matplot(t, fout$mcmc.draws$gamma, type = "1", main = "Gamma", xlab = "Iteration", ylab = "Draw")
dev.new()
matplot(fout$fit.draws$xgrid, cbind(fxgridt, fout$post.est$fhatm, fout$post.est$fhatq),
        type = "1", main = "Regression Function", xlab = "X", ylab = "Y")
# Compute RMISE for regression function
sse <- (fout$post.est$fhatm - fxgridt)^2</pre>
rmise <- intgrat(sse, 1/nxgrid)</pre>
rmise <- sqrt(rmise)</pre>
rmise
```

bsardpm

Bayesian Shape-Restricted Spectral Analysis Regression with Dirichlet Process Mixture Errors

Description

This function fits a Bayesian semiparametric regression model to estimate shape-restricted functions using a spectral analysis of Gaussian process priors. The model assumes that the errors follow a Dirichlet process mixture model.

Usage

```
bsardpm(formula, xmin, xmax, nbasis, nint,
mcmc = list(), prior = list(), egrid, ngrid, location = TRUE,
shape = c('Free', 'Increasing', 'Decreasing', 'IncreasingConvex', 'DecreasingConcave',
'IncreasingConcave', 'DecreasingConvex', 'IncreasingS', 'DecreasingS',
'IncreasingRotatedS','DecreasingRotatedS','InvertedU','Ushape'),
verbose = FALSE)
```

Arguments

formula	an object of class "formula"
xmin	a vector or scalar giving user-specific minimum values of \mathbf{x} . The default values are minimum values of \mathbf{x} .
xmax	a vector or scalar giving user-specific maximum values of \mathbf{x} . The default values are maximum values of \mathbf{x} .
nbasis	number of cosine basis functions.

nint number of grid points where the unknown function is evaluated for plotting. The default is 200.

mcmc a list giving the MCMC parameters. The list includes the following integers

(with default values in parentheses): nblow0 (1000) giving the number of initialization period for adaptive metropolis, maxmodmet (5) giving the maximum number of times to modify metropolis, nblow (10000) giving the number of MCMC in transition period, nskip (10) giving the thinning interval, smcmc (1000) giving the number of MCMC for analysis, and ndisp (1000) giving the number of saved draws to be displayed on screen (the function reports on

the screen when every ndisp iterations have been carried out).

prior a list giving the prior information. The list includes the following parame-

ters (default values specify the non-informative prior): if lagprior choosing a smoothing prior for spectral coefficients (iflagprior=0 assigns T-Smoother prior (default), iflagprior=1 chooses Lasso-Smoother prior), theta0_m0 and theta0_s0 giving the hyperparameters for prior distribution of the spectral coefficients (theta0_m0 and theta0_s0 are used when the functions have shape-restriction), tau2_m0, tau2_s0 and w0 giving the prior mean and standard deviation of smoothing prior (When iflagprior=1, tau2_m0 is only used as the hyperparameter), beta_m0 and beta_v0 giving the hyperparameters of the multivariate normal distribution for parametric part including intercept, sigma2_m0 and sigma2_v0 giving the prior mean and variance of the inverse gamma prior for the scale parameter of response, alpha_m0 and alpha_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the constant of integration, if lagps i determining the prior of slope for logisitic function in S or U shaped (iflagpsi=1 (default), slope ψ is sampled and iflagpsi=0, ψ is fixed), psifixed giving initial value (iflagpsi=1) or fixed value (iflagpsi=0) of slope, omega_m0 and omega_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the inflection point of S or U shaped func-

tion.

egrid a vector giving grid points where the residual density estimate is evaluated. The

default range is from -10 to 10.

ngrid a vector giving number of grid points where the residual density estimate is

evaluated. The default value is 500.

location a logical value. If it is true, error density is modelled using location-scale mix-

ture.

shape a vector giving types of shape restriction.

verbose a logical variable. If TRUE, the iteration number and the Metropolis acceptance

rate are printed to the screen.

Details

This generic function fits a Bayesian spectral analysis regression model for estimating shape-restricted functions using Gaussian process priors. For enforcing shape-restrictions, the model assumes that the derivatives of the functions are squares of Gaussian processes. The model also assumes that the errors follow a Dirichlet process mixture model.

Let y_i and w_i be the response and the vector of parametric predictors, respectively. Further, let $x_{i,k}$ be the covariate related to the response through an unknown shape-restricted function. The model for estimating shape-restricted functions is as follows.

$$y_i = w_i^T \beta + \sum_{k=1}^K f_k(x_{i,k}) + \epsilon_i, \ i = 1, \dots, n,$$

where f_k is an unknown shape-restricted function of the scalar $x_{i,k} \in [0,1]$ and the error terms $\{\epsilon_i\}$ are a random sample from a Dirichlet process mixture model,

1. scale mixture:

$$\begin{split} \epsilon_i \sim f(\epsilon) &= \int N(\epsilon; 0, \sigma^2) dG(\sigma^2), \\ G \sim DP(M, G0), \ \ G0 &= Ga\left(\sigma^{-2}; \frac{r_{0,\sigma}}{2}, \frac{s_{0,\sigma}}{2}\right). \end{split}$$

2. location-scale mixture:

$$\begin{split} \epsilon_i \sim f(\epsilon) &= \int N(\epsilon; \mu, \sigma^2) dG(\mu, \sigma^2), \\ G \sim DP(M, G0), \ \ G0 &= N\left(\mu; \mu_0, \kappa \sigma^2\right) Ga\left(\sigma^{-2}; \frac{r_{0,\sigma}}{2}, \frac{s_{0,\sigma}}{2}\right). \end{split}$$

The prior of function without shape restriction is:

$$f(x) = Z(x),$$

where Z is a second-order Gaussian process with mean function equal to zero and covariance function $\nu(s,t)=E[Z(s)Z(t)]$ for $s,t\in[0,1]$. The Gaussian process is expressed with the spectral representation based on cosine basis functions:

$$Z(x) = \sum_{j=0}^{\infty} \theta_j \varphi_j(x)$$

$$\varphi_0(x) = 1$$
 and $\varphi_j(x) = \sqrt{2}\cos(\pi j x), \ j \ge 1, \ 0 \le x \le 1$

The shape-restricted functions are modeled by assuming the qth derivatives of f are squares of Gaussian processes:

$$f^{(q)}(x) = \delta Z^2(x) h(x), \ \delta \in \{1, -1\}, \ q \in \{1, 2\},$$

where h is the squish function. For monotonic, monotonic convex, and concave functions, h(x) = 1, while for S and U shaped functions, h is defined by

$$h(x) = \frac{1 - \exp[\psi(x - \omega)]}{1 + \exp[\psi(x - \omega)]}, \ \psi > 0, \ 0 < \omega < 1$$

For the spectral coefficients of functions without shape constraints, the scale-invariant prior is used (The intercept is included in β):

$$\theta_j | \tau, \gamma \sim N(0, \tau^2 \exp[-j\gamma]), j \ge 1$$

The priors for the spectral coefficients of shape restricted functions are:

$$\theta_0 \sim N(m_{\theta_0}, v_{\theta_0}^2), \quad \theta_j | \tau, \gamma \sim N(m_{\theta_j}, \tau^2 \exp[-j\gamma]), \ j \ge 1$$

To complete the model specification, the popular normal prior is assumed for β :

$$\beta | \sim N(m_{0,\beta}, V_{0,\beta})$$

Value

An object of class beam representing the Bayesian spectral analysis model fit. Generic functions such as print, fitted and plot have methods to show the results of the fit.

The MCMC samples of the parameters in the model are stored in the list mcmc.draws, the posterior samples of the fitted values are stored in the list fit.draws, and the MCMC samples for the log marginal likelihood are saved in the list loglik.draws. The output list also includes the following objects:

post.est posterior estimates for all parameters in the model.

lpml log pseudo marginal likelihood using Mukhopadhyay and Gelfand method.

imodmet the number of times to modify Metropolis.

pmet proportion of θ accepted after burn-in.

call the matched call.

mcmctime running time of Markov chain from system.time().

References

Jo, S., Choi, T., Park, B. and Lenk, P. (2019). bsamGP: An R Package for Bayesian Spectral Analysis Models Using Gaussian Process Priors. *Journal of Statistical Software*, **90**, 310-320.

Lenk, P. and Choi, T. (2017) Bayesian Analysis of Shape-Restricted Functions using Gaussian Process Priors. *Statistica Sinica*, **27**, 43-69.

MacEachern, S. N. and Müller, P. (1998) Estimating mixture of Dirichlet process models. *Journal of Computational and Graphical Statistics*, **7**, 223-238.

Mukhopadhyay, S. and Gelfand, A. E. (1997) Dirichlet process mixed generalized linear models. *Journal of the American Statistical Association*, **92**, 633-639.

Neal, R. M. (2000) Markov chain sampling methods for Dirichlet process mixture models. *Journal of Computational and Graphical Statistics*, **9**, 249-265.

See Also

bsar, bsaqdpm

28 cadmium

Examples

