## Package 'causalBatch'

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Type Package

Title Causal Batch Effects

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Maintainer Eric W. Bridgeford <ericwb95@gmail.com>

Description Software which provides numerous functionalities for detecting and removing grouplevel effects from high-dimensional scientific data which, when combined with additional assumptions, allow for causal conclusions, as-described in our manuscripts Bridgeford et al. (2024) <doi:10.1101/2021.09.03.458920> and Bridgeford et al. (2023) <arXiv:2307.13868>. Also provides a number of useful utilities for generating simulations and balancing covariates across multiple groups/batches of data via matching and propensity trimming for more than two groups.

**Depends** R (>= 4.2.0)

#### biocViews

Imports cdcsis, sva, MatchIt, nnet, dplyr, magrittr

URL https://github.com/neurodata/causal\_batch

**Encoding** UTF-8

VignetteBuilder knitr

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Author Eric W. Bridgeford [aut, cre], Michael Powell [ctb], Brian Caffo [ctb], Joshua T. Vogelstein [ctb]

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cb.align.kway\_match K-Way matching

## Description

A function for performing k-way matching using the matchIt package. Looks for samples which have corresponding matches across all other treatment levels.

#### Usage

```
cb.align.kway_match(
   Ts,
   Xs,
   match.form,
   reference = NULL,
   match.args = list(method = "nearest", exact = NULL, replace = FALSE, caliper = 0.1),
   retain.ratio = 0.05
)
```

Ts	[n] the labels of the samples, with $K < n$ levels, as a factor variable.
Xs	[n, r] the r covariates/confounding variables, for each of the n samples, as a data frame with named columns.
match.form	A formula of columns from Xs, to be passed directly to matchit for subsequent matching. See formula argument from matchit for details.
reference	the name of the reference/control batch, against which to match. Defaults to NULL, which treats the reference batch as the smallest batch.

match.args	A named list arguments for the matchit function, to be used to specify specific
	matching strategies, where the list names are arguments and the corresponding
	values the value to be passed to matchit. Defaults to inexact nearest-neighbor
	caliper (width 0.1) matching without replacement.
retain.ratio	If the number of samples retained is less than retain.ratio*n, throws a warn- ing. Defaults to 0.05.

an [m] vector consisting of the sample ids of the n original samples that were retained after matching.

#### Details

For more details see the help vignette: vignette("causal\_balancing", package = "causalBatch")

#### Author(s)

Eric W. Bridgeford

#### References

Eric W. Bridgeford, et al. "A Causal Perspective for Batch Effects: When is no answer better than a wrong answer?" Biorxiv (2024).

Daniel E. Ho, et al. "MatchIt: Nonparametric Preprocessing for Parametric Causal Inference" JSS (2011).

#### Examples

```
library(causalBatch)
sim <- cb.sims.sim_linear(a=-1, n=100, err=1/8, unbalancedness=1.5)
cb.align.kway_match(sim$Ts, data.frame(Covar=sim$Xs), "Covar")</pre>
```

cb.align.vm\_trim Vector Matching

#### Description

A function for implementing the vector matching procedure, a pre-processing step for causal conditional distance correlation. Uses propensity scores to strategically include/exclude samples from subsequent inference, based on whether (or not) there are samples with similar propensity scores across all treatment levels (conceptually, a k-way "propensity trimming"). It is imperative that this function is used in conjunction with domain expertise to ensure that the covariates are not colliders, and that the system satisfies the strong ignorability condiiton to derive causal conclusions.

#### Usage

```
cb.align.vm_trim(Ts, Xs, retain.ratio = 0.05, ddx = FALSE)
```

#### Arguments

Ts	[n] the labels of the samples, with $K < n$ levels, as a factor variable.
Xs	[n, r] the r covariates/confounding variables, for each of the n samples.
retain.ratio	If the number of samples retained is less than retain.ratio*n, throws a warn- ing. Defaults to 0.05.
ddx	whether to show additional diagnosis messages. Defaults to FALSE. Can help with debugging if unexpected results are obtained.