```
## Not run:
########################
# Increasing-convex #
# Simulate data
set.seed(1)
n <- 200
x <- runif(n)
e <- c(rnorm(n/2, sd = 0.5), rnorm(n/2, sd = 3))
y < -exp(6*x - 3) + e
# Number of cosine basis functions
nbasis <- 50
# Fit the model with default priors and mcmc parameters
fout <- bsardpm(y \sim fs(x), nbasis = nbasis, shape = 'IncreasingConvex')
# Summary
print(fout); summary(fout)
# fitted values
fit <- fitted(fout)</pre>
# Plot
plot(fit, ask = TRUE)
## End(Not run)
```

cadmium

Cadmium dose-response meta data

Description

This dataset includes minimal information of NCC-2012 meta data.

Usage

```
data("cadmium")
```

Format

A data frame with 190 observations on the following 5 variables.

```
gender a numeric vector with 1 : Female, 0 : Male, 0.5 : Unknown or both ethnicity a integer vector with 1 : Asian, 2 : Caucasian
```

Elec.demand 29

```
Ucd_GM a numeric vector of Geometric means of urinary cadmium
b2_GM a numeric vector of Geometric means of Beta2-Microglobulin
isOld a logical vector whether the observation is older than 50
```

References

Lee, Minjea, Choi, Taeryon; Kim, Jeongseon; Woo, Hae Dong (2013) Bayesian Analysis of Dose-Effect Relationship of Cadmium for Benchmark Dose Evaluation. *Korean Journal of Applied Statistics*, **26**(3), 453–470.

Examples

```
## Not run:
data(cadmium)
## End(Not run)
```

Elec.demand

Electricity demand data

Description

The Elec.demand data consists of 288 quarterly observations in Ontario from 1971 to 1994.

Usage

```
data(Elec.demand)
```

Format

A data frame with 288 observations on the following 7 variables.

```
quarter date (yyyy-mm) from 1971 to 1994
enerm electricity demand.
gdp gross domestic product.
pelec price of electricity.
pgas price of natural gas.
hddam, the number of heating degree days relations.
```

hddqm the number of heating degree days relative to a reference temperature.

cddqm the number of cooling degree days relative to a reference temperature.

Source

Yatchew, A. (2003). *Semiparametric Regression for the Applied Econometrician*. Cambridge University Press.

30 fitted.blm

References

Engle, R. F., Granger, C. W. J., Rice, J. and Weiss, A. (1986). Semiparametric estimates of the relation between weather and electricity sales. *Journal of the American Statistical Association*, **81**, 310-320.

Lenk, P. and Choi, T. (2017). Bayesian analysis of shape-restricted functions using Gaussian process priors. *Statistica Sinica*, **27**, 43-69.

Examples

```
## Not run:
data(Elec.demand)
plot(Elec.demand)
## End(Not run)
```

fitted.blm

Compute fitted values for a blm object

Description

Computes pointwise posterior means and 95% credible intervals of the fitted Bayesian linear models.

Usage

```
## S3 method for class 'blm'
fitted(object, alpha = 0.05, HPD = TRUE, ...)
```

Arguments

object a bsam object

alpha a numeric scalar in the interval (0,1) giving the $100(1-\alpha)\%$ credible intervals. HPD a logical variable indicating whether the $100(1-\alpha)\%$ Highest Posterior Density

(HPD) intervals are calculated. If HPD=FALSE, the $100(1-\alpha)\%$ equal-tail

credible intervals are calculated. The default is TRUE.

... not used

Details

None.

Value

A list containing posterior means and 95% credible intervals.

The output list includes the following objects:

wbeta posterior estimates for regression function.

yhat posterior estimates for generalised regression function.

fitted.bsad 31

References

Chen, M., Shao, Q. and Ibrahim, J. (2000) *Monte Carlo Methods in Bayesian computation*. Springer-Verlag New York, Inc.

See Also

```
blq, blr, gblr
```

Examples

```
## See examples for blq and blr
```

fitted.bsad

Compute fitted values for a bsad object

Description

Computes pointwise posterior means and $100(1 - \alpha)\%$ credible intervals of the fitted Bayesian spectral analysis density estimation model.

Usage

```
## S3 method for class 'bsad'
fitted(object, alpha = 0.05, HPD = TRUE, ...)
```

Arguments

object a bsad object

alpha a numeric scalar in the interval (0,1) giving the $100(1-\alpha)\%$ credible intervals. HPD a logical variable indicating whether the $100(1-\alpha)\%$ Highest Posterior Density

(HPD) intervals are calculated. If HPD=FALSE, the $100(1-\alpha)\%$ equal-tail

credible intervals are calculated. The default is TRUE.

... not used

Details

None.

Value

A list object of class fitted. bsad containing posterior means and $100(1-\alpha)\%$ credible intervals. Generic function plot displays the results of the fit.

The output list includes the following objects:

fpar posterior estimates for parametric model.
fsemi posterior estimates for semiparametric model.

fsemiMaxKappa posterior estimates for semiparametric model with maximum number of basis.

32 fitted.bsam

See Also

bsad

Examples

```
## See examples for bsad
```

fitted.bsam

Compute fitted values for a bsam object

Description

Computes pointwise posterior means and $100(1 - \alpha)\%$ credible intervals of the fitted Bayesian spectral analysis models.

Usage

```
## S3 method for class 'bsam'
fitted(object, alpha = 0.05, HPD = TRUE, ...)
```

Arguments

object a bsam object a numeric scalar in the interval (0,1) giving the $100(1-\alpha)\%$ credible intervals. HPD a logical variable indicating whether the $100(1-\alpha)\%$ Highest Posterior Density (HPD) intervals are calculated. If HPD=FALSE, the $100(1-\alpha)\%$ equal-tail credible intervals are calculated. The default is TRUE. . . . not used

Details

None.

Value

A list object of class fitted. bsam containing posterior means and $100(1-\alpha)\%$ credible intervals. Generic function plot displays the results of the fit.

The output list includes the following objects:

fxobs posterior estimates for unknown functions over observation.

fxgrid posterior estimates for unknown functions over grid points.

wbeta posterior estimates for parametric part.

yhat posterior estimates for fitted values of response. For gbsar, it gives posterior

estimates for expectation of response.

fitted.bsamdpm 33

See Also

```
bsaq, bsaqdpm, bsar, bsardpm
```

Examples

```
## See examples for bsaq, bsaqdpm, bsar, and bsardpm
```

fitted.bsamdpm

Compute fitted values for a bsamdpm object

Description

Computes pointwise posterior means and $100(1 - \alpha)\%$ credible intervals of the fitted Bayesian spectral analysis models with Dirichlet process mixture error.

Usage

```
## S3 method for class 'bsamdpm'
fitted(object, alpha = 0.05, HPD = TRUE, ...)
```

Arguments

object a bsamdpm object a numeric scalar in the interval (0,1) giving the $100(1-\alpha)\%$ credible intervals. HPD a logical variable indicating whether the $100(1-\alpha)\%$ Highest Posterior Density (HPD) intervals are calculated. If HPD=FALSE, the $100(1-\alpha)\%$ equal-tail credible intervals are calculated. The default is TRUE.

... not used

Details

None.

Value

A list object of class fitted.bsamdpm containing posterior means and 95% credible intervals. Generic function plot displays the results of the fit.

The output list includes the following objects:

edens posterior estimate for unknown error distribution over grid points.

fxobs posterior estimates for unknown functions over observation.

fxgrid posterior estimates for unknown functions over grid points.

wbeta posterior estimates for parametric part.

yhat posterior estimates for fitted values of response.

34 gblr

See Also

bsaqdpm, bsardpm

Examples

```
## See examples for bsaqdpm and bsardpm
```

fs

Specify a Fourier Basis Fit in a BSAM Formula

Description

A symbolic wrapper to indicate a nonparametric term in a formula argument to bsaq, bsaqdpm, bsar, bsardpm, and gbsar.

Usage

fs(x)

Arguments

Х

a vector of the univariate covariate for nonparametric component

Examples

```
## Not run:
# fit x using a Fourier basis
y ~ w + fs(x)
# fit x1 and x2 using a Fourier basis
y ~ fs(x1) + fs(x2)
## End(Not run)
```

gblr

Generalized Bayesian Linear Models

Description

This function fits a Bayesian generalized linear regression model.

Usage