#### Value

a [m] vector containing the indices of samples retained after vector matching.

#### Details

For more details see the help vignette: vignette("causal\_balancing", package = "causalBatch")

#### Author(s)

Eric W. Bridgeford

#### References

Michael J. Lopez, et al. "Estimation of Causal Effects with Multiple Treatments" Statistical Science (2017). ran

#### Examples

```
library(causalBatch)
sim <- cb.sims.sim_linear(a=-1, n=100, err=1/8, unbalancedness=3)
cb.align.vm_trim(sim$Ts, sim$Xs)</pre>
```

cb.correct.caus\_cComBat

Causal Conditional ComBat

#### Description

A function for implementing the causal conditional ComBat (causal cComBat) algorithm. This algorithm allows users to remove batch effects (in each dimension), while adjusting for known confounding variables. It is imperative that this function is used in conjunction with domain expertise (e.g., to ensure that the covariates are not colliders, and that the system satisfies the strong ignorability condiiton) to derive causal conclusions. See citation for more details as to the conditions under which conclusions derived are causal.

## Usage

```
cb.correct.caus_cComBat(
    Ys,
    Ts,
    Xs,
    match.form,
    reference = NULL,
    match.args = list(method = "nearest", exact = NULL, replace = FALSE, caliper = 0.1),
    retain.ratio = 0.05
)
```

#### Arguments

Ys	an [n, d] matrix, for the outcome variables with n samples in d dimensions.
Ts	[n] the labels of the samples, with $K < n$ levels, as a factor variable.
Xs	[n, r] the r covariates/confounding variables, for each of the n samples, as a data frame with named columns.
match.form	A formula of columns from Xs, to be passed directly to matchit for subsequent matching. See formula argument from matchit for details.
reference	the name of the reference/control batch, against which to match. Defaults to NULL, which treats the reference batch as the smallest batch.
match.args	A named list arguments for the matchit function, to be used to specify specific matching strategies, where the list names are arguments and the corresponding values the value to be passed to matchit. Defaults to inexact nearest-neighbor caliper (width 0.1) matching without replacement.
retain.ratio	If the number of samples retained is less than retain.ratio*n, throws a warn- ing. Defaults to 0.05.

#### Value

a list, containing the following:

- Ys. corrected an [m, d] matrix, for the m retained samples in d dimensions, after correction.
- Ts [m] the labels of the m retained samples, with K < n levels.
- Xs the r covariates/confounding variables for each of the m retained samples.
- Retained.Ids a [m] vector consisting of the sample ids of the n original samples that were retained after matching.

#### Details

For more details see the help vignette: vignette("causal\_ccombat", package = "causalBatch")

#### Author(s)

Eric W. Bridgeford

#### References

Eric W. Bridgeford, et al. "A Causal Perspective for Batch Effects: When is no answer better than a wrong answer?" Biorxiv (2024).

Daniel E. Ho, et al. "MatchIt: Nonparametric Preprocessing for Parametric Causal Inference" JSS (2011).

W Evan Johnson, et al. "Adjusting batch effects in microarray expression data using empirical Bayes methods" Biostatistics (2007).

#### Examples

```
library(causalBatch)
sim <- cb.sims.sim_linear(a=-1, n=100, err=1/8, unbalancedness=3)
cb.correct.caus_cComBat(sim$Ys, sim$Ts, data.frame(Covar=sim$Xs), "Covar")</pre>
```

cb.detect.caus\_cdcorr Causal Conditional Distance Correlation

#### Description

A function for implementing the causal conditional distance correlation (causal cDCorr) algorithm. This algorithm allows users to identify whether a treatment causes changes in an outcome, given assorted covariates/confounding variables. It is imperative that this function is used in conjunction with domain expertise (e.g., to ensure that the covariates are not colliders, and that the system satisfies the strong ignorability condiiton) to derive causal conclusions. See citation for more details as to the conditions under which conclusions derived are causal.

#### Usage

```
cb.detect.caus_cdcorr(
   Ys,
   Ts,
   Xs,
   R = 1000,
   dist.method = "euclidean",
   distance = FALSE,
   seed = 1,
   num.threads = 1,
   retain.ratio = 0.05,
   ddx = FALSE
)
```

## Arguments Ys

Either:

• [n, d] matrix the outcome variables with n samples in d dimensions. In this case, distance should be FALSE.

	• [n, n] dist object a distance object for the n samples. In this case, distance should be TRUE.
Ts	[n] the labels of the samples, with K < n levels, as a factor variable.
Xs	[n, r] the r covariates/confounding variables, for each of the n samples.
R	the number of repetitions for permutation testing. Defaults to 1000.
dist.method	the method used for computing distance matrices. Defaults to "euclidean". Other options can be identified by seeing the appropriate documention for the method argument for the dist function.
distance	a boolean for whether (or not) Ys are already distance matrices. Defaults to FALSE, which will use dist.method parameter to compute an [n, n] pairwise distance matrix for Ys.
seed	a random seed to set. Defaults to 1.
num.threads	The number of threads for parallel processing (if desired). Defaults to 1.
retain.ratio	If the number of samples retained is less than retain.ratio*n, throws a warn- ing. Defaults to 0.05.
ddx	whether to show additional diagnosis messages. Defaults to FALSE. Can help with debugging if unexpected results are obtained.

a list, containing the following:

- Test The outcome of the statistical test, from cdcov.test.
- Retained. Ids The sample indices retained after vertex matching, which correspond to the samples for which statistical inference is performed.

#### Details

For more details see the help vignette: vignette("causal\_cdcorr", package = "causalBatch")

#### Author(s)

Eric W. Bridgeford

#### References

Eric W. Bridgeford, et al. "A Causal Perspective for Batch Effects: When is no answer better than a wrong answer?" Biorxiv (2024).

Eric W. Bridgeford, et al. "Learning sources of variability from high-dimensional observational studies" arXiv (2023).

Xueqin Wang, et al. "Conditional Distance Correlation" American Statistical Association (2015).

#### Examples

```
library(causalBatch)
sim <- cb.sims.sim_linear(a=-1, n=100, err=1/8, unbalancedness=3)
cb.detect.caus_cdcorr(sim$Ys, sim$Ts, sim$Xs)</pre>
```

cb.sims.covar\_generator

Covariate generator function

#### Description

Covariate generator function

#### Usage

cb.sims.covar\_generator(batches, a1, b1, a2, b2)

## Arguments

batches	an n vector, consisting of the batch labels for each of the n samples.
a1	alpha of the first covariate distribution.
b1	beta of the first covariate distribution.
a2	alpha of the second covariate distribution.
b2	beta of the second covariate distribution.

## Value

an n vector, consisting of the covariate values for each of the n samples.

```
cb.sims.get_beta_overlap
```

Compute overlap of two beta distributions

## Description

Compute overlap of two beta distributions

## Usage

```
cb.sims.get_beta_overlap(a1, b1, a2, b2, nbreaks = 1000)
```

a1	alpha of the first covariate distribution.
b1	beta of the first covariate distribution.
a2	alpha of the second covariate distribution.
b2	beta of the second covariate distribution.
nbreaks	the number of breakpoints for approximating the covariate overlap.

the level of covariate overlap, corresponding to the AUC upper-bounded by the probability density functions for each of the beta distributions.