```
gblr(formula, data = NULL, family, link, mcmc = list(), prior = list(),
marginal.likelihood = TRUE, algorithm = c('AM', 'KS'), verbose = FALSE)
```

gblr 35

Arguments

formula an object of class "formula" data an optional data frame.

family a description of the error distribution to be used in the model: The family

contains bernoulli ("bernoulli"), poisson ("poisson"), negative-binomial ("neg-

ative.binomial"), poisson-gamma mixture ("poisson.gamma").

link a description of the link function to be used in the model.

mcmc a list giving the MCMC parameters. The list includes the following integers

(with default values in parentheses): nblow (10000) giving the number of MCMC in transition period, nskip (10) giving the thinning interval, smcmc (1000) giving the number of MCMC for analysis, and ndisp (1000) giving the number of saved draws to be displayed on screen (the function reports on the screen when

every ndisp iterations have been carried out).

prior a list giving the prior information. The list includes the following parameters

(default values specify the non-informative prior): beta_m0 and beta_v0 giving the hyperparameters of the multivariate normal distribution for parametric part including intercept, kappa_m0 and kappa_v0 giving the prior mean and variance of the gammal prior distribution for dispersion parameter (negative-binomial).

marginal.likelihood

a logical variable indicating whether the log marginal likelihood is calculated.

The methods of Gelfand and Dey (1994) is used.

algorithm a description of the algorithm to be used in the fitting of the logistic model:

The algorithm contains the Gibbs sampler based on the Kolmogorov-Smirnov

distribution (KS) and an adaptive Metropolis algorithm (AM).

verbose a logical variable. If TRUE, the iteration number and the Metropolis acceptance

rate are printed to the screen.

Details

This generic function fits a Bayesian generalized linear regression models.

Let y_i and w_i be the response and the vector of parametric predictors, respectively. The model is as follows.

$$y_i | \mu_i \sim F(\mu_i),$$

$$g(\mu_i) = w_i^T \beta, \ i = 1, \dots, n,$$

where $g(\cdot)$ is a link function and $F(\cdot)$ is a distribution of an exponential family.

For unknown coefficients, the following prior is assumed for β :

$$\beta \sim N(m_{0,\beta}, V_{0,\beta})$$

The prior for the dispersion parameter of negative-binomial regression is

$$\kappa \sim Ga(r_0, s_0)$$

36 gblr

Value

An object of class blm representing the generalized Bayesian linear model fit. Generic functions such as print, fitted and plot have methods to show the results of the fit.

The MCMC samples of the parameters in the model are stored in the list mcmc.draws, the posterior samples of the fitted values are stored in the list fit.draws, and the MCMC samples for the log marginal likelihood are saved in the list loglik.draws. The output list also includes the following objects:

post.est posterior estimates for all parameters in the model.

lmarg log marginal likelihood using Gelfand-Dey method.

family the family object used.

link the link object used.

methods the method object used in the logit model.

call the matched call.

mcmctime running time of Markov chain from system. time().

References

Albert, J. H. and Chib, S. (1993) Bayesian Analysis of Binary and Polychotomous Response Data. *Journal of the American Statistical Association*, **88**, 669-679.

Holmes, C. C. and Held, L. (2006) Bayesian Auxiliary Variables Models for Binary and Multinomial Regression. *Bayesian Analysis*, **1**, 145-168.

Gelfand, A. E. and Dey, K. K. (1994) Bayesian Model Choice: Asymptotics and Exact Calculations. *Journal of the Royal Statistical Society. Series B - Statistical Methodology*, **56**, 501-514.

Roberts, G. O. and Rosenthal, J. S. (2009) Examples of Adaptive MCMC. *Journal of Computational and Graphical Statistics*, **18**, 349-367.

See Also

blr, blq

Examples

```
# Summary
print(fout); summary(fout)
# Plot
plot(fout)
# fitted values
fitf <- fitted(fout)</pre>
```

gbsar

Bayesian Shape-Restricted Spectral Analysis for Generalized Partial Linear Models

Description

This function fits a Bayesian generalized partial linear regression model to estimate shape-restricted functions using a spectral analysis of Gaussian process priors.

Usage

Arguments

Suments	
formula	an object of class "formula"
xmin	a vector or scalar giving user-specific minimum values of \mathbf{x} . The default values are minimum values of \mathbf{x} .
xmax	a vector or scalar giving user-specific maximum values of \mathbf{x} . The default values are maximum values of \mathbf{x} .
family	a description of the error distribution to be used in the model: The family contains bernoulli ("bernoulli"), poisson ("poisson"), negative-binomial ("negative.binomial"), poisson-gamma mixture ("poisson.gamma").
link	a description of the link function to be used in the model.
nbasis	number of cosine basis functions.
nint	number of grid points where the unknown function is evaluated for plotting. The default is 200.
mcmc	a list giving the MCMC parameters. The list includes the following integers (with default values in parentheses): nblow0 (1000) giving the number of initialization period for adaptive metropolis, maxmodmet (5) giving the maximum number of times to modify metropolis, nblow (10000) giving the number of MCMC in transition period, nskip (10) giving the thinning interval, smcmc (1000) giving the number of MCMC for analysis, and ndisp (1000) giving

the number of saved draws to be displayed on screen (the function reports on the screen when every ndisp iterations have been carried out).

prior

a list giving the prior information. The list includes the following parameters (default values specify the non-informative prior): if lagprior choosing a smoothing prior for spectral coefficients (iflagprior=0 assigns T-Smoother prior (default), iflagprior=1 chooses Lasso-Smoother prior), theta_m0, theta0_m0 and theta0_s0 giving the hyperparameters for prior distribution of the spectral coefficients (theta0_m0 and theta0_s0 are used when the functions have shape-restriction), tau2_m0, tau2_s0 and w0 giving the prior mean and standard deviation of smoothing prior (When iflagprior=1, tau2_m0 is only used as the hyperparameter), beta_m0 and beta_v0 giving the hyperparameters of the multivariate normal distribution for parametric part including intercept, alpha_m0 and alpha_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the constant of integration, iflagpsi determining the prior of slope for logisitic function in S or U shaped (iflagpsi=1 (default), slope ψ is sampled and iflagpsi=0, ψ is fixed), psifixed giving initial value (iflagpsi=1) or fixed value (iflagpsi=0) of slope, omega_m0 and omega_s0 giving the prior mean and standard deviation of the truncated normal prior distribution for the inflection point of S or U shaped function, kappa_m0 and kappa_v0 giving the prior mean and variance of the gammal prior distribution for dispersion parameter (negative-binomial).

shape

a vector giving types of shape restriction.

marginal.likelihood

a logical variable indicating whether the log marginal likelihood is calculated. The methods of Gelfand and Dey (1994) and Newton and Raftery (1994) are used.

algorithm

a description of the algorithm to be used in the fitting of the logistic model: The algorithm contains the Gibbs sampler based on the Kolmogorov-Smirnov distribution (KS) and an adaptive Metropolis algorithm (AM).

verbose

a logical variable. If TRUE, the iteration number and the Metropolis acceptance rate are printed to the screen.

Details

This generic function fits a Bayesian generalized partial linear regression models for estimating shape-restricted functions using Gaussian process priors. For enforcing shape-restrictions, they assumed that the derivatives of the functions are squares of Gaussian processes.

Let y_i and w_i be the response and the vector of parametric predictors, respectively. Further, let $x_{i,k}$ be the covariate related to the response through an unknown shape-restricted function. The model for estimating shape-restricted functions is as follows.

$$y_i | \mu_i \sim F(\mu_i),$$
 $g(\mu_i) = w_i^T \beta + \sum_{k=1}^K f_k(x_{i,k}), \ i = 1, \dots, n,$

where $g(\cdot)$ is a link function and f_k is an unknown nonlinear function of the scalar $x_{i,k} \in [0,1]$.

The prior of function without shape restriction is:

$$f(x) = Z(x),$$

where Z is a second-order Gaussian process with mean function equal to zero and covariance function $\nu(s,t)=E[Z(s)Z(t)]$ for $s,t\in[0,1]$. The Gaussian process is expressed with the spectral representation based on cosine basis functions:

$$Z(x) = \sum_{j=0}^{\infty} \theta_j \varphi_j(x)$$

$$\varphi_0(x) = 1$$
 and $\varphi_j(x) = \sqrt{2}\cos(\pi j x), j \ge 1, 0 \le x \le 1$

The shape-restricted functions are modeled by assuming the qth derivatives of f are squares of Gaussian processes:

$$f^{(q)}(x) = \delta Z^2(x)h(x), \ \delta \in \{1, -1\}, \ q \in \{1, 2\},$$

where h is the squish function. For monotonic, monotonic convex, and concave functions, h(x) = 1, while for S and U shaped functions, h is defined by

$$h(x) = \frac{1 - \exp[\psi(x - \omega)]}{1 + \exp[\psi(x - \omega)]}, \quad \psi > 0, \quad 0 < \omega < 1$$

For the spectral coefficients of functions without shape constraints, the following prior is used (The intercept is included in β):

$$\theta_j | \tau, \gamma \sim N(0, \tau^2 \exp[-j\gamma]), j \ge 1$$

The priors for the spectral coefficients of shape restricted functions are:

$$|\theta_0| \sim N(m_{\theta_0}, v_{\theta_0}^2), \quad \theta_j | \tau, \gamma \sim N(m_{\theta_j}, \tau^2 \exp[-j\gamma]), \ j \ge 1$$

To complete the model specification, the following prior is assumed for β :

$$\beta | \sim N(m_{0,\beta}, V_{0,\beta})$$

Value

An object of class beam representing the Bayesian spectral analysis model fit. Generic functions such as print, fitted and plot have methods to show the results of the fit.

The MCMC samples of the parameters in the model are stored in the list mcmc.draws, the posterior samples of the fitted values are stored in the list fit.draws, and the MCMC samples for the log marginal likelihood are saved in the list loglik.draws. The output list also includes the following objects:

post.est posterior estimates for all parameters in the model.

lmarg.gd log marginal likelihood using Gelfand-Dey method.

lmarg.nr log marginal likelihood using Netwon-Raftery method, which is biased.

family the family object used.
link the link object used.
call the matched call.

mcmctime running time of Markov chain from system.time().

References

Jo, S., Choi, T., Park, B. and Lenk, P. (2019). bsamGP: An R Package for Bayesian Spectral Analysis Models Using Gaussian Process Priors. *Journal of Statistical Software*, **90**, 310-320.

Lenk, P. and Choi, T. (2017) Bayesian Analysis of Shape-Restricted Functions using Gaussian Process Priors. *Statistica Sinica*, **27**, 43-69.

Roberts, G. O. and Rosenthal, J. S. (2009) Examples of Adaptive MCMC. *Journal of Computational and Graphical Statistics*, **18**, 349-367.

Holmes, C. C. and Held, L. (2006) Bayesian Auxiliary Variables Models for Binary and Multinomial Regression. *Bayesian Analysis*, **1**, 145-168.

Gelfand, A. E. and Dey, K. K. (1994) Bayesian model choice: asymptotics and exact calculations. *Journal of the Royal Statistical Society. Series B - Statistical Methodology*, **56**, 501-514.

Newton, M. A. and Raftery, A. E. (1994) Approximate Bayesian inference with the weighted likelihood bootstrap (with discussion). *Journal of the Royal Statistical Society. Series B - Statistical Methodology*, **56**, 3-48.

Albert, J. H. and Chib, S. (1993) Bayesian Analysis of Binary and Polychotomous Response Data. *Journal of the American Statistical Association*, **88**, 669-679.

See Also

bsaq, bsar

```
## Not run:
################################
# Probit Regression Model #
###############################
# Simulate data
set.seed(1)
f \leftarrow function(x) 1.5 * sin(pi * x)
n <- 1000
b < -c(1,-1)
rho <- 0.7
u \leftarrow runif(n, min = -1, max = 1)
x <- runif(n, min = -1, max = 1)
w1 \leftarrow runif(n, min = -1, max = 1)
w2 < - round(f(rho * x + (1 - rho) * u))
w \leftarrow cbind(w1, w2)
y < - w %*% b + f(x) + rnorm(n)
y < - (y > 0)
# Number of cosine basis functions
nbasis <- 50
# Fit the model with default priors and mcmc parameters
```

intgrat 41