cb.sims.sim\_impulse Impulse Simulation

## Description

Impulse Simulation

#### Usage

```
cb.sims.sim_impulse(
    n = 100,
    pi = 0.5,
    eff_sz = 1,
    alpha = 2,
    unbalancedness = 1,
    err = 1/2,
    null = FALSE,
    a = -0.5,
    b = 1/2,
    c = 4,
    nbreaks = 200
)
```

n	the number of samples. Defaults to 100.
pi	the balance between the classes, where samples will be from group 1 with probability pi, and group 2 with probability 1 - pi. Defaults to 0.5.
eff_sz	the treatment effect between the different groups. Defaults to 1.
alpha	the alpha for the covariate sampling procedure. Defaults to 2.
unbalancedness	the level of covariate dissimilarity between the covariates for each of the groups. Defaults to 1.
err	the level of noise for the simulation. Defaults to 1/2.
null	whether to generate a null simulation. Defaults to FALSE. Same behavior can be achieved by setting $eff_{sz} = 0$ .
а	the first parameter for the covariate/outcome relationship. Defaults to -0.5.
b	the second parameter for the covariate/outcome relationship. Defaults to 1/2.
с	the third parameter for the covariate/outcome relationship. Defaults to 1.
nbreaks	the number of breakpoints for computing the expected outcome at a given co- variate level for each batch. Defaults to 200.

a list, containing the following:

Ys	an [n, 2] matrix, containing the outcomes for each sample. The first dimension contains the "treatment effect".
Ts	an [n, 1] matrix, containing the group/batch labels for each sample.
Xs	an [n, 1] matrix, containing the covariate values for each sample.
Eps	an [n, 1] matrix, containing the error for each sample.
x.bounds	the theoretical bounds for the covariate values.
Ytrue	an [nbreaks*2, 2] matrix, containing the expected outcomes at a covariate level indicated by Xtrue.
Ttrue	an [nbreaks*2,1] matrix, indicating the group/batch the expected outcomes and covariate breakpoints correspond to.
Xtrue	an [nbreaks*2, 1] matrix, indicating the values of the covariate breakpoints for the theoretical expected outcome in Ytrue.
Overlap	the theoretical degree of overlap between the covariate distributions for each of the two groups/batches.

#### Details

A sigmoidal relationship between the covariate and the outcome. The first dimension of the outcome is:

$$Y_i = c \times \phi(X_i, \mu = a, \sigma = b) - \text{eff\_sz} \times T_i + \frac{1}{2}\epsilon_i$$

where  $\phi(x, \mu, \sigma)$  is the probability density function for the normal distribution with mean  $\mu$  and standard deviation  $\sigma$ .

where the batch/group labels are:

 $T_i \stackrel{iid}{\sim} Bern(\pi)$ 

The beta coefficient for the covariate sampling is:

 $\beta = \alpha \times \text{unbalancedness}$ 

The covariate values for the first batch are:

$$X_i|T_i = 0 \stackrel{ind}{\sim} 2Beta(\alpha, \beta) - 1$$

and the covariate values for the second batch are:

$$X_i | T_i = 1 \stackrel{ind}{\sim} 2Beta(\beta, \alpha) - 1$$

Note that  $X_i|T_i = 0 \stackrel{D}{=} -X_i|T_i = 1$ , or that the covariates are symmetric about the origin in distribution.

Finally, the error terms are:

$$\epsilon_i \stackrel{iid}{\sim} Norm(0, \text{err}^2)$$

For more details see the help vignette: vignette("causal\_simulations", package = "causalBatch")

#### Author(s)

Eric W. Bridgeford

#### References

Eric W. Bridgeford, et al. "A Causal Perspective for Batch Effects: When is no answer better than a wrong answer?" Biorxiv (2024).

## Examples

library(causalBatch)
sim = cb.sims.sim\_impulse()

cb.sims.sim\_impulse\_asycov

Impulse Simulation with Asymmetric Covariates

## Description

Impulse Simulation with Asymmetric Covariates

#### Usage

```
cb.sims.sim_impulse_asycov(
    n = 100,
    pi = 0.5,
    eff_sz = 1,
    alpha = 2,
    unbalancedness = 1,
    null = FALSE,
    a = -0.5,
    b = 1/2,
    c = 4,
    err = 1/2,
    nbreaks = 200
)
```

n	the number of samples. Defaults to 100.
pi	the balance between the classes, where samples will be from group 1 with probability pi, and group 2 with probability 1 - pi. Defaults to 0.5.
eff_sz	the treatment effect between the different groups. Defaults to 1.
alpha	the alpha for the covariate sampling procedure. Defaults to 2.