```
fout <- gbsar(y ~ w1 + w2 + fs(x), family = "bernoulli", link = "probit",
             nbasis = nbasis, shape = 'Free')
# Summary
print(fout); summary(fout)
# fitted values
fit <- fitted(fout)</pre>
# Plot
plot(fit, ask = TRUE)
# Logistic Additive Regression Model #
# Wage-Union data
data(wage.union); attach(wage.union)
race[race==1 | race==2]=0
race[race==3]=1
y <- union
w <- cbind(race,sex,south)</pre>
x <- cbind(wage,education,age)</pre>
# mcmc parameters
mcmc \leftarrow list(nblow0 = 10000,
            nblow = 10000,
            nskip = 10,
            smcmc = 1000,
            ndisp = 1000,
            maxmodmet = 10)
foutGBSAR \leftarrow gbsar(y \sim race + sex + south + fs(wage) + fs(education) + fs(age),
                  family = 'bernoulli', link = 'logit', nbasis = 50, mcmc = mcmc,
                  shape = c('Free','Decreasing','Increasing'))
# fitted values
fitGBSAR <- fitted(foutGBSAR)</pre>
# Plot
plot(fitGBSAR, ask = TRUE)
## End(Not run)
```

42 intsim

Description

Trapezoidal rule is a technique for approximating the definite integral.

Usage

```
intgrat(f, delta)
```

Arguments

f Function values to be integrated.

delta Spacing size.

Value

intgrat returns the value of the intergral.

 ${\tt intsim}$

Numerical integration using Simpson's rule

Description

Simpson's rule is a method for numerical integration.

Usage

```
intsim(f, delta)
```

Arguments

f Function values to be integrated.

delta Spacing size.

Value

intsim returns the value of the intergral.

London.Mortality 43

London.Mortality

Daily Moratlity in London

Description

The London.Mortality data consists of daily death occurrences from Jan. 1st, 1993 to Dec. 31st, 2006 and corresponding weather observations including temperature and humidity in London.

Usage

```
data(London.Mortality)
```

Format

A data frame with 5113 observations on the following 7 variables.

date date in YYYY-MM-DD.

tmean Mean temperature.

tmin Minimum dry-bulb temperature.

tmax Maximum dry-bulb temperature.

dewp Dew point.

rh Relative humidity.

death the number of death occurences.

Source

Office for National Statistics

British Atmospheric Data Centre

https://github.com/gasparrini/2015_gasparrini_Lancet_Rcodedata

References

Armstrong BG, Chalabi Z, Fenn B, Hajat S, Kovats S, Milojevic A, Wilkinson P (2011). Association of mortality with high temperatures in a temperate climate: England and Wales. *Journal of Epidemiology & Community Health*, **65**(4), 340–345.

Gasparrini A, Armstrong B, Kovats S, Wilkinson P (2012). The effect of high temperatures on cause-specific mortality in England and Wales. *Occupational and Environmental Medicine*, **69**(1), 56–61.

Gasparrini A, Guo Y, Hashizume M, Lavigne E, Zanobetti A, Schwartz J, Tobias A, Tong S, Rocklöv J, Forsberg B, et al.(2015). Mortality risk attributable to high and low ambient temperature: a multicountry observational study. *The Lancet*, **386**(9991), 369-375.

44 plasma

Examples

```
## Not run:
data(London.Mortality)
## End(Not run)
```

plasma

A Data Set for Plasma Levels of Retinol and Beta-Carotene

Description

This data set contains 314 observations on 14 variables.

Usage

```
data(plasma)
```

Format

```
age Age (years).
sex Sex (1=Male, 2=Female).
smoke Smoking status (1=Never, 2=Former, 3=Current Smoker).
vmi BMI values (weight/(height^2)).
vitas Vitamin use (1=Yes,fairly often, 2=Yes, not often, 3=No).
calories Number of calories consumed per day.
fat Grams of fat consumed per day.
fiber Grams of fiber consumed per day.
alcohol Number of alcoholic drinks consumed per week.
cholesterol Cholesterol consumed (mg per day).
beta diet Dietary beta-carotene consumed (mcg per day).
reedit Dietary retinol consumed (mcg per day).
betaplasma Plasma beta-carotene (ng/ml).
retplasma Plasma Retinol (ng/ml).
```

Source

```
https://lib.stat.cmu.edu/datasets/Plasma_Retinol
```

References

Nierenberg, D. W., Stukel, T. A., Baron, J. A., Dain, B. J., and Greenberg, E. R. (1989). Determinants of plasma levels of beta-carotene and retinol. *American Journal of Epidemiology*, **130**, 511-521.

Meyer, M. C., Hackstadt, A. J., and Hoeting, J. A. (2011). Bayesian estimation and inference for generalized partial linear models using shape-restricted splines. *Journal of Nonparametric Statistics*, **23**(4), 867-884.

plot.blm 45

Examples

```
## Not run:
data(plasma)
## End(Not run)
```

plot.blm

Plot a blm object

Description

Plots the posterior samples for Bayesian linear models

Usage

```
## S3 method for class 'blm' plot(x, ...)
```

Arguments

x a blm object

. . . other options to pass to the plotting functions

Value

Returns a plot.

See Also

```
blq, blr
```

```
## See examples for blq and blr
```

46 plot.bsam

plot.bsad

Plot a bsad object

Description

Plots the posterior samples for Bayesian semiparametric density estimation using a logistic Gaussian process.

Usage

```
## S3 method for class 'bsad' plot(x, ...)
```

Arguments

x a bsad object

... other options to pass to the plotting functions

Value

Returns a plot.

See Also

bsad

Examples

```
## See examples for bsad
```

plot.bsam

Plot a bsam object

Description

Plots the posterior samples for Bayesian spectral analysis models.

Usage

```
## S3 method for class 'bsam' plot(x, ...)
```

Arguments

x a bsam object

... other options to pass to the plotting functions

plot.bsamdpm 47

Value

Returns a plot.

See Also

```
bsaq, bsaqdpm, bsar, bsardpm
```

Examples

```
## See examples for bsaq, bsaqdpm, bsar, and bsardpm
```

plot.bsamdpm

Plot a bsamdpm object

Description

Plots the posterior samples for Bayesian spectral analysis models with Dirichlet process mixture error.

Usage

```
## S3 method for class 'bsamdpm' plot(x, ...)
```

Arguments

x a bsamdpm object

... other options to pass to the plotting functions

Value

Returns a plot.

See Also

bsaqdpm, bsardpm

```
## See examples for bsaqdpm and bsardpm
```

48 plot.fitted.bsam

plot.fitted.bsad

Plot a fitted.bsad object

Description

Plots the predictive density for Bayesian density estimation model using logistic Gaussian process

Usage

```
## S3 method for class 'fitted.bsad'
plot(x, ggplot2, legend.position, nbins, ...)
```

Arguments

x a fitted.bsad object

ggplot2 a logical variable. If TRUE the ggplot2 package is used.

legend.position

the position of legends ("none", "left", "right", "bottom", "top"). It is used when

ggplot2 = TRUE.

nbins Number of bins used. Default is 30.

... other options to pass to the plotting functions

Value

Returns a plot.

See Also

```
bsad, fitted.bsad
```

Examples

```
## See example for bsad
```

plot.fitted.bsam

Plot a fitted.bsam object

Description

Plots the data and the fit for Bayesian spectral analysis models.

Usage

```
## S3 method for class 'fitted.bsam'
plot(x, type, ask, ggplot2, legend.position, ...)
```

plot.fitted.bsamdpm 49

Arguments

x a fitted.bsam object

type the type of fitted plot. The default is on the scale of the response variable type="response";

the alternative type="term" is on the scale of the nonparametric predictor. Note that this affects only on glm type models. For example, binomial model with the

default option gives the predicted probabilites.

ask see. par

ggplot2 a logical variable. If TRUE the ggplot2 package is used.

legend.position

the position of legends ("none", "left", "right", "bottom", "top"). It is used when

ggplot2 = TRUE.

... other options to pass to the plotting functions

Value

Returns a plot.

See Also

```
bsaq, bsaqdpm, bsar, bsardpm, fitted.bsam
```

Examples

```
## See examples for bsaq, bsaqdpm, bsar, and bsardpm
```

Description

Plots the data and the fit for Bayesian spectral analysis models with Dirichlet process mixture error.

Usage

```
## S3 method for class 'fitted.bsamdpm'
plot(x, ask, ggplot2, legend.position, ...)
```

Arguments

```
x a fitted.bsamdpm object
```

ask see. par

ggplot2 a logical variable. If TRUE the ggplot2 package is used.

legend.position

the position of legends ("none", "left", "right", "bottom", "top"). It is used when

ggplot2 = TRUE.

... other options to pass to the plotting functions

50 predict.blm

Value

Returns a plot.

See Also

```
bsaqdpm, bsardpm, fitted.bsamdpm
```

Examples

```
## See examples for bsaqdpm and bsardpm
```

predict.blm

Predict method for a blm object

Description

Computes predicted values of Bayesian linear models.

Usage

```
## S3 method for class 'blm'
predict(object, newdata, alpha = 0.05, HPD = TRUE, ...)
```

Arguments

object a bsam object

newdata an optional data matrix or vector with which to predict. If omitted, the fitted

values are returned.

alpha a numeric scalar in the interval (0,1) giving the $100(1-\alpha)\%$ credible intervals.

HPD a logical variable indicating whether the $100(1-\alpha)\%$ Highest Posterior Density

(HPD) intervals are calculated. If HPD=FALSE, the $100(1-\alpha)\%$ equal-tail

credible intervals are calculated. The default is TRUE.

... not used

Details

None.

Value

A list containing posterior means and 95% credible intervals.

The output list includes the following objects:

wbeta posterior estimates for regression function.

yhat posterior estimates for generalised regression function.

predict.bsam 51

References

Chen, M., Shao, Q. and Ibrahim, J. (2000) *Monte Carlo Methods in Bayesian computation*. Springer-Verlag New York, Inc.

See Also

```
blq, blr, gblr
```

Examples

predict.bsam

Predict method for a bsam object

Description

Computes the predicted values of Bayesian spectral analysis models.

Usage

```
## S3 method for class 'bsam'
predict(object, newp, newnp, alpha = 0.05, HPD = TRUE, type = "response", ...)
```

Arguments

object a bsam object

newp an optional data of parametric components with which to predict. If omitted, the

fitted values are returned.

52 predict.bsam

newnp	an optional data of nonparametric components with which to predict. If omitted, the fitted values are returned.
alpha	a numeric scalar in the interval (0,1) giving the $100(1-\alpha)\%$ credible intervals.
HPD	a logical variable indicating whether the $100(1-\alpha)\%$ Highest Posterior Density (HPD) intervals are calculated. If HPD=FALSE, the $100(1-\alpha)\%$ equal-tail credible intervals are calculated. The default is TRUE.
type	the type of prediction required. type = "response" gives the posterior predictive samples as default. The "mean" option returns expectation of the posterior estimates.
	not used

Details

None.

Value

A list object of class predict . bsam containing posterior means and $100(1-\alpha)\%$ credible intervals. The output list includes the following objects:

fxobs posterior estimates for unknown functions over observation.

wbeta posterior estimates for parametric part.

yhat posterior estimates for fitted values of either response or expectation of response.

For gbsar, it gives posterior estimates for expectation of response.

fxResid posterior estimates for fitted parametric residuals. Not applicable for gbsar.

See Also

```
bsaq, bsar, gbsar
```

predict.bsamdpm 53

predict.bsamdpm

Predict method for a bsamdpm object

Description

Computes the predicted values of Bayesian spectral analysis models with Dirichlet process mixture errors.

Usage

```
## S3 method for class 'bsamdpm'
predict(object, newp, newnp, alpha = 0.05, HPD = TRUE, ...)
```

Arguments

object	a bsamdpm object
newp	an optional data of parametric components with which to predict. If omitted, the fitted values are returned.
newnp	an optional data of nonparametric components with which to predict. If omitted, the fitted values are returned.
alpha	a numeric scalar in the interval (0,1) giving the $100(1-\alpha)\%$ credible intervals.
HPD	a logical variable indicating whether the $100(1-\alpha)\%$ Highest Posterior Density (HPD) intervals are calculated. If HPD=FALSE, the $100(1-\alpha)\%$ equal-tail credible intervals are calculated. The default is TRUE.
	not used

Details

None.

54 rald

Value

A list object of class predict.bsamdpm containing posterior means and $100(1-\alpha)\%$ credible intervals.

The output list includes the following objects:

fxobs posterior estimates for unknown functions over observation.

wbeta posterior estimates for parametric part.

yhat posterior estimates for fitted values of response.

See Also

bsaqdpm, bsardpm

Examples