unbalancedness	the level of covariate dissimilarity between the covariates for each of the groups. Defaults to 1.
null	whether to generate a null simulation. Defaults to FALSE. Same behavior can be achieved by setting $eff_sz = 0$ .
а	the first parameter for the covariate/outcome relationship. Defaults to -0.5.
b	the second parameter for the covariate/outcome relationship. Defaults to 1/2.
С	the third parameter for the covariate/outcome relationship. Defaults to 1.
err	the level of noise for the simulation. Defaults to 1/2.
nbreaks	the number of breakpoints for computing the expected outcome at a given co- variate level for each batch. Defaults to 200.

a list, containing the following:

Ys	an [n, 2] matrix, containing the outcomes for each sample. The first dimension contains the "treatment effect".
Ts	an [n, 1] matrix, containing the group/batch labels for each sample.
Xs	an [n, 1] matrix, containing the covariate values for each sample.
Eps	an [n, 1] matrix, containing the error for each sample.
x.bounds	the theoretical bounds for the covariate values.
Ytrue	an [nbreaks*2, 2] matrix, containing the expected outcomes at a covariate level indicated by Xtrue.
Ttrue	an [nbreaks*2,1] matrix, indicating the group/batch the expected outcomes and covariate breakpoints correspond to.
Xtrue	an [nbreaks*2, 1] matrix, indicating the values of the covariate breakpoints for the theoretical expected outcome in Ytrue.
Overlap	the theoretical degree of overlap between the covariate distributions for each of the two groups/batches.

#### Details

A sigmoidal relationship between the covariate and the outcome. The first dimension of the outcome is:

$$Y_i = c \times \phi(X_i, \mu = a, \sigma = b) - \text{eff\_sz} \times T_i + \frac{1}{2}\epsilon_i$$

where  $\phi(x, \mu, \sigma)$  is the probability density function for the normal distribution with mean  $\mu$  and standard deviation  $\sigma$ .

where the batch/group labels are:

 $T_i \stackrel{iid}{\sim} Bern(\pi)$ 

The beta coefficient for the covariate sampling is:

 $\beta = \alpha \times \text{unbalancedness}$ 

cb.sims.sim\_linear

The covariate values for the first batch are asymmetric, in that for the first batch:

$$X_i|T_i = 0 \stackrel{ind}{\sim} 2Beta(\alpha, \alpha) - 1$$

and the covariate values for the second batch are:

$$X_i|T_i = 1 \stackrel{ind}{\sim} 2Beta(\beta, \alpha) - 1$$

. .

Finally, the error terms are:

 $\epsilon_i \stackrel{iid}{\sim} Norm(0, \text{err}^2)$ 

For more details see the help vignette: vignette("causal\_simulations", package = "causalBatch")

#### Author(s)

Eric W. Bridgeford

#### References

Eric W. Bridgeford, et al. "A Causal Perspective for Batch Effects: When is no answer better than a wrong answer?" Biorxiv (2024).

#### Examples

library(causalBatch)
sim = cb.sims.sim\_impulse\_asycov()

cb.sims.sim\_linear Linear Simulation

#### Description

Linear Simulation

#### Usage

```
cb.sims.sim_linear(
    n = 100,
    pi = 0.5,
    eff_sz = 1,
    alpha = 2,
    unbalancedness = 1,
    err = 1/2,
    null = FALSE,
    a = -2,
    b = -1,
    nbreaks = 200
)
```

## Arguments

n	the number of samples. Defaults to 100.
pi	the balance between the classes, where samples will be from group 1 with prob- ability pi, and group 2 with probability 1 - pi. Defaults to 0.5.
eff_sz	the treatment effect between the different groups. Defaults to 1.
alpha	the alpha for the covariate sampling procedure. Defaults to 2.
unbalancedness	the level of covariate dissimilarity between the covariates for each of the groups. Defaults to 1.
err	the level of noise for the simulation. Defaults to 1/2.
null	whether to generate a null simulation. Defaults to FALSE. Same behavior can be achieved by setting $eff_sz = 0$ .
а	the first parameter for the covariate/outcome relationship. Defaults to -2.
b	the second parameter for the covariate/outcome relationship. Defaults to -1.
nbreaks	the number of breakpoints for computing the expected outcome at a given co- variate level for each batch. Defaults to 200.

## Value

a list, containing the following:

Ys	an [n, 2] matrix, containing the outcomes for each sample. The first dimension contains the "treatment effect".
Ts	an [n, 1] matrix, containing the group/batch labels for each sample.
Xs	an [n, 1] matrix, containing the covariate values for each sample.
Eps	an [n, 1] matrix, containing the error for each sample.
x.bounds	the theoretical bounds for the covariate values.
Ytrue	an [nbreaks*2, 2] matrix, containing the expected outcomes at a covariate level indicated by Xtrue.
Ttrue	an [nbreaks*2,1] matrix, indicating the group/batch the expected outcomes and covariate breakpoints correspond to.
Xtrue	an [nbreaks*2, 1] matrix, indicating the values of the covariate breakpoints for the theoretical expected outcome in Ytrue.
Overlap	the theoretical degree of overlap between the covariate distributions for each of the two groups/batches.

## Details

A linear relationship between the covariate and the outcome. The first dimension of the outcome is:

$$Y_i = a \times (X_i + b) - \text{eff\_sz} \times T_i + \frac{1}{2}\epsilon_i$$

where the batch/group labels are:

 $T_i \stackrel{iid}{\sim} Bern(\pi)$ 

The beta coefficient for the covariate sampling is:

$$\beta = \alpha \times \text{unbalancedness}$$

The covariate values for the first batch are:

$$X_i | T_i = 0 \stackrel{ind}{\sim} 2Beta(\alpha, \beta) - 1$$

and the covariate values for the second batch are:

$$X_i | T_i = 1 \stackrel{ind}{\sim} 2Beta(\beta, \alpha) - 1$$

Finally, the error terms are:

$$\epsilon_i \stackrel{iid}{\sim} Norm(0, \mathrm{err}^2)$$

For more details see the help vignette: vignette("causal\_simulations", package = "causalBatch")

#### Author(s)

Eric W. Bridgeford

#### References

Eric W. Bridgeford, et al. "A Causal Perspective for Batch Effects: When is no answer better than a wrong answer?" Biorxiv (2024).

## Examples

library(causalBatch)
sim = cb.sims.sim\_linear()

cb.sims.sim\_sigmoid Sigmoidal Simulation

#### Description

Sigmoidal Simulation

#### Usage

```
cb.sims.sim_sigmoid(
  n = 100,
  pi = 0.5,
  eff_sz = 1,
  alpha = 2,
  unbalancedness = 1,
  null = FALSE,
```

```
a = -4,
b = 8,
err = 1/2,
nbreaks = 200
)
```

## Arguments

n	the number of samples. Defaults to 100.
pi	the balance between the classes, where samples will be from group 1 with probability pi, and group 2 with probability 1 - pi. Defaults to 0.5.
eff_sz	the treatment effect between the different groups. Defaults to 1.
alpha	the alpha for the covariate sampling procedure. Defaults to 2.
unbalancedness	the level of covariate dissimilarity between the covariates for each of the groups. Defaults to 1.
null	whether to generate a null simulation. Defaults to FALSE. Same behavior can be achieved by setting $eff_sz = 0$ .
а	the first parameter for the covariate/outcome relationship. Defaults to -4.
b	the second parameter for the covariate/outcome relationship. Defaults to 8.
err	the level of noise for the simulation. Defaults to 1/2.
nbreaks	the number of breakpoints for computing the expected outcome at a given co- variate level for each batch. Defaults to 200.