```
## Not run:
# Increasing-convex #
######################
# Simulate data
set.seed(1)
n <- 200
x <- runif(n)
e <- c(rnorm(n/2, sd = 0.5), rnorm(n/2, sd = 3))
y < -exp(6*x - 3) + e
# Number of cosine basis functions
nbasis <- 50
# Fit the model with default priors and mcmc parameters
fout \leftarrow bsardpm(y \sim fs(x), nbasis = nbasis, shape = 'IncreasingConvex')
# Prediction
xnew <- runif(n)</pre>
predict(fout, newnp = xnew)
## End(Not run)
```

rald

The asymmetric Laplace distribution

Description

Density for and random values from a three-parameter asymmetric Laplace distribution.

traffic 55

Usage

Arguments

n Number of random values to be generated.

location Location parameter.

scale Scale parameter.

p Skewness parameter.

Details

This generic function generates a random variable from an asymmetric Laplace distribution (ALD). The ALD has the following probability density function:

$$ALD_p(x; \mu, \sigma) = \frac{p(1-p)}{\sigma} \exp\Big(-\frac{(x-\mu)[p-I(x \le \mu)]}{\sigma}\Big),$$

where $0 is the skew parameter, <math>\sigma > 0$ is the scale parameter, $-\infty < \mu < \infty$ is the location parameter, and $I(\cdot)$ is the indication function. The range of x is $(-\infty, \infty)$.

Value

rald gives out a vector of random numbers generated by the asymmetric Laplace distribution.

References

Koenker, R. and Machado, J. (1999). Goodness of fit and related inference processes for quantile regression. *Journal of the American Statistical Association*, **94**(3), 1296-1309.

Yu, K. and Zhang, J. (2005). A Three-parameter asymmetric Laplace distribution and its extension. *Communications in Statistics - Theory and Methods*, **34**, 1867-1879.

traffic

Monthly traffic accidents data

Description

This data set contains 108 observations on 6 variables.

Usage

data(traffic)

56 wage.union

Format

```
ln_number logarithm of the number of monthly automobile accidents in the state of Michigan.
month months from January 1st, 1979 to Decembe 31st, 1987.
ln_unemp logarithm of unemployment rate
spring indicator for spring season.
summer indicator for summer season.
fall indicator for fall season.
```

References

Lenk (1999) Bayesian inference for semiparametric regression using a Fourier representation. *Journal of the Royal Statistical Society: Series B*, **61**(4), 863-879.

Examples

```
## Not run:
data(traffic)
pairs(traffic)
## End(Not run)
```

wage.union

Wage-Union data

Description

This data set contains 534 observations on 11 variables.

Usage

```
data(wage.union)
```

Format

```
education number of years of education.

south indicator of living in southern region of U.S.A.

sex gender indicator: 0=male,1=female.

experience number of years of work experience.

union indicator of trade union membership: 0=non-member, 1=member.

wage wages in dollars per hour.

age age in years.

race 1=black, 2=Hispanic, 3=white.

occupation 1=management, 2=sales, 3=clerical, 4=service, 5=professional, 6=other.

sector 0=other, 1=manufacturing, 2=construction.

married indicator of being married: 0=unmarried, 1=married.
```

wage.union 57

References

Berndt, E.R. (1991) *The Practice of Econometrics*. New York: Addison-Wesley. Ruppert, D., Wand, M.P. and Carroll, R.J. (2003) *Semiparametric Regression*. Cambridge University Press.

```
## Not run:
data(wage.union)
pairs(wage.union)
## End(Not run)
```

Index

* Big Data	blq, 2
bsarBig, 22	* shape-restricted partial linear regression
* Dirichlet processes	gbsar, 37
bsaqdpm, 13	* shape-restricted quantile regression
bsardpm, 24	bsaq, 9
* Gaussian processes	bsaqdpm, 13
bsaq, 9	* shape-restricted regression
bsaqdpm, 13	bsar, 17
bsar, 17	bsardpm, 24
bsarBig, 22	
bsardpm, 24	blq, 2, 6, 31, 36, 45, 51
gbsar, 37	blr, 4, 4, 31, 36, 45, 51
* datasets	bsad, 6, <i>32</i> , <i>46</i> , <i>48</i>
cadmium, 28	bsaq, 9, 16, 33, 40, 47, 49, 52
Elec.demand, 29	bsaqdpm, 13, 27, 33, 34, 47, 49, 50, 54
London.Mortality, 43	bsar, 12, 17, 23, 27, 33, 40, 47, 49, 52
plasma, 44	bsarBig, 22
traffic, 55	bsardpm, 16, 20, 24, 33, 34, 47, 49, 50, 54
wage.union, 56	during 20
* density estimation	cadmium, 28
bsad, 6	Elec.demand, 29
fitted.bsad, 31	Lice. delilaria, 29
* distribution	fitted.blm, 30
rald, 54	fitted.bsad, 31, 48
* generalized linear model	fitted.bsam, 32, 49
gblr, 34	fitted.bsamdpm, 33, 50
* integration	formula, 3, 5, 9, 14, 18, 22, 24, 35, 37
intgrat, 41	fs, 34
intsim, 42	
* linear regression model	gblr, 4, 6, 31, 34, 51
blr, 4	gbsar, <i>12</i> , <i>32</i> , <i>37</i> , <i>52</i>
* logistic Gaussian process	
bsad, 6	intgrat, 41
fitted.bsad, 31	intsim, 42
* parametric model	London.Mortality, 43
blq, 2	Edition. Flor tallity, 43
blr, 4	par, <i>49</i>
gblr, 34	plasma, 44
* quantile regression model	plot.blm, 45
1	h=====================================

INDEX 59

```
plot.bsad, 46
plot.bsam, 46
plot.bsamdpm, 47
plot.fitted.bsad, 48
plot.fitted.bsam, 48
plot.fitted.bsamdpm, 49
predict.blm, 50
predict.bsam, 51
predict.bsamdpm, 53
rald, 54
traffic, 55
wage.union, 56
```