## Value

a list, containing the following:

Υ	an [n, 2] matrix, containing the outcomes for each sample. The first dimension contains the "treatment effect".
Ts	an [n, 1] matrix, containing the group/batch labels for each sample.
Xs	an [n, 1] matrix, containing the covariate values for each sample.
Eps	an [n, 1] matrix, containing the error for each sample.
x.bounds	the theoretical bounds for the covariate values.
Ytrue	an [nbreaks*2, 2] matrix, containing the expected outcomes at a covariate level indicated by Xtrue.
Ttrue	an [nbreaks*2,1] matrix, indicating the group/batch the expected outcomes and covariate breakpoints correspond to.
Xtrue	an [nbreaks*2, 1] matrix, indicating the values of the covariate breakpoints for the theoretical expected outcome in Ytrue.
Overlap	the theoretical degree of overlap between the covariate distributions for each of the two groups/batches.

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#### Details

A sigmoidal relationship between the covariate and the outcome. The first dimension of the outcome is:

$$Y_i = a \times \text{sigmoid}(b \times X_i) - a - \text{eff\_sz} \times T_i + \frac{1}{2}\epsilon_i$$

where the batch/group labels are:

 $T_i \stackrel{iid}{\sim} Bern(\pi)$ 

The beta coefficient for the covariate sampling is:

$$\beta = \alpha \times \text{unbalancedness}$$

The covariate values for the first batch are:

$$X_i | T_i = 0 \stackrel{ind}{\sim} 2Beta(\alpha, \beta) - 1$$

and the covariate values for the second batch are:

$$X_i | T_i = 1 \stackrel{ind}{\sim} 2Beta(\beta, \alpha) - 1$$

Finally, the error terms are:

$$\epsilon_i \stackrel{iid}{\sim} Norm(0, \text{err}^2)$$

For more details see the help vignette: vignette("causal\_simulations", package = "causalBatch")

## Author(s)

Eric W. Bridgeford

#### References

Eric W. Bridgeford, et al. "A Causal Perspective for Batch Effects: When is no answer better than a wrong answer?" Biorxiv (2024).

#### Examples

```
library(causalBatch)
sim = cb.sims.sim_sigmoid()
```

covariate.match

#### Description

Pairwise covariate matching

## Usage

```
covariate.match(covar.tx, covar.cont, match.form, match.args = NULL)
```

#### Arguments

covar.tx	the treatment covariate/label matrix.
covar.cont	the control covariate/label matrix.
match.form	A formula of columns from Xs, to be passed directly to matchit for subsequent matching. See formula argument from matchit for details.
match.args	A named list arguments for the matchit function, to be used to specify specific matching strategies, where the list names are arguments and the corresponding values the value to be passed to matchit.

#### Value

a list containing:

- I.mat.k index matrix of control samples that have a match.
- M.mat.k match matrix of treatment samples that are correspondingly matched to a control.

ohe

A utility to one-hot encode a treatment vector.

## Description

A utility to one-hot encode a treatment vector.

#### Usage

ohe(Ts)

## Arguments

Ts

[n] the labels of the samples, with K < n levels, as a factor variable.

#### Value

[n, K] a one-hot encoding of Ts.

## sigmoid

## Author(s)

Eric W. Bridgeford

sigmoid	Sigmoid function
Description	
Sigmoid function	
Usage	
sigmoid(x)	
Arguments	
Х	the value
alue	
sigmoid(x)	
zero_one_dist	A utility to compute the zero-one distances for a treatment vector.

## Description

A utility to compute the zero-one distances for a treatment vector.

## Usage

```
zero_one_dist(Ts)
```

#### Arguments

Ts [n] the labels of the samples, with K < n levels, as a factor variable.

## Value

[n, n] the pairwise zero-one distance matrix.

#### Author(s)

Eric W. Bridgeford

